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# **THERMODYNAMICS**

OF THE

# STEAM-ENGINE

AND

OTHER HEAT-ENGINES

ВY

CECIL H. PEABODY

PROFESSOR OF NAVAL ARCHITECTURE AND MARINE ENGINEERING,
MASSACHUSETTS INSTITUTE OF TECHNOLOGY

FIFTH EDITION, REWRITTEN
SECOND THOUSAND

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#### PREFACE TO FIFTH EDITION.

When this work was first in preparation the author had before him the problem of teaching thermodynamics so that students in engineering could use the results immediately in connection with experiments in the Engineering Laboratories of the Massachusetts Institute of Technology. The acceptance of the book by teachers of engineering appears to justify its general plan, which will be adhered to now that the development of engineering calls for a complete revision.

The author is still of the opinion that the general mathematical presentation due to Clausius and Kelvin is most satisfactory and carries with it the ability to read current thermodynamic investigations by engineers and physicists. At the same time it is recognized that recent investigations of superheated steam are presented in such a way as to narrow the applications of the general method so that there is justification for those who prefer special methods for those applications. To provide for both views of this subject, the general mathematical discussion is presented in a separate chapter, which may be omitted at the first reading (or altogether), provided that the special methods, which also are given in the proper places, are taken to be sufficient.

The first edition presented fundamental data not generally accepted at that time, so that it was considered necessary to justify the data by giving the derivation at length; much of this matter, which is no longer new, is removed to an appendix, to relieve the student of discussions that must appear unnecessary and tedious.

The introduction of the steam-turbine has changed adiabatic calculations for steam, from an apparent academic abstraction, to a common necessity. To meet this changed condition, the Tables of

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University Libraries Carnegie Mellon University Pittsburgh PA 15213-3890 Properties of Saturated Steam have had added to them columns of entropies of vaporization; and further there has been computed a table of the quality (or dryness factor) the heat contents and volume at constant entropy, for each degree Fahrenheit. This table will enable the computer to determine directly the effect of adiabatic expansion to any pressure or volume, and to calculate with ease the external work in a cylinder or the velocity of flow through an orifice or nozzle including the effect of friction; and also to determine the distribution of work and pressure for a steam-turbine. For the greater part of practical work this table may be used without interpolation, or by interpolation greater refinement may be had.

Advantage is taken of recent experiments on the properties of superheated steam and of the application to tests on engines to place that subject in a more satisfactory condition. Attention is also given to the development of internal combustion engines and to the use of fuel and blast-furnace gas. A chapter is given on the thermodynamics of the steam-turbine with current method of computation, and results of tests.

So far as possible the various chapters are made independent, so that individual subjects, such as the steam-engine, steam-turbine, compressed-air and refrigerating machines, may be read separately in the order that may commend itself.

## PREFACE TO FIRST EDITION.

This work is designed to give instruction to students in technical schools in the methods and results of the application of thermodynamics to engineering. While it has been considered desirable to follow commonly accepted methods, some part differ from other text-books, either in substance or in manner of presentation, and may require a few words of explanation.

The general theory or formal presentation of thermodynamic

is that employed by the majority of writers, and was prepared with the view of presenting clearly the difficulties inherent in the subject, and of giving familiarity with the processes employed.

In the discussion of the properties of gases and vapors the original experimental data on which the working equations, whether logical or empirical, must be based are given quite fully, to afford an idea of the degree of accuracy attainable in calculations made with their aid. Rowland's determination of the mechanical equivalent of heat has been adopted, and with it his determination of the specific heat of water at low temperatures. The author's "Tables of the Properties of Saturated Steam and Other Vapors" were calculated to accompany this work, and may be considered to be an integral part of it.

The chapters on the flow of gases and vapors and on the injector are believed to present some novel features, especially in the comparisons with experiments.

The feature in which this book differs most from similar works is in the treatment of the steam-engine. It has been deemed advisable to avoid all approximate theories based on the assumption of adiabatic changes of steam in an engine cylinder, and instead to make a systematic study of steamengine tests, with the view of finding what is actually known on the subject, and how future investigations and improvements may be made. For this purpose a large number of tests have been collected, arranged, and compared. Special attention is given to the investigations of the action of steam in the cylinder of an engine, considerable space being given to Hirn's researches and to experiments that provide the basis for them. Directions are given for testing engines, and for designing simple and compound engines.

Chapters have been added on compressed-air and refrigerating machines, to provide for the study of these important subjects in connection with the theory of thermodynamics.

Wherever direct quotations have been made, references have been given in foot-notes, to aid in more extended investigations. It does not appear necessary to add other acknowledgment of assistance from well-known authors, further than to say that their writings have been diligently searched in the preparation of this book, since any text-book must be largely an adaptation of their work to the needs of instruction.

C. H. P.

Massachusetts Institute of Technology, May, 1889.

## PREFACE TO FOURTH EDITION.

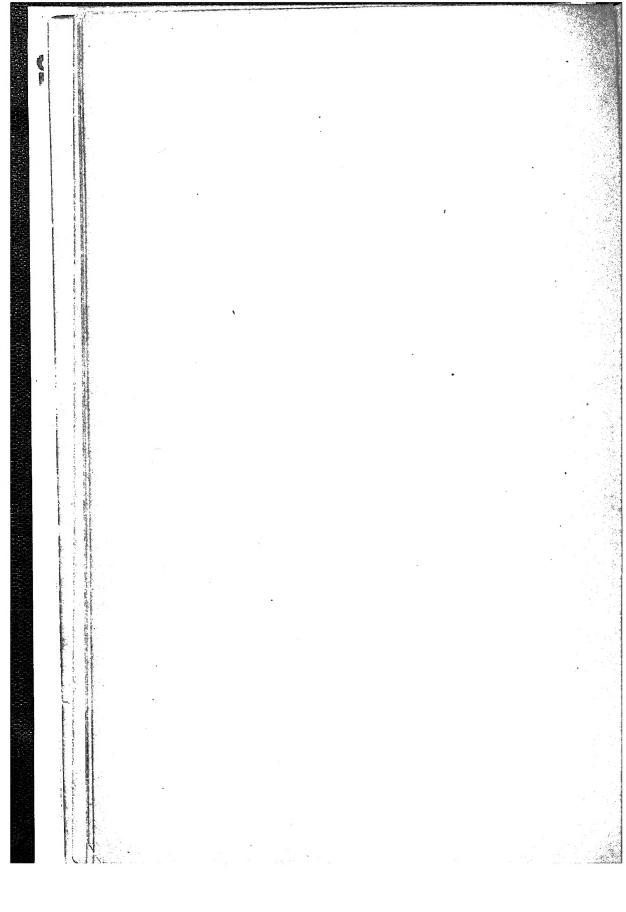
A THOROUGH revision of this work has been made to bring it into accord with more recent practice and to include later experimental work. Advantage is taken of this opportunity to make changes in matter or in arrangement which it is believed will make it more useful as a text-book.

C. H. P.

Massachusetts Institute of Technology July, 1898.

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### THERMODYNAMICS OF THE STEAM-ENGINE.

#### CHAPTER I.

#### THERMAL CAPACITIES.

THE object of thermodynamics, or the mechanical theory of heat, is the solution of problems involving the action of heat, and, for the engineer, more especially those problems presented by the steam-engine and other thermal motors. The substances in which the engineer has the most interest are gases and vapors, more especially air and steam. Fortunately an adequate treatment can be given of these substances for engineering purposes.

First General Principle. — In the development of the theory of thermodynamics it is assumed that if any two characteristics or properties of a substance are known these two, treated as independent variables, will enable us to calculate any third property.

As an example, we have from the combination of the laws of Boyle and Gay-Lussac the general equation for gases,

in which p is the pressure, v is the volume, T is the absolute temperature by the air-thermometer, and R is a constant which for air has the value 53.35 when English units are used. It is probable that this equation led to the general assumption just quoted. That assumption is purely arbitrary, and is to be justified by its results. It may properly be considered to be the first general principle of the theory of thermodynamics; the other two general principles are the so-called first and second laws of thermodynamics, which will be stated and discussed later.

Characteristic Equation. — An equation which gives the relations of the properties of any substance is called the characteristic equation for that substance. The properties appearing in a characteristic equation are commonly pressure, volume and temperature, but other properties may be used if convenient The form of the equation must be determined from experiment either directly or indirectly.

The characteristic equation for a gas is, as already quote

$$pv = RT$$
.

The characteristic equation for an imperfect gas, like superheated steam, is likely to be more complex; for example, the equation given by Knoblauch, Linde, and Klebe is

$$pv = BT - p(1 + ap) \left[ C \left( \frac{373}{T} \right)^3 - D \right].$$

On the other hand, the properties of saturated steam, especial if mixed with water, cannot be represented by a single equation

Specific Pressure. — The pressure is assumed to be a hydrostatic pressure, such as a fluid exerts on the sides of the containing vessel or on an immersed body. The pressure consequently the pressure exerted by the substance under consideration rather than the pressure on that substance. It example, in the cylinder of a steam-engine the pressure of steam is exerted on the piston during the forward stroke a does work on the piston; during the return stroke, when steam is expelled from the cylinder, it still exerts pressure the piston and abstracts work from it.

For the purposes of the general theory pressures expressed in terms of pounds on the square foot for the Engl system of units. In the metric system the pressure is expres in terms of kilograms on the square metre. A pressure t expressed is called the *specific pressure*. In engineering prac other terms are used, such as pounds on the square inch, inc of mercury, millimetres of mercury, atmospheres, or kilogra on the square centimetre.

Specific Volume. — It is convenient to deal with one unit of weight of the substance under discussion, and to consider the volume occupied by one pound or one kilogram of the substance; this is called the *specific volume*, and is expressed in cubic feet or in cubic metres. The specific volume of air at freezing-point and under the normal atmospheric pressure is 12.39 cubic feet; the specific volume of saturated steam at 212° F. is 26.6 cubic feet; and the specific volume of water is about  $\frac{1}{62.4}$ , or nearly 0.016 of a cubic foot.

Temperature is commonly measured by aid of a mercurial thermometer which has for its reference-points the freezing-point and boiling-point of water. A centigrade thermometer has the volume of the stem between the reference-points divided into one hundred equal parts called degrees. The Fahrenheit thermometer differs from the centigrade in having one hundred and eighty degrees between the freezing-point and the boiling-point, and in having its zero thirty-two degrees below freezing.

The scale of a mercurial thermometer is entirely arbitrary, and its indications depend on the relative expansion of glass and mercury. Indications of such thermometers, however carefully made, differ appreciably, mainly on account of the varying nature of the glass. For refined investigations thermometric readings are reduced to the air-thermometer, which has the advantage that the expansion of air is so large compared with the expansion of glass that the latter has little or no effect.

It is convenient in making calculations of the properties of air to refer temperatures to the absolute zero of the scale of the air-thermometer. To get a conception of what is meant by this expression we may imagine the air-thermometer to be made of a uniform glass tube with a proper index to show the volume of the air. The position of the index may be marked at boiling-point and at freezing-point as on the mercurial thermometer, and the space between may be divided into one hundred parts or degrees. If the graduations are continued to the closed end of the tube there will be found to be 273 of them. It will be

shown later that there is reason to suppose that the absolute zero of temperature is 273° centigrade below the freezing-point of water. Speculations as to the meaning of absolute zero and discussions concerning the nature of substances at that temperature are not now profitable. It is sufficient to know that equations are simplified and calculations are facilitated by this device. For example, if temperature is reckoned from the arbitrary zero of the centigrade thermometer, then the characteristic equation for a perfect gas becomes

$$pv = \left(\frac{1}{\alpha} + t\right)R,$$

in which  $\alpha$  is the coefficient of dilatation and  $\frac{I}{\alpha} = 273$  nearly.

In order to distinguish the absolute temperature from the temperature by the thermometer we shall designate the former by T and the latter by t, bearing in mind that

$$T = t + 273^{\circ}$$
 centigrade,  
 $T = t + 459.5$  Fahrenheit.

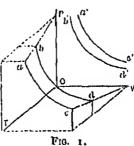
Physicists give great weight to the discussion of a scale of temperature that can be connected with the fundamental units of length and weight like the foot and the pound. Such a scale, since it does not depend on the properties of any substance (glass, mercury, or air), is considered to be the absolute scale of temperature. The differences between such a scale and the scale of the air-thermometer are very small, and are difficult to determine, and for the engineer are of little moment. At the proper place the conception of the absolute scale can be easily stated.

Graphical Representation of the Characteristic Equation.—
Any equation with three variables may be represented by a geometrical surface referred to co-ordinate axes, of which surface the variables are the co-ordinates. In the case of a perfect gas which conforms to the equation

$$pv = RT$$

the surface is such that each section perpendicular to the axis of T is a rectangular hyperbola (Fig. 1).

Returning now to the general case, it is apparent that the characteristic equation of any substance may be represented by a geometrical surface referred to co-ordinate axes, since the equation is assumed to contain only three variables; but the surface will in general be less simple in form than that representing the combined laws of Boyle and Gay-Lussac.



If one of the variables, as T, is given a special constant value, it is equivalent to taking a section perpendicular to the axis of T; and a plane curve will be cut from the surface, which may be conveniently projected on the (p, v) plane. The reason for choosing the (p, v) plane is that the curves correspond with those drawn by the steam-engine indicator.

Considerable use is made of such thermal curves in explaining thermodynamic conceptions. As a rule, a graphical process or representation is merely another way of presenting an idea that has been, or may be, presented analytically; there is, however, an advantage in representing a condition or a change to the eye by a diagram, especially in a discussion which appears to be abstract. A number of thermal curves are explained on page 16.

Standard Temperature. — For many purposes it is convenient to take the freezing-point of water for the standard temperature, since it is one of the reference-points on the thermometric scale; this is especially true for air. But the properties of water change rapidly at and near freezing-point and are very imperfectly known. It has consequently become customary to take 62° F, for the standard temperature for the English system of units; there is a convenience in this, inasmuch as the pound and yard are standards at that temperature. For the metric system 15° C, is used, though the kilogram and metre are standards at freezing-point.

thermal units (B. T. U.). A British thermal unit is the required to raise one pound of water from 62° F. to 63' like manner a calorie is the heat required to raise one k of water from 15° C. to 16° C.

Specific Heat is the number of thermal units required a unit of weight of a given substance one degree of temperature course, unity.

If the specific heat of a given substance is constant, theat required to raise one pound through a given range perature is the product of the specific heat by the incretemperature. Thus if c is the specific heat and  $t-t_1$  is the of temperature the heat required is

$$Q = c (t - t_1)$$
, and  $c = \frac{Q}{t - t_1}$ .

If the specific heat varies the amount of heat must be of by integration — that is,

$$Q = \int c dt,$$

and conversely

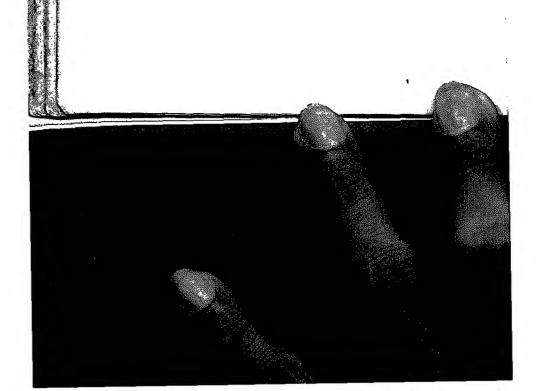
$$c = \frac{dQ}{dt}.$$

It is customary to distinguish two specific heats for gases; specific heat at constant pressure and specific I constant volume, which may be represented by

$$c_p = \left(\frac{\delta Q}{\delta t}\right)_p$$
 and  $c_v = \left(\frac{\delta Q}{\delta t}\right)_v$ ;

the subscript attached to the parenthesis indicates the pu which is constant during the change. It is evident the specific heats just expressed are partial differential coeffice

Latent Heat of Expansion is the amount of heat requirerease the volume of a unit of weight of the substance



cubic foot, or one cubic metre, at constant temperature. It may be represented by

 $l = \left(\frac{\delta Q}{\delta v}\right)_{l}$ 

Thermal Capacities. — The two specific heats and the latent heat of expansion are known as thermal capacities. It is customary to use three other properties suggested by those just named which are represented as follows:

$$m = \left(\frac{\delta Q}{\delta p}\right)_i$$
;  $n = \left(\frac{\delta Q}{\delta p}\right)_v$  and  $o = \left(\frac{\delta Q}{\delta v}\right)_p$ .

The first represents the amount of heat that must be applied to one pound of a substance (such as air) to increase the pressure by the amount of one pound per square foot at constant temperature; this property is usually negative and represents the heat that must be abstracted to prevent the temperature from rising. The other two can be defined in like manner if desired, but it is not very important to state the definitions nor to try to gain a conception as to what they mean, as it is easy to express them in terms of the first three, for which the conceptions are not difficult. They have no names assigned to them, which is, on the whole, fortunate, as, of the first three, two have names that have no real significance, and the third is a misnomer.

General Equations of the Effects Produced by Heat. — In order to be able to compute the amount of heat required to produce a change in a substance by aid of the characteristic equation, it is necessary to admit that there is a functional relation between the heat applied and some two of the properties that enter into the characteristic equation. It will appear later in connection with the discussion of the first law of thermodynamics that an integral equation cannot in general be written directly, but we may write a differential equation in one of the three following forms:

$$dQ = \left(\frac{\delta Q}{\delta l}\right)_{\nu} dl + \left(\frac{\delta Q}{\delta \nu}\right)_{l} d\nu,$$

$$dQ = \left(\frac{\delta Q}{\delta t}\right)_{p} dt + \left(\frac{\delta Q}{\delta p}\right)_{t} dp,$$

$$dQ = \left(\frac{\delta Q}{\delta p}\right)_{v} dp + \left(\frac{\delta Q}{\delta v}\right)_{p} dv,$$

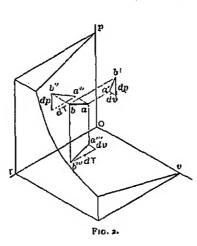
or substituting for the partial differential coefficients the letters which have been selected to represent them,

$$dQ = c_v dt + l dv \qquad . \qquad . \qquad . \qquad . \qquad . \qquad . \qquad (1)$$

$$dQ = c_v dt + l dv . . . . (1)$$

$$dQ = c_p dt + m dp . . . . (2)$$

$$dQ = ndp + odv \qquad . \qquad . \qquad . \qquad . \qquad . \qquad (3)$$



This matter may perhaps be clearer if it is presented graphically as in Fig. 2, where ab is intended to represent the path of a point on the characteristic surface in consequence of the addition of the heat dQ. There will in general be a change of temperature volume and pressure as indicated on the figure.

Now the path ab, which for a small change may be considered to be a straight line, will be projected on

the three planes at a'b', a"b" and a"b". The projection on the (v,T) plane may be resolved into the components  $\delta v$  and  $\delta T$ ; the first represents a change of volume at constant temperature requiring the heat ldv, and the second represents a change of temperature at constant volume requiring the heat c.dt. quently the heat required for the change in terms of the volume and temperature is

$$dO = c_v dt + \iota dv$$
.



Relations of the Thermal Capacities. — The three equations (1), (2), and (3), show the changes produced by the addition of an amount of heat dQ to a unit of weight of a substance, the difference coming from the methods of analyzing the changes. We may conveniently find the relations of the several thermal capacities by the method of undetermined coefficients. Thus equating the right-hand members of equations (1) and (2),

From the characteristic equation we shall have in general

$$v = F(p, T),$$

as, for example, for air we have

$$v = \frac{RT}{b}$$
,

and consequently we may write

$$dv = \frac{\delta v}{\delta t} dt + \frac{\delta v}{\delta p} dp,$$

which substituted in equation (4) gives,

$$c_{p}dt + mdp = c_{p}dt + l\left(\frac{\delta v}{\delta l}dt + \frac{\delta v}{\delta p}dp\right).$$

$$\therefore c_{p}dt - mdp = \left(c_{p} + l\frac{\delta v}{\delta l}\right)dt + l\frac{\delta v}{\delta p}dp. \qquad (5)$$

It will be noted that, as T differs from t only by the addition of a constant, the differential dt may be used in all cases, whether we are dealing with absolute temperatures, or temperatures on the ordinary thermometer.

In equation (5) p and T are independent variables, and each may have all possible values; consequently we may equate like coefficients.

Also, equating the remaining coefficients,

$$l\frac{\delta v}{\delta p} = m \cdot . \cdot . \cdot (7)$$

If the characteristic equation is solved for the pressure we shall have

 $p = F_1(T, v),$ 

so that

$$dp = \frac{\delta p}{\delta t} dt + \frac{\delta p}{\delta v} dv . . . . . . . (8)$$

which substituted in equation (4) gives

$$c_v dt + m \left( \frac{\delta p}{\delta t} dt + \frac{\delta p}{\delta v} dv \right) = c_v dt + l dv.$$

$$\therefore \left(\epsilon_p + m \frac{\delta p}{\delta l}\right) dl + m \frac{\delta p}{\delta v} dv = \epsilon_v dl + l dv.$$

Equating like coefficients,

$$c_p + m \frac{\delta p}{\delta l} = c_p \dots \qquad (9)$$

$$-m\frac{\delta p}{\delta t}=c_p-c_v . . . . (10)$$

From equations (2) and (3)

$$c_p dt + m dp = n dp + o dv \qquad . \qquad . \qquad . \qquad . \qquad . \qquad (11)$$

and from an equation

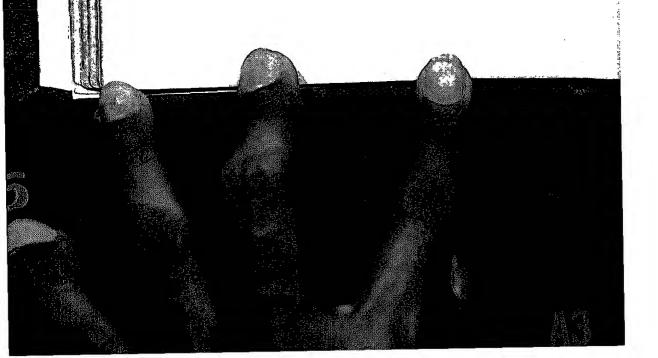
$$T = F_2(v, p)$$
$$dt = \frac{\delta t}{\delta v} dv + \frac{\delta t}{\delta p} dp;$$

which latter substituted in equation (11) gives

$$c_p \frac{\delta_l}{\delta_v} dv + c_p \frac{\delta_l}{\delta_p} dp + mdp = ndp + odv.$$

Equating coefficients of dv,

$$o = c_p \frac{\delta t}{\delta v} \quad . \quad . \quad . \quad . \quad (12)$$



Finally, from equations (1) and (3),

Substituting for dt as above,

$$c_v \frac{\delta l}{\delta v} dv + c_v \frac{\delta l}{\delta p} dp + l dv = n dp + o dv.$$

Equating coefficients of dp,

$$n = c_v \frac{\delta_l}{\delta \rho} \quad . \quad . \quad . \quad . \quad . \quad (14)$$

For convenience the several relations of the thermal capacities may be assembled as follows:

$$l = (c_p - c_v) \frac{\partial l}{\partial v}; \qquad m = -(c_p - c_o) \frac{\partial l}{\partial p}$$

$$n = c_v \frac{\delta l}{\delta p}; \quad o = c_p \frac{\delta l}{\delta v}$$

$$m = l \frac{\delta v}{\delta p}.$$

They are the necessary algebraic relations of the literal functions growing out of the first general principle, and are independent of the scale of temperature, or of any other theoretical or experimental principle of thermodynamics other than the one already stated — namely, that any two properties of a given substance, treated as independent variables, are sufficient to allow us to calculate any third property.

Of the six thermal capacities the specific heat at constant pressure is the only one that is commonly known by direct experiment. For perfect gases this thermal capacity is a constant, and, further, the ratio of the specific heats

is a constant, so that c, is readily calculated. The relations of the thermal capacities allow us to calculate values for the other thermal capacities, *l*, *m*, *n*, and *o*, provided that we first determine the several partial differential coefficients will appear in the proper equations. But for a perfect gas characteristic equation is

$$pv = RT$$

from which we have

$$\frac{\delta v}{\delta l} = \frac{R}{p}; \quad \frac{\delta p}{\delta l} = \frac{R}{v};$$

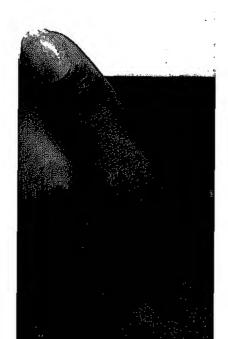
$$\frac{\delta t}{\delta p} = \frac{v}{R}; \quad \frac{\delta t}{\delta v} = \frac{p}{R}.$$

Substituting these values in the equations for the the capacities, we have

$$l = \frac{p}{R}(c_p - c_v); \quad -m = \frac{v}{R}(c_p - c_v);$$

$$n = \frac{v}{R}c_v; \quad o = \frac{p}{R}c_p;$$

by aid of which the several thermal capacities may be calcul numerically, or, what is the usual procedure, may be represe in terms of the specific heats.



#### CHAPTER II.

#### FIRST LAW OF THERMODYNAMICS.

Tire formal statement of the first law of thermodynamics is:

Heat and mechanical energy are mutually convertible, and
heat requires for its production and produces by its disappearance
a definite number of units of work for each thermal unit.

This law, which may be considered to be the second general principle of thermodynamics, is the statement of a well-determined physical fact. It is a special statement of the general law of the conservation of energy, i.e., that energy may be transformed from one form to another, but can neither be created nor destroyed. It should be stated, however, that the general law of conservation of energy, though universally accepted, has not been proved by direct experiment in all cases; there may be cases that are not susceptible of so direct a proof as we have for the transformation of heat into work.

The best determinations of the mechanical equivalent of heat were made by Rowland, whose work will be considered in detail in connection with the properties of steam and water. From his work it appears that 778 foot-pounds of work are required to raise one pound of water from 62° to 63° Fahrenheit; this value of the mechanical equivalent of heat is now commonly accepted by engineers, and is verified by the latest determinations by Joule and other experimenters.

The values of the mechanical equivalent of heat for the English system and for the metric system are:

1 B. T. U. = 778 foot-pounds.
1 calorie = 426.9 metre-kilograms.

This physical constant is commonly represented by the letter J; the reciprocal is represented by A.

monly quoted as 772 for the English system and 424 for the metric system. The error of these values is about one per cent.

Effects of the Transfer of Heat. — Let a quantity of any substance of which the weight is one unit - i.e., one pound or one kilogram — receive a quantity of heat dQ. It will, in general, experience three changes, each requiring an expenditure of energy. They are: (1) The temperature will be raised, and, according to the theory that sensible heat is due to the vibrations of the particles of the body, the kinetic energy will be increased. Let dS represent this change of sensible heat or vibration work expressed in units of work. (2) The mean positions of the particles will be changed; in general the body will expand. Let d1 represent the units of work required for this change of internal potential energy, or work of disgregation. (3) The expansion indicated in (2) is generally against an external pressure, and to overcome the same — that is, for the change in external potential energy - there will be required the work dW.

If during the transmission no heat is lost, and if no heat is transformed into other forms of energy, such as sound, electricity, etc., then the first law of thermodynamics gives

$$dQ = A(dS + dI + dW) \quad . \quad . \quad . \quad (15)$$

It is to be understood that any or all of the terms of the equation may become zero or may be negative. If all the terms become negative heat is withdrawn instead of added, and dQ is negative. It is not easy to distinguish between the vibrationwork and the disgregation work, and for many purposes it is unnecessary; consequently they are treated together under the name of intrinsic energy, and we have

$$dQ = A(dS + dI + dW) = A(dE + dW)$$
 . . (16)

The inner work, or intrinsic energy, depends on the state of the body, and not at all on the manner by which it arrived at



ence to a given plane consisting of kinetic energy and potential energy, depends on the velocity of the body and the height above the plane, and not on the previous history of the body.

The external work is assumed to be done by a fluid-pressure; consequently

$$dW = pdv . . . . . . . . (17)$$

where  $v_2$  and  $v_1$  are the final and initial volumes.

In order to find the value of the integral v in equation (18) it is necessary to know the manner in which the pressure varies with the volume. Since the pressure may vary in different ways, the external work cannot be determined from the initial and final states of the body; consequently the heat required to effect a change from one state to another depends on the manner in which the change is effected.

Assuming the law of the variation of the pressure and volume to be known, we may integrate thus:

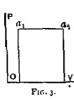
$$Q = A \left( E_3 - E_1 + \int_{v_1}^{v_2} p dv \right) . . . . (19)$$

In order to determine E for any state of a body it would be necessary to deprive it entirely of vibration and disgregation energy, which would of course involve reducing it to a state of absolute cold; consequently the direct determination is impossible. However, in all our work the substances operated on are changed from one state to another, and in each state the intrinsic energy depends on the state only; consequently the change of intrinsic energy may be determined from the initial and final states only, without knowing the manner of change from one to the other.

In general, equations will be arranged to involve differences

vibration and disgregation work avoided.

Thermal Lines. — The external work can be determined only when the relations of p and v are known, or, in general, when the characteristic equation is known. It has already been shown that in such case the equation may be represented by a geometrical surface, on which so-called thermal lines can be drawn representing the properties of the substance under consideration. These lines are commonly projected on the (p, v) plane. It is convenient in many cases to find the relation of p and v under a given condition and represent it by a curve drawn directly on the (p, v) plane.



Lines of Equal Pressure. — The change of condition takes place at constant pressure, and consists of a change of volume, as represented in Fig. 3. The tracing-point moves from  $a_1$  to  $a_2$ , and the volume changes from  $v_1$  to  $v_2$ . The work done is represented by the rectangular area under  $a_1a_2$ , or by

$$W = p \int_{v_1}^{v_2} dv = p(v_2 - v_1) \quad . \quad . \quad . \quad (20)$$

During the change the temperature may or may not change; the diagram shows nothing concerning it.

Lines of Equal Volume. — The pressure increases at constant volume, and the tracing-point moves from  $a_1$  to  $a_2$ . The temperature usually increases meanwhile. Since dv is zero,

$$W = \int_{v_1}^{v_2} p dv = 0$$
 . . . (21)

Isothermal Lines, or Lines of Equal Temperature. — The temperature remains constant, and a line is drawn, usually convex, toward the axis OV. The pressure of a mixture of a



figure and its vapor is constant for a given temperature; consequently the isothermal for such a mixture is a line of equal pressure, represented by Fig. 3. The isothermal of a perfect gas, on the other hand, is an equilateral hyperbola, as appears from the law of Boyle, which may be written

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$$pv = C.$$

Isodynamic or Isoenergic Lines are lines representing changes during which the intrinsic energy remains constant. Consequently all the heat received is transformed into external work. It will be seen later that the isodynamic and isothermal lines for a gas are the same.

Adiabatic Lines. - A very important problem in thermodynamics is to determine the behavior of a substance when a change of condition takes place in a non-conducting vessel. During the change -- for example, an increase of volume or expansion — some of the heat in the substance may be changed into work; but no heat is transferred to or from the substance through the walls of the containing vessel. Such changes are called adiabatic changes.

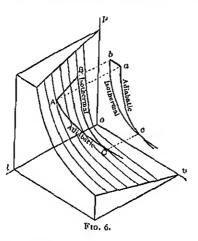
Very rapid changes of dry air in the cylinder of an air-compressor or a compressed-air engine are very nearly adiabatic. Adiabatic changes never occur in the cylinder of a steam-engine on account of the rapidity with which steam is condensed on or vaporized from the cast-iron walls of the cylinder.

Since there is no transmission of heat to (or from) the working substance, equation (19) becomes

$$Q = A(E_2 - E_1 + \int_{v_1}^{v_2} p dv) . . . . (22)$$

that is, the external work is done wholly at the expense of the intrinsic energy of the working substance, as must be the case in conformity with the assumption of an adiabatic change.

Relation of Adiabatic and Isothermal Lines. — An important property of adiabatic lines can be shown to advantage at this



place, namely, that such a line is steeper than an isothermal line on the (p, v) plane where they cross, as represented in Fig. 6. The essential feature of adiabatic expansion is that no heat is supplied and that consequently the external work of expansion is done at the expense of the intrinsic energy which consequently decreases. The intrinsic energy is the sum of the vibration energy and the disgregation energy, both of

which in general decrease during an adiabatic expansion; in particular the decrease of vibration energy means a loss of temperature. Conversely an adiabatic compression is accompanied by an increase of temperature. If an isothermal compression is represented by cb, then an adiabatic compression will be represented by a steeper line like ca, crossing the constant pressure line ba to the right of b, and thus indicating that at that pressure there is a greater volume, as must be the case for a body which expands during a rise of temperature at constant pressure.

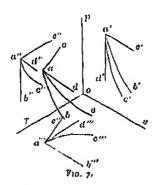
It is very instructive to note the relation of these lines on the surface which represents the characteristic equation for a perfect gas. In Fig. 6, which is an isometric projection, the general form of the surface can be recognized from the following conditions:—a horizontal section representing constant pressure cuts the surface in a straight line which indicates that the volume increases proportionally to the absolute temperature, and this line is projected as a horizontal line on the (p, v) plane; a vertical section parallel to the (p, t) plane shows that the pressure in this case increases as the absolute temperature, and the line of intersection with the surface is projected as a vertical line on the



(p, v) plane; finally vertical sections parallel to the (p, v) plane are rectangular hyperbolæ which are projected in their true form on the (p, v) plane. If AC is an adiabatic curve on the characteristic surface, its loss of temperature is properly represented by the fact that it crosses a series of isothermals in passing from A to C; AB is a line of constant pressure showing a decrease of temperature between the isothermals through A and through C; finally the projection of ABC on to the (p, v) plane shows that the adiabatic line ac is steeper than the isothermal line bc. Attention should be called to the fact that the first statement of this relation is the more general as it holds for all substances that expand with rise of temperature at constant pressure whatever may be the form of the characteristic equation.

Thermal Lines and their Projections. — The treatment given of thermal lines is believed to be the simplest and to present the features that are most useful in practice. There is, however, both interest and instruction in considering their relation in space and their projections on the three thermal planes. It is well to look attentively at Fig. 6, which is a correct isometric projection of the characteristic surface of a gas following the law of Boyle and Gay-Lussac, noting that every section by a

plane parallel to the (p, v) plane is a rectangular hyperbola which has the same form in space and when projected on the (p, v) plane. The sections by a plane parallel to the (p, t) plane are straight lines and are of course projected as straight lines on that plane and on the (p, v) plane; in like manner the sections by planes parallel to the (t, v) plane are straight lines. The adiabatic line in space



and as projected on the (p, v) plane is probably drawn a little too steep, but the divergence from truth is not evident to the eye.

In Fig. 7 the same method of projection is used, but other lines are added together with their projections on the several

isothermal which is projected as a rectangular hyperbol on the (p, v) plane, and as straight lines a''b'' and a'''l the (p, t) and (l, v) plane. The adiabatic line ac is s than the isothermal, both in space and on the (p, v) pla already explained; it is projected as a curve (a''c'' or a'''c' the other planes. The section showing constant pressi represented in space by the straight line ae which project the (p, t) plane is parallel to the axis ot, and on the plane is parallel to the line itself in space; on the (p, v) plan horizontal, as shown in Fig. 3. In much the same way ad section by a plane parallel to the (t, v) plane, and a''d', and a'''d''' are its projections.

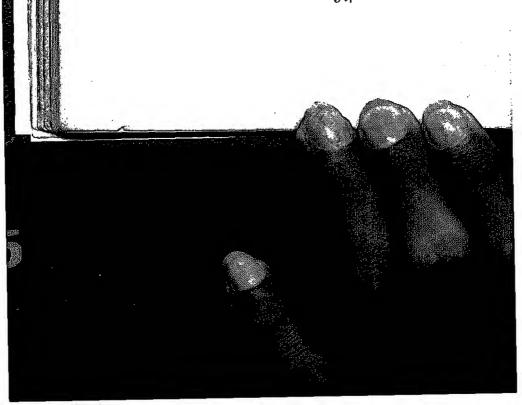
Graphical Representations of Change of Intrinsic Energy Professor Rankine first used a graphical method of represe a change of intrinsic energy, employing adiabatic lines on follows:

Suppose that a substance is originally in the state A (Figura 1) and that it expands adiabatically; then the external work is at the expense of the intrinsic energy; hence if the expansa has proceeded to  $A_1$  the area  $AA_1a_1a$ , which represents external work, also represents the change of intrinsic en Suppose that the expansion were to continue indefinitely;

the adiabatic will approach the axis indefinitely, and the area representing work will be included between the curve produced indefinitely, the ordinate Aa, the axis OV; this area will represent al work that can be obtained by the expan of the substance; and if it be admitted

during the expansion all the intrinsic energy is transformation work, so that at the end the intrinsic energy is zero, it resents also the intrinsic energy. In cases for which the etion of the adiabatic can be found it is easy to show that

$$E_1 = \int_{v_1}^{\infty} p dv \quad . \quad . \quad . \quad .$$



is a finite quantity; and in any case, if we admit an absolute zero of temperature, it is evident that the intrinsic energy cannot be infinite. On the other hand, if an isothermal curve were treated in the same way the area would be infinite, since heat would be continually added during the expansion.

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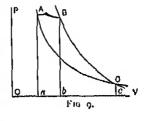
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Now suppose the body to pass from the condition represented by A to that represented by B, by any path whatever — that is, by any succession of changes whatever — for example, that represented by the irregular curve AB. The intrinsic energy in the state B is represented by the area  $VbB\beta$ . The change of intrinsic energy is represented by the area  $\beta BbaA\alpha$ , and this area does not depend on the form of the curve AB. This graphical process is only another way of saying that the intrinsic energy depends on the state of the substance only, and that change of intrinsic energy depends on the final and initial states only.

Another way of representing change of intrinsic energy by aid of isodynamic lines avoids an infinite diagram. Suppose the change of state to be represented by the

the change of state to be represented by the curve AB (Fig. 9). Draw an isodynamic line AC through the point A, and an adiabatic line BC through B, intersecting at C; in general the isoenergic line is distinct from the isothermal line; for example, the isothermal line for a saturated vapor is a straight line parallel to the OV axis, and the isomeorate line is represented approximately



the isoenergic line is represented approximately by the equation

Then the aven ABba represents the external work, and the area bBCc represents the change of intrinsic energy; for if the body be allowed to expand adiabatically till the intrinsic energy is reduced to its original amount at the condition represented by A the external work bBCc will be done at the expense of the intrinsic energy.

#### CHAPTER III.

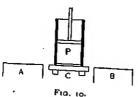
## SECOND LAW OF THERMODYNAMICS.

Heat-engines are engines by which heat is transformed into work. All actual engines used as motors go through continuous cycles of operations, which periodically return things to the original conditions. All heat-engines are similar in that they receive heat from some source, transform part of it into work, and deliver the remainder (minus certain losses) to a refrigerator.

The source and refrigerator of a condensing steam-engine are the furnace and the condenser. The boiler is properly considered as a part of the engine, and receives heat from the source.

Carnot's Engine. - It is convenient to discuss a simple ideal engine, first described by Carnot.

Let P of Fig. 10 represent a cylinder with non-conducting walls, in which is fitted a piston, also of non-conducting material,



and moving without friction; on the other hand, the bottom of the cylinder is supposed to be of a material that is a perfect conductor. There is a nonconducting stand C on which the cylinder can be placed while adiabatic changes take place.

The source of heat A at a temperature t is supposed to be so maintained that in operations during which the cylinder is placed on it, and draws heat from it, the temperature is unchanged. refrigerator B at the temperature  $t_i$  in like manner can withdraw heat from the cylinder, when it is placed on it, at a constant temperature.

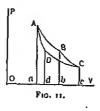
Let there be a unit of weight (for example, one pound) of a certain substance in the cylinder at the temperature t of the source of heat. Place the cylinder on the source of heat A





(Fig. 10), and let the substance expand at the constant temperature t, receiving heat from the source  $\Lambda$ .

If the first condition of the substance be represented by A (Fig. 11), then the second will be represented by B, and AB will be an isothermal. If  $E_a$  and  $E_b$  are the intrinsic energies at A and B, and if  $W_{ab}$ , represented by the area aABb, be the external work, the heat received from A will be



$$Q = A (E_b - E_a + W_{ab}) . . . . . (25)$$

Now place the cylinder on the stand C (Fig. 10), and let the substance expand adiabatically until the temperature is reduced to  $t_1$ , that of the refrigerator, the change being represented by the adiabatic BC (Fig. 11). If  $E_e$  is the intrinsic energy at C, then, since no heat passes into or out of the cylinder,

$$o = A (E_c - E_b + W_{bc}) \dots (26)$$

where  $W_{bc}$  is the external work represented by the area bBCc. Place the cylinder on the refrigerator B, and compress the substance till it passes through the change represented by CD, yielding heat to the refrigerator so that the temperature remains constant. If  $E_d$  is the intrinsic energy at D, then

$$-Q_1 = A (E_d - E_c - W_{cd}) . . . (27)$$

is the heat yielded to the refrigerator, and  $W_{cd}$ , represented by the area cCDd, is the external work, which has a minus sign, since it is done on the substance.

The point D is determined by drawing an adiabatic from A to intersect an isothermal through C. The process is completed by compressing the substance while the cylinder is on the stand C (Fig. 10) till the temperature rises to I, the change being represented by the adiabatic DA. Since there is no transfer of heat,

$$0 = A (E_a - E_d - W_{da}) \dots \dots \dots (28)$$



Adding together the several equations, member to member,

$$Q - Q_1 = A (W_{ab} + W_{bc} - W_{cd} - W_{da}) . . (29)$$

or, if W be the resulting work represented by the area ABCD, then

$$Q - Q_1 = AW \dots \qquad (30)$$

that is, the difference between the heat received and the heat delivered to the refrigerator is the heat transformed into work.

A Reversible Engine is one that may run either in the usual manner, transforming heat into work, or reversed, describing the same cycle in the opposite direction, and transforming work into heat.

A Reversible Cycle is the cycle of a reversible engine.

Carnot's engine is reversible, the reversed cycle being ADCBA (Fig. 11), during which work is done by the engine on the working substance. The engine then draws from the refrigerator a certain quantity of heat, it transforms a certain quantity of work into heat, and delivers the sum of both to the source of heat.

No actual heat-engine is reversible in the sense just stated, for when the order of operations can be reversed, changing the engine from a motor into a pump or compressor, the reversed cycle differs from the direct cycle. For example, the valve-gear of a locomotive may be reversed while the train is running, and then the cylinders will draw gases from the smoke-box, compress them, and force them into the boiler. The locomotive as ordinarily built is seldom reversed in this way, as the hot gases from the smoke-box injure the surfaces of the valves and cylinders. Some locomotives have been arranged so that the exhaust-nozzles can be shut off and steam and water supplied to the exhaust-pipe, thus avoiding the damage from hot gases when the engine is reversed in this way. Such an engine may then have a reversed cycle, drawing steam into the cylinders, compressing and forcing it into the boiler; but in any case the



reversed cycle differs from the direct cycle, and the engine is not properly a reversible engine.

A Closed Cycle is any cycle in which the final state is the same

as the initial state. Fig. 12 represents such a cycle made up of four curves of any nature whatever. If the four curves are of two species only, as in the diagram representing the cycle of Carnot's engine, the cycle is said to be simple.



In general we shall have for a cycle like that of Fig. 12,

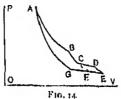
$$\begin{array}{ll} Q_{ab} + Q_{bc} - Q_{cd} - Q_{da} = 2Q = A2W \\ = A (W^a_b + W_{bo} - W_{cd} - W_{da}). \end{array}$$



A closed curve of any form may be considered to be the general form of a closed cycle, as that in Fig. 13. For such a cycle we have  $\int dQ = A \int dW, \text{ which is one more way of}$ 

stating the first law of thermodynamics.

It may make this last clearer to consider the cycle of Fig. 14 composed of the isothermals AB, CD, and EG, and the adiabatics BC, DE, and GA. The cycle may be divided by drawing the curve through from C to F. It is indifferent whether the path followed be ABCDEGA or ABCFCDEGA, or, again, ABCFGA + CDEFC.

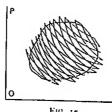


an irregular figure may be Again, imagined to be cut into elementary areas by isothermals and adiabatic lines, as in Fig. 15. The summation of the areas will give the entire area, and the summation of the works represented by these will give the entire work represented by the entire area,

The Efficiency of an engine is the ratio of the heat changed into work to the entire heat applied; so that if it be represented by c,

$$e^{\frac{AW}{Q}} \stackrel{\text{\tiny post}}{=} \frac{Q - Q'}{Q} \dots \dots \dots (31)$$

for the heat Q' rejected to the refrigerator is what is left after AW thermal units have been changed into work.



Carnot's Principle. — It was first pointed out by Carnot that the efficiency of reversible engine does not depend on the nature of the working substance, but that it depends on the temperatures of the source of heat and the refrigerator.

Let us see what would be the consequence if this principle were not true.

Suppose there are two reversible engines R and A, each taking Q thermal units per second from the source of heat, of which A is the more efficient, so that

$$\frac{AW_a}{Q} = \frac{Q - Q_{a'}}{Q} \cdot \cdot \cdot \cdot \cdot \cdot \cdot (32)$$

is larger than

$$\frac{AW_r}{Q} = \frac{Q - Q_r'}{Q} \cdot \cdot \cdot \cdot \cdot \cdot \cdot (33)$$

this can happen only because  $Q_{a'}$  is less than  $Q_{r'}$ , for Q is assumed to be the same for each engine. Let the engine R be reversed and coupled to A, which can run it and still have left the useful work  $W_a - W_r$ . This useful work cannot come from the source of heat, for the engine R when reversed gives to the source Q thermal units per second, and A takes the same amount in the same time. It must be assumed to come from the refrigerator. which receives Qa' thermal units per second, and gives up Q thermal units per second, so that it loses

$$Q_r' - Q_a' = A (W_a - W_r)$$

thermal units per second. This equation may be derived from equations (32) and (33) by subtraction.

Now it cannot be proved by direct experiment that such at ra action as that just described is impossible. Again, the first law of thermodynamics is scrupulously regarded, and there is no



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law no contradiction or formal absurdity of statement. And yet when the consequences of the negation of Carnot's principles are clearly set forth they are naturally rejected as improbable, if not impossible. The justification of the principle is found in the fact that theoretical deductions from it are confirmed by experiments.

Second Law of Thermodynamics.—The formal statement of Carnot's principle is known as the second law of thermodynamics. Various forms are given by different investigators, none of which are entirely satisfactory, for the conception is not simple, as is that of the first law.

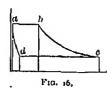
The following are some of the statements of the second law:

- (1) All reversible engines working between the same source of heat and refrigerator have the same efficiency.
- (2) The efficiency of a reversible engine is independent of the working substance.
- (3) A self-acting machine cannot convey heat from one body to another at a higher temperature.

The second law is the third general principle of thermodynamics; it differs from each of the others and is independent of them. Summing up briefly, the first general principle is a pure assumption that thermodynamic equations may contain only two independent variables; the second is the statement of an experimental fact; the third is a choice of one of two propositions of a dilemma. The first and third are justified by the results of the applications of the theory of thermodynamics.

So far as efficiency is concerned, the second law of thermodynamics shows that it would be a matter of indifference what working substance should be chosen; we might use air or steam in the same engine and get the same efficiency from either; there would, however, be a great difference in the power that would be obtained. In order to obtain a diagram of convenient size and distinctness, the adiabatics are made much steeper than the isothermals in Fig. 11; as a matter of fact the diagram drawn correctly is so long and attenuated that it would be practically

worthless even if it could be obtained with reasonable a mation in practice, as the work of the cycle would hard come the friction of the engine. The isothermals for a of water and steam are horizontal, and the diagram ta



form shown by Fig. 16. In practice gram closely resembling Carnot's c chosen as the ideal, differing mainly steam is assumed to be supplied a hausted. In a particular case an working between the temperatures 36

and 158° F. had an actual thermal efficiency of o. ideal cycle had an efficiency of 0.23, and Carnot's cyan efficiency of 0.25. The ratio of 0.18 to 0.23 is about which compares favorably with the efficiency of turbine wheels.

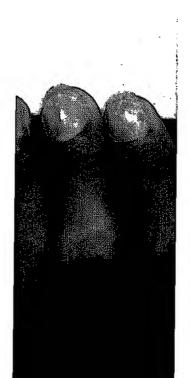
cfliciency of a reversible engine is independent of the nathe working substance; consequently the expression is efficiency will not include such properties of the working stance as specific volume and specific pressure. But the ciple asserts also that the efficiency depends on the tempe of the source of heat and the refrigerator, which indeed only properties of the source and refrigerator that can the working of the engine.

We may then represent the efficiency as a function of the peratures of the source of heat and the refrigerator, or amounts to the same thing, as a function of the superic perature and the difference of the temperatures, and may

$$e = \frac{AW}{Q} = \frac{Q - Q'}{Q} = F(l, l - l')$$

where Q is the heat received, Q' the heat rejected, and t are the temperatures of the source of heat and of the refrigon any scale whatsoever, absolute or relative.

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t ho cliathe source of heat, Q - Q' and t - t' become  $\Delta Q$  and  $\Delta t$ , and at the limit dQ and dt, so that

$$\frac{dQ}{Q} = F(t, dt) . . . . . . . (34)$$

It is convenient to assume that the equation can be expressed in the form

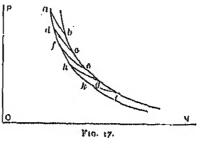
$$\frac{dQ}{Q} = f(t) dt.$$

The function f(t) is known as Carnot's function, and physicists consider that the isolation of this function and the relation of the function to temperature are of great theoretical importance.

Absolute Scale of Temperature. - It is convenient and customary to assign to Carnot's function the form  $\frac{1}{T^{1}}$ , where T is the temperature by the absolute scale referred to on page 3, measured from the absolute zero of temperature. This assumption is justified by the facts that the theory of thermodynamics is much simplified thereby, and that the difference between such a scale of temperature and the scale of the air-thermometer is very small.

Kelvin's Graphical Method. — This treatment of Carnot's function was first proposed by Lord Kelvin, who illustrated the general conception by the following graphical construction:

In Fig. 17 let ak and bi be two adiabatic lines, and let the substance have its condition represented by the point a. Through a and d draw isothermal lines; then the diagram abod represents the cycle of a simple reversible engine. Draw the isothermal line fe, so that the area deef shall be equal to abed; then the diagram deef



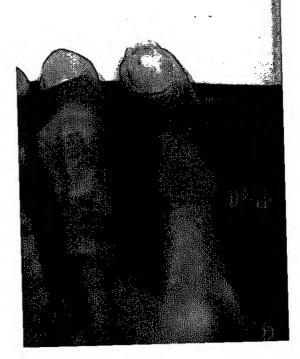
represents the cycle of a reversible engine, doing the same amount of work per stroke as that engine whose cycle is reprefrom the source and delivered to the refrigerator — i.e., the heat transformed into work — is the same. The refrigerator of the first engine might serve for the source of heat for the second.

Suppose that a series of equal areas are cut off by isothermal lines, as fegh, hgik, etc., and suppose there are a series of reversible engines corresponding; then there will be a series of sources of heat of determinate temperatures, which may be chosen to establish a thermometric scale. In order to have the scale correspond with those of ordinary thermometers, one of the sources of heat must be at the temperature of boiling water, and one at that of melting ice; and for the centigrade scale there will be one hundred, and for the Fahrenheit scale one hundred and eighty, such cycles, with the appropriate sources of heat, between boiling-point and freezing-point. To establish the absolute zero of the scale the series must be imagined to be continued till the area included between an isothermal and the two adiabatics, continued indefinitely, shall not be greater than one of the equal areas.

C 100 h-200 Fig. 18.

This conception of the absolute zero may be made clearer by taking wide intervals of temperature, as on Fig. 18, where the cycle abcd is assumed to extend between the isothermals of o° and 100° C.; that is, from freezing-point to boiling-point. The next cycle, edef, extends to - 100° C., and the third cycle, efgh, extends to - 200° C. The remaining area, which is of infinite length and extremely attenuated, is bounded by the isothermal gh and the two adiabatics  $-\infty$  ha and  $g\beta$ . The diagram of course cannot be completed, and consequently the area cannot be measured;

but when the equations to the isothermal and the adiabatics are known it can be computed. So computed, the area is found



to be  $\frac{73}{100}$  of one of the three equal areas abed, edfe, and effig.

The absolute zero is consequently 273° C. below freezing-point. Further discussion of the absolute scale will be deferred till a comparison is made with the air-thermometer.

Spacing of Adiabatics. — Kelvin's graphical scale of temperature is clearly a method of spacing isothermals which depends only on our conceptions of thermodynamics and on the fundamental units of weight and length. Evidently the same method may be applied to spacing adiabatics, and thereby a new conception of great importance may be introduced into the theory of thermodynamics. On this conception is based the method for solving problems involving adiabatic expansion of steam, as will be explained in the discussion of that subject.

In Fig. 19 let an and do be two isothermals, and let ad, be, Im and no be a series of adiabatics, so drawn that the areas of the figures abed, blme, and lnom are equal; then we have a series of adiabatics that are spaced in the same manner as are the isothermals in Figs. 17 and 18, and, as with those iso-

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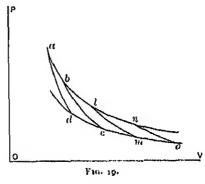
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thermals, the spacing depends only on our conceptions of thermodynamics and the fundamental units of weight and length.

In the discussion of Figs. 17 and 18 it was shown that the area of the strip between the initial isothermal ab and the two adiabatic lines must be treated as finite, and that in consequence the graphical process leads to an absolute zero of temperature. On the contrary, the area between the adiabatic ad and the two isothermals an and do if extended infinitely will be infinite, and it will be found that there is no limit to the number of adiabatics that can be drawn with the spacing indicated. A like result will follow if the isothermals are extended to the right and

upward, and if adiabatics are spaced off in the same manner. This conclusion comes from the fact pointed out on page 21, that the area under an isothermal curve which is extended without limit is infinite, because heat is continuously supplied, some part of which can be changed into work.

It is convenient to introduce a new function at this place which shall express the spacing of adiabatics as represented in Fig. 19, and which will be called entropy. From what precedes it is evident that entropy has the same relations to the adiabatics of Fig. 19 that temperature has to the isothermals of Figs. 17 and 18, but that there is this radical difference, that while there is a natural absolute zero of temperature, there is no zero of entropy. Consequently in problems we shall always deal with differences of entropy, and if we find it convenient to treat the entropy of a certain condition of a given substance as a zero point it is only that we may count up and down from that point.

If the adiabatic line ad in Fig. 19 should be extended to the right, it would clearly lie beneath the adiabatic no, which agrees with the tacit convention of that figure, i.e., that as spaced the adiabatics are to be numbered toward the right and that the entropy increases from a toward n.

The simplest and the most natural definition of entropy from the present considerations, is that entropy is that function which remains constant for any change represented by a reversible adiabatic expansion (or compression). With this definition in view, the adiabatic lines might be called isoentropic lines. It should be borne in mind that our present discussion is purposely limited to expansion in a non-conducting cylinder closed by a piston, or to like operations. More complex operations than that just mentioned may require an extension of the conception of entropy and lead to fuller definitions. Such extensions of the conception of entropy have been found very fruitful in certain physical investigations, and many writers on thermodynamics for engineers consider that they get like advantages from them. There is, however, an advantage in limiting the conception of

new function, however simple that conception may be; and there is an added advantage in being able to return to a simple conception at will.

Efficiency of Reversible Engines. — Returning to equation (34) and replacing Carnot's function f(t) by  $\frac{1}{T}$ , as agreed, we have for the differential equation of the efficiency of a reversible engine

$$\frac{dQ}{Q} = \frac{dl}{T},$$

or, integrating between limits,

$$\log_{\mathbf{a}} \frac{Q'}{Q} = \log_{\mathbf{a}} \frac{T'}{T'},$$

$$\therefore \frac{Q'}{Q} = \frac{T'}{T'},$$

and the efficiency for the cycle becomes

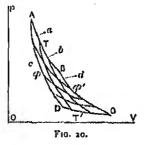
$$\frac{Q-Q'}{Q} = \frac{T-T'}{T} \cdot \cdot \cdot \cdot \cdot \cdot (35)$$

This result might have been obtained before (or without) the discussion of Kelvin's graphical method, and leads to the same conclusion, that the absolute temperature can be made to depend on the efficiency of Carnot's cycle, and may, therefore, be inde-

pendent of any thermometric substance. As has already been said, this conception is more important on the physical side than on the engineering side, and its reiteration need not be considered to call for any speculation by the student at this time.

Graphical Representation of Efficiency.

— Let Fig. 20 represent the cycle of a reversible heat-engine. For convenience



it is supposed there are four degrees of temperature from the isothermal AB to the isothermal DC, and that there are three intervals or units of entropy between the adiabatics AD and

BC. First it will be shown that all the small areas into whe the cycle is divided by drawing the intervening adiabatics isothermals are equal. Thus we have to begin with a a = c by construction. But engines working on the cycle and b have the same efficiency and reject the same and b have the same efficiency and reject the same are could to engines working on the cycles c and d, which conscious take in the same amounts of heat. But these engines between the same limits of temperature and have the efficiency, and consequently change the same amount into work. Therefore the areas c and d are equal. In amanner all the small areas are equal, and each representation thermal unit, or 778 foot-pounds of work.

It is evident that the heat changed into work is represented

$$(T-T')(\phi'-\phi),$$

and, further, that the same expression would be obtained for similar diagram, whatever number of degrees there received between the isothermals, or intervals of entropy between adiabatics, and that it is not invalidated by using fractional degrees and fractions of units of entropy. It is consequent the general expression for the heat changed into works engine having a reversible cycle.

It is clear that the work done on such a cycle increases and lower temperature T' decreases, and that it is a maximum of the heat a policy changed into work. Therefore the heat applied is represent by

$$Q = T (\phi' - \phi),$$

and the efficiency of the engine working on the cycle regardless by Fig. 20 is

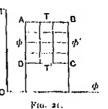
$$\frac{AW}{Q} = \frac{Q - Q'}{Q} = \frac{(T - T')(\phi' - \phi)}{T(\phi' - \phi)} = \frac{T - T'}{T}$$

as found by equation (35). The deduction of this equation integration is more simple and direct, but the graphical

is interesting and may give the student additional light on this subject.

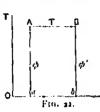
Temperature-Entropy Diagram. — Thermal diagrams are commonly drawn with pressure and volume for the co-ordinates, but for some purposes it is convenient to use other properties as co-ordinates, in particular temperature and entropy. For

example, Fig. 21 represents Carnot's cycle drawn with entropies for abscisse and temperatures for ordinates, with the advantage that indefinite extensions of the lines are avoided, and the areas under consideration are evidently finite and measurable. With the exception that there appears now to be no



necessity to show that the areas obtained by subdivision are all equal, the discussion for Fig. 20 drawn with pressures and volumes may be repeated with temperatures and entropies.

Expression for Entropy. --- One advantage of using the temperature-entropy diagram is that it leads at once to a method for computing changes of entropy. Thus in Fig. 22 let AB



represent an isothermal change, and let Aa and Bb be adiabatics drawn to the axis of  $\phi$ ; then the diagram ABba may be considered to be the cycle for a Carnot's engine working between the temperature T and the absolute zero, and consequently baving the efficiency unity. The heat changed into work may there-

fore be represented by  $Q = T(\phi' - \phi)$  . . . . . . (36)

If we are dealing with a change under any other condition than constant temperature, we may for an infinitesimal change, write the expression

and for the entire change may express the change of entropy by

$$\phi' - \phi \approx \int \frac{dQ}{T}$$

which should for any particular case either be integrated between limits or else a constant of integration should be determined.

Attention should be called to the fact that the conception of the spacing of isothermals and adiabatics is based fundamentally on Carnot's cycle and the second law of thermodynamics, which has been applied only to reversible operations. The method of calculating changes of entropy applies in like manner to reversible operations; and when entropy is employed for calculations of operations that are not reversible, discretion must be used to avoid inconsistency and error.

On the other hand, the entropy of a unit weight of a given substance under certain conditions is a perfectly definite quantity and is independent of the previous history of the substance. \* This may be made evident by the consideration that any point on the line no, Fig. 19, page 31, has a certain number of units of entropy (for example, three) more than that of any point on the adiabatic ad.

Example. — There may be an advantage in giving a calculation of a change of entropy to emphasize the point that it can be represented by a number. Let it be required to find the change of entropy during an isothermal expansion of one pound air from four cubic feet to eight cubic.

The heat applied may be obtained by integrating the expression

$$d\phi = \frac{dQ}{T} = \frac{ldv}{T} = (c_p - c_u) \frac{p}{R} \frac{dv}{T},$$

the value of the latent heat having been taken from page 12. From the characteristic equation

$$pv = RT$$

the above expression may be reduced to

$$d\phi = (c_p - c_v) \frac{dv}{v}.$$

or 
$$\phi' - \phi = (c_p - c_p) \log_a \frac{v}{v'}$$
$$\phi' - \phi = (0.2375 - 0.1690) \log_a \frac{8}{4} = 0.0475.$$

A problem for air is chosen because it can be readily worked out at this place; as a matter of fact, there are few occasions in practice where there is reason to refer to entropy of air.

Application to a Reversible Cycle. — A very important result is obtained by the application of equation (37) to the calculation of entropy during a reversible cycle. In the first place, it is clear that the entropy of a substance having its condition represented by the point a (Fig. 23), depends on the adiabatic line drawn through it; in other words, the entropy depends only

on the condition of the substance. In this regard entropy is like intrinsic energy and differs from external work. Suppose now that the substance is made to pass through a cycle of operations represented by the point a tracing the diagram on

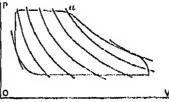
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Fig. 23; it is clear that the entropy will be the same at the end of the cycle as at the beginning, for the tracing-point will then be on the original adiabatic line. As the tracing-point moves toward the right from adiabatic to adiabatic the entropy increases, and as it moves to the left the entropy decreases, the algebraic sum of changes of entropy being zero for the entire cycle. This conclusion holds whether the cycle is reversible or non-reversible. The cycle represented by Fig. 23 is purposely drawn like a steam-engine indicator diagram (which is not reversible) to emphasize the fact that the change of entropy is zero in any case.

If the cycle is reversible, then equation (37) may be used for calculating the several changes of entropy, and for calculating the change for the entire cycle, giving for the cycle

This is a very important conclusion from the second law of thermodynamics, and is considered to represent that law. The second law is frequently applied by using this equation in connection with a general equation or a characteristic equation, in a manner to be explained later.

Though the discussion just given is simple and complete, there is some advantage in showing that equation (38) holds for certain simple and complex reversible cycles.

Thus for Carnot's cycle, represented by Fig. 20, the increase of entropy during isothermal expansion is

$$\phi' - \phi = \int \frac{dQ}{T} = \frac{1}{T} \int dQ = \frac{Q}{T}$$

because the temperature is constant. In like manner the decrease during isothermal compression is

$$\phi - \phi' = \frac{Q'}{T'},$$

so that the change of entropy for the cycle is

$$\frac{Q}{T} - \frac{Q'}{T'}$$

But from the efficiency of the cycle we have

$$\frac{Q-Q'}{Q}=\frac{T-T'}{T}. \qquad \therefore \frac{Q'}{Q}=\frac{T'}{T}. \qquad \therefore \frac{Q}{T}-\frac{Q'}{T'}=0.$$

A complex cycle like that represented by Fig. 24 may be broken up into two simple cycles ABFG

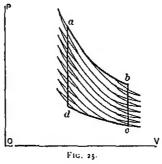
A\ and CDFE, for each of which individually

the same result will be obtained—that is, the increase of entropy from A to B is equal to the decrease from F to  $G_1$  and the increase from G to G is equal to the

decrease from E to F, so that the summation of changes for the entire cycle gives zero.

Fig. 25 represents the simplified ideal diagram of a hot-air engine, in which by the aid of a regenerator the adiabatic lines

of Carnot's cycle are replaced by vertical lines without affecting the reversibility or the efficiency of the cycle. We may replace the actual diagram by a series of simple cycles made up of isothermals and adiabatics, so drawn that the perimeter of the complex cycle includes the same area and corresponds approximately with that of the



actual diagram. The summation of the change of entropy for the complex cycle is clearly zero, as before. But by drawing the adiabatic lines near enough together we may make the perimeter approach that of the actual diagram as nearly as we please, and we may therefore conclude that the integration for the changes of entropy for that cycle is also zero.

Maximum Efficiency. — In order that heat may be transformed into work with the greatest efficiency, all the heat should be applied at the highest practicable temperature, and the heat rejected should be given up at the lowest practicable temperature; this condition is found for Carnot's cycle, which serves as the ideal type to which we approach as nearly as practical conditions allow. Deviations from the ideal type are of two sorts, (1) commonly a different and inferior cycle is chosen as being practically more convenient, and (2) the material of which the working cylinder is made absorbs heat at high temperature and gives out heat at low temperature, thus interfering with the attainment of the cycle selected.

The principle just stated must be accepted as immediately evident; but there may be an advantage in giving an illustration. The complex cycle of Fig. 24 is made up of two simple Carnot cycles ABFG and CDEF; if two thirds of the heat is applied during the isothermal expansion AB at 500° C., and one third during the expansion CD, at 250° C., and if all the heat is re-

jected at 20° C., the combined efficiency of the diagram rmay computed to be

$$\frac{2}{3} \times \frac{500 - 20}{500 + 273} + \frac{1}{3} \times \frac{250 - 20}{250 + 273} = 0.56;$$

had the heat been all applied at 500° C., the efficiency wo have been

$$\frac{500-20}{500+273} = 0.02.$$

The loss in this case from applying part of the heat at lost temperature is, therefore,

$$\frac{0.63 - 0.56}{0.02} \approx 0.007.$$

Non-reversible Cycles. — If a process or a cycle is non-resible, then the change of entropy cannot be calculated by extion (37), and equation (38) will not hold. The entropy indeed, be the same at the end as at the beginning of the cycle the integration of  $\frac{dQ}{T}$  for the cycle will not give zero. the contrary, it can be shown that the integration of entire cycle will give a negative quantity. Thus let the reversible engine A take the same amount of heat per strok the reversible engine R which works on Carnot's cycle. but it have a less efficiency, so that

$$\frac{Q-Q'}{Q}<\frac{Q-Q'}{Q} \cdot \dots \cdot$$

where Q' represents the heat rejected by the engine .

$$Q - Q_1' < Q - Q' \sim (T - T') (\phi' - \phi) \qquad . \qquad .$$

Suppose now that T' approaches zero and that  $\phi'$  approaches then at the limit we shall have

$$dQ_1 < dQ = Td\phi,$$

or

$$\frac{dQ_1}{T} < d\phi.$$

Integrating for the entire cycle, we shall have

where -N represents a negative quantity. The absolute value of N will, of course, depend on the efficiency of the non-reversible engine. If the efficiency is small compared with that of a reversible engine, then the value of N will be large. If the efficiency approaches that of a reversible engine, then N approaches zero. It is scarcely necessary to point out that N cannot be positive, for that would infer that the non-reversible engine had a greater efficiency than a reversible engine working between the same temperatures.

Some non-reversible operations, like the flow of gas through an orifice, result in the development of kinetic energy of motion. In such case the equation representing the distribution of energy contains a fourth term K to represent the kinetic energy, and equation (15) becomes

$$dQ = A \left( dS + dI + dW + dK \right) \quad . \quad . \quad . \quad (42)$$

As before S represents vibration work, I represents disgregation work, and W represents external work. If the vibration and disgregation work cannot be separated, then we may write

$$dQ = A (dE + dW + dK)$$
 . . . . . (43)

If a non-reversible process like that just discussed takes place in apparatus or appliances that are made of non-conducting material, or if the action of the walls on the substance contained can be neglected, the operation may properly be called adiabatic; such a use is clearly an extension of the idea stated on page 32, and conclusions drawn from adiabatic expansion in a closed cylinder cannot be directly extended to this new application. Such a non-reversible operation is not likely to be isoentropic, and there is some advantage in drawing a distinction between operations which are isoentropic and those which are adiabatic.

A non-reversible operation in non-conducting receptacles made isothermal, or may be with constant intrinsic energy. as appear in the discussion of flow of air in pipes on page 3801 the discussion of the steam calorimeter, page 191. Any reversible process is likely to be accompanied by an increasentropy; this will appear in special cases discussed in chapter on flow of fluids.

Since the entropy of a pound of a given substance given conditions, reckoned from an arbitrary zero, is a perl definite numerical quantity, it is possible to determine its cn for any series of conditions, without regard to the methe passing from one condition to another. It is, therefore, al possible to represent any changes of a fixed weight cof a stance, by a diagram drawn with temperatures and critt for co-ordinates. If the diagram can be properly interpt conclusions from it will be valid. It is, however, to be ther mind that thermodynamics is essentially an analytical results. ical treatment; the treatment, so far as it applies to engine is neither extensive nor difficult. But the student is caut not to consider that because he has drawn a diagram repri ing a given operation to the eye, he necessarily has a conception of the operation. If any operation in wolve increase (or decrease) of weight of the substance operate thermal diagrams are likely to be difficult to devise and to misinterpretation.

## CHAPTER IV.

#### GENERAL THERMODYNAMIC METHOD.

In the three preceding chapters a discussion has been given of the three fundamental principles of thermodynamics, namely, (1) the assumption that the properties of any substance can be represented by an equation involving three variables; (2) the acceptance of the conservation of energy; and (3) the idea of Carnot's principle. In the ideal case each of these principles should be represented by an equation, and by the combination of the three several equations all the relations of the properties of a substance should be brought out so that unknown properties may be computed from known properties, and in particular advantage may be taken of opportunities to calculate such properties as cannot be readily determined by direct experiment from those which may be determined experimentally with precision.

Recent experiments have so far changed the condition of affairs that there is less occasion than formerly for such a general treatment. Of the three classes of substances that are interesting to engineers, namely, gases, saturated vapors, and superheated vapors, the conditions appear to be as follows. gases there are sufficient experimental data to solve all problems without referring to the general method, though the ratio of the specific heats is probably best determined by that method. saturated steam there is one property, namely, the specific volume, which is computed by aid of the general method, but there are experimental determinations of volume which are reliable though less extensive. The characteristic equation of superheated steam is now well determined, and the specific heat is determined with sufficient precision for engineering purposes, so that there is no difficulty in making the customary calculations.

The one class of substances for which the necessary must be computed by aid of the general method, are three tile fluids like ammonia and sulphur dioxide, which for refrigerating machines.

On the whole, even with conditions as stated, it is that the student should master the general therressist method, given in this chapter. That method is notified nor hard, and is so commonly accepted that students mastered it will have no difficulty in reading standard and current literature involving thermodynamic discussion. Those cases remaining where the general method or its lent must be used, are best treated by that method, accepted the general method.

The case having been presented as fairly as presented cretion may be left with the student or his instructors when the shall read the remainder of this chapter before presented or whether the chapter shall be altogether omitted.

The following method of combining the three general ciples of thermodynamics, which is due to Lord Kelvin.

$$\begin{array}{ccc} \delta^{1} x & \delta^{2} x \\ \hline \delta y \delta z & \delta z \delta y \end{array}$$

as the basis of an operation. This expression is generall as a criterion to determine whether a certain differential that can be integrated directly, ever some additional relation must be sought by aid of select expression may be transformed so that it can be integrated

Conversely, if we know, from the nature of a give as gas like intrinsic energy, that it can be always calculated fixes a condition as represented by two variables like tempersum and volume, then we are justified in concluding that the engages

$$\frac{\delta^2 F_c}{\delta v \delta t} = \frac{\delta^2 F_c}{\delta (\delta v)}$$

Now in laying out a general method it is impossible to select any particular characteristic equation, and for that reason, if no other, the form of the integral equation connecting E with t and v cannot be assigned. But the fact remains that the possibility of working out any method depends on the assumption of the ultimate possibility of writing such an equation, and that assumption carries with it the assumption that dE is an exact differential.

Application of the First Law. — The first general principle may be taken to be represented by equation (1),

$$dQ \rightarrow c_v dt + l dv$$
,

and the first law of thermodynamics by equation (16),

$$dQ \bowtie A (dE + dW) \bowtie A (dE + pdv).$$

Combining these equations gives

$$dE = \frac{\epsilon_p}{A} dt + \left(\frac{l}{A} - p\right) dv;$$

and comparing with the general form,

$$dE = \frac{\delta E}{\delta t} dt + \frac{\delta E}{\delta v} dv,$$

it is evident that

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$$\frac{\delta E}{\delta t} = \frac{c_y}{A}$$
 and  $\frac{\delta E}{\delta v} = \frac{I}{A} - p$ .

Now equation (44) is an abbreviated way of writing the expression for continued differentiation which may be expanded to

$$\frac{\delta \frac{\delta E}{\delta t}}{\delta v} = \frac{\delta \frac{\delta E}{\delta v}}{\delta t}$$

or replacing the first partial differential coefficients by their equivalents,

the subscripts being written to avoid possible confusion with other partial differential coefficients to be deduced later.

From the first law of thermodynamics and equation (2) was have in like manner

$$dQ = A (dE + pdv) = c_p dt + mdp.$$

Since the differential dv is inconvenient, we may replace it by

$$dv = \frac{\delta v}{\delta \rho} d\rho + \frac{\delta v}{\delta l} dl,$$

so that

$$A\left(dE+p\ \frac{\delta v}{\delta p}\ dp+p\ \frac{\delta v}{\delta t}\ dt\right)\cdots c_p dt+m dp.$$

$$\therefore dE = \left(\frac{\epsilon_p}{A} - \rho \frac{\delta v}{\delta l}\right) dt + \left(\frac{m}{A} - \rho \frac{\delta v}{\delta \rho}\right) d\rho.$$

Making use of the equation

$$\frac{\delta \frac{\delta E}{\delta l}}{\delta p} = \frac{\delta \frac{\delta E}{\delta p}}{\delta l}$$

gives

$$\frac{\delta}{\delta \rho} \left( \frac{\epsilon_{\nu}}{A} - \rho \frac{\delta v}{\delta l} \right) = \frac{\delta}{\delta l} \left( \frac{m}{A} - \rho \frac{\delta v}{\delta \rho} \right).$$

$$\therefore \frac{1}{A} \left( \frac{\delta c_p}{\delta p} \right)_i - \frac{\delta v}{\delta l} - p \frac{\delta^3 v}{\delta p \delta l} - \frac{1}{A} \left( \frac{\delta m}{\delta l} \right)_p - p \frac{\delta^3 v}{\delta l \delta p}.$$

But the assumption of a characteristic equation connecting  $p_i/v_i$  and t carries with it the assumption that

$$\frac{\delta' i'}{\delta \rho \delta l} = \frac{\delta' i v}{\delta l \delta \rho'}$$

so that

$$\frac{1}{A} \left[ \left( \frac{\delta c_p}{\delta p} \right)_i - \left( \frac{\delta m}{\delta l} \right)_p \right] - \frac{\delta v}{\delta l} \cdot \cdot \cdot \cdot \cdot \cdot (46)$$

Again, from equation (3) we may have

$$dQ = A (dE + pdv) = ndp + odv$$
,

$$\therefore dE = \frac{n}{A} dp + \left(\frac{n}{A} + p\right) dv \quad , \quad , \quad , \quad , \quad (47)$$

or, making use of

$$\frac{\delta^{1}F}{\delta v \delta \rho} = \frac{\delta^{1}F}{\delta \rho \delta v^{1}}$$

$$= \frac{1}{A} \begin{pmatrix} \delta n \\ \delta v \end{pmatrix}_{p} = \frac{1}{A} \begin{pmatrix} \delta j \\ \delta \rho \end{pmatrix}_{p} = 1,$$

$$\therefore \frac{1}{A} \begin{bmatrix} \begin{pmatrix} \delta j \\ \delta \rho \end{pmatrix}_{v} & \begin{pmatrix} \delta n \\ \delta v \end{pmatrix}_{p} \end{bmatrix} = 1, \qquad (48)$$

Application of the Second Law. ... The second law of thermodynamics can be expressed by equation (38), page 37,

$$\int \frac{dQ}{T} = o,$$

which makes  $\frac{dQ}{T}$  or  $d\phi$  an exact differential, so that we may write

To prepare equation (1) for this transformation, we may write

$$d\phi = \frac{dQ}{T} = \frac{\epsilon_T}{T} dt + \frac{1}{T} dv_t$$

so that the preceding equation gives

$$\frac{\delta}{\delta v} \left( \frac{c_v}{T} \right) = \frac{\delta}{\delta l} \left( \frac{l}{T} \right).$$

$$\therefore \frac{1}{T} \left( \frac{\delta c_v}{\delta v} \right)_l = \frac{T \left( \frac{\delta l}{\delta l} \right)_v - l}{T^2}$$
or
$$\left( \frac{\delta l}{\delta l} \right)_v - \left( \frac{\delta c_v}{\delta v} \right)_l = \frac{l}{T} . . . . . . . . . . . (49)$$

Performing a like operation on equation (2) we have

$$\frac{dQ}{T} = \frac{c_p}{T}dl + \frac{m}{T}dp,$$

$$\frac{\delta}{\delta p} \left(\frac{c_p}{T}\right) = \frac{\delta}{\delta l} \left(\frac{m}{T}\right).$$

$$\therefore \frac{1}{T} \left(\frac{\delta c_p}{\delta p}\right)_l = \frac{T \left(\frac{\delta m}{\delta l}\right)_p - m}{T^2}.$$

$$\therefore \left(\frac{\delta c_p}{\delta p}\right)_l - \left(\frac{\delta m}{\delta l}\right)_p = -\frac{m}{T}.$$
(50)

Again, from equation (3) we have

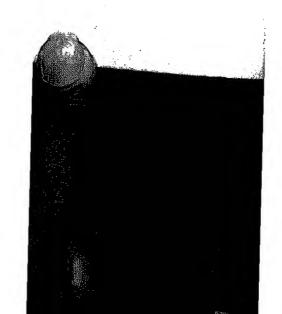
$$\frac{dQ}{T} = \frac{n}{T} dp + \frac{o}{T} dv.$$

$$\therefore \frac{\delta}{\delta v} \left(\frac{n}{T}\right) = \frac{\delta}{\delta p} \left(\frac{o}{T}\right).$$

$$\therefore \frac{T\left(\frac{\delta n}{\delta v}\right)_{p} - n\frac{\delta t}{\delta v}}{T^{2}} = \frac{T\left(\frac{\delta o}{\delta p}\right)_{n} - o\frac{\delta t}{\delta p}}{T^{2}}.$$

$$\therefore \frac{1}{T} \left(o\frac{\delta t}{\delta p} - n\frac{\delta t}{\delta v}\right) = \left(\frac{\delta o}{\delta p}\right)_{v} - \left(\frac{\delta n}{\delta v}\right)_{p} . . . . (51)$$

First and Second Laws Combined. — The result of applying both the first and the second laws of thermodynamics to the



equations (1), (2), and (3) may be obtained by combining the equations resulting from the application of the laws separately.

Thus equations (45) and (49) give

$$\frac{\delta p}{\delta t} = \frac{1}{A} \frac{I}{I} + \cdots + \cdots + (54)$$

Equations (46) and (50) give

$$\frac{dv}{dt} = -\frac{t}{A}\frac{m}{T} \cdot \cdot \cdot \cdot \cdot \cdot \cdot \cdot (53)$$

And equations (48) and (51) give

$$A = \frac{1}{T} \left( n \frac{\delta_t}{\delta_D} + n \frac{\delta_t}{\delta_C} \right), \quad , \quad , \quad (54)$$

It is convenient to transform this last equation by taking values of n and a from page (x), yielding

$$t_{\mu} \sim t_{\mu} \sim AT \frac{\delta_{I}}{\delta_{I}} \frac{\delta_{I}}{\delta_{I}} + \cdots + (55)$$

The equations deduced in this chapter show the necessary relations among the thermal capacities if the laws of thermo-dynamics are accepted. Some of them, or equations deduced from them, have been used by writers on thermodynamics to establish relations or compute properties that cannot be readily obtained by direct experiments.

For the student familiarity with the processes is of more importance than any of the results.

Alternative Method. Some writers on thermodynamics reserve the discussion of temperature until they are ready to define or assume an absolute scale independent of any substance and depending only on the fundamental units of length and weight. Of the three general equations  $(x)_1(x)$ , and (x) they use at first only the latter:

$$d() = ndp + ndv$$

Now from equation (16), representing the first law of thermodynamics,

$$dQ = A (dE + pdv),$$

it is evident that dQ is not an exact differential, since the equation cannot be integrated directly. The fact that in certain cases p may be expressed as a function of v, and the integral for external work can be deduced, does not affect this general statement. Suppose that there is some integrating factor, which may be represented by  $\frac{1}{S}$ , so that

$$\frac{dQ}{S} = \frac{n}{S} dp + \frac{o}{S} dv$$

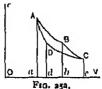
may be integrated directly; we may then consider that we have a series of thermal lines represented by making

$$\frac{1}{S}$$
 = const.,  $\frac{1}{S'}$  = const.,  $\frac{1}{S''}$  = const., etc.

These lines with a series of adiabatic lines represented by

$$\phi = \text{const.}, \quad \phi' = \text{const.}, \quad \phi'' = \text{const.}, \text{ etc.},$$

allow us to draw a simple cycle of operations represented by Fig. 25a, in which AB and CD are represented by the equations



$$\frac{1}{S} = C$$
, and  $\frac{1}{S'} = C'$ ,

while AD and BC are adiabatics. The effio a a b c v ciency of a reversible engine receiving the
heat Q during the operation AB, and rejecting the heat Q' during the operation CD, will be

$$c = \frac{Q - Q'}{Q} = \frac{AW}{Q}.$$

But  $\frac{dO}{S}$  is an exact differential, and depends on the state of

the substance only, and consequently is the same at the end as at the beginning of the cycle, so that for the entire cycle

$$\int \frac{dQ}{S} = 0.$$

Now during the operations represented by the adiabatics AD and BC no heat is transmitted, and during the operations represented by the lines AB and CD,  $\frac{1}{S}$  is constant; consequently the integration of the above equation for the cycle gives

$$\frac{Q}{S} - \frac{Q'}{S'} = 0.$$

$$\therefore \frac{Q - Q'}{Q} = \frac{S - S'}{S};$$

that is, the efficiency of an engine working on such a cycle depends on S and S', and on nothing else.

Zeuner's Equations. — A special form of thermodynamic equations has been developed by Zeuner and through his influence has been impressed to a large extent on German writings. These equations can be deduced from those already given in the following manner.

From the application of the first law of thermodynamics to equation (3) we have equation (47), page 47,

$$dE = \frac{n}{A}dp + \left(\frac{o}{A} - p\right)dv.$$

Now

$$dE = \frac{\delta E}{\delta p} dp + \frac{\delta E}{\delta v} dv,$$

so that

$$\frac{n}{A} = \frac{\delta E}{\delta p}, \qquad \frac{o}{A} = \frac{\delta E}{\delta v} + p.$$

These properties Zeuner writes

$$X = \frac{\delta E}{\delta p}, \qquad Y = p + \frac{\delta E}{\delta v}.$$

Solving equation (54) first for o and then for  $n_i$ 

$$o = \frac{AT + n\frac{\delta t}{\delta v}}{\frac{\delta t}{\delta p}}$$
$$-n = \frac{AT - o\frac{\delta t}{\delta p}}{\frac{\delta t}{\delta v}}.$$

In equation (3)

$$dQ = ndp + odv$$

we may substitute the above values successively giving

$$dQ = \frac{1}{\delta t} \left( n \frac{\delta t}{\delta p} dp + n \frac{\delta t}{\delta v} dv + A T dv \right).$$

$$\therefore dQ = \frac{1}{\delta t} \left( n dt + A T dv \right)$$
because 
$$dt = \frac{\delta t}{\delta p} dp + \frac{\delta t}{\delta v} dv.$$
And also 
$$dQ = \frac{1}{\delta t} \left( o \frac{\delta t}{\delta p} dp + o \frac{\delta t}{\delta v} dv - A T dp \right).$$

$$\therefore dQ = \frac{1}{\delta t} \left( o dt - A T dp \right).$$

Replacing o and n by their values in terms of X and Y,

$$dQ = A \left( Xdp + Ydv \right),$$

$$dQ = \frac{A}{\delta t} \left[ Xdt + \left( \frac{I}{\alpha} + t \right) dv \right],$$

$$dQ = \frac{A}{\delta t} \left[ Ydt + \left( \frac{I}{\alpha} + t \right) dp \right].$$

In these equations  $\alpha$  is the coefficient of dilutation, or  $\frac{1}{\alpha} + t$  is equal to T, and

$$X = \frac{1}{A} n = \frac{1}{A} \left( \frac{\delta Q}{\delta \rho} \right)_{\nu}; \quad Y = \frac{1}{A} o = \frac{1}{A} \left( \frac{\delta Q}{\delta v} \right)_{\nu}.$$

If this derivation of Zeuner's equations is borne in mind, the treatment of thermodynamics by many German writers may be readily recognized to be only a variant on that developed by Clausius and Kelvin.

### CHAPTER V.

#### PERFECT GASES.

The characteristic equation for a perfect gas is derived from a combination of the laws of Boyle and Gay-Lussac, which may be stated as follows:

Boyle's Law. — When a given weight of a perfect gas is compressed (or expanded) at a constant temperature the product of the pressure and the volume is a constant. This law is nearly true at ordinary temperatures and pressures for such gases as oxygen, hydrogen, and nitrogen. Gases which are readily liquefied by pressure at ordinary temperatures, such as ammonia and carbonic acid, show a notable deviation from this law. The law may be expressed by the equation

$$pv = p_1v_1 \dots \dots (56)$$

in which  $p_1$  and  $v_1$  are the initial pressure and volume; p is any pressure and v is the corresponding volume.

Gay-Lussac's Law. — It was found by Gay-Lussac that any volume of gas at freezing-point increases about 0.003665 of its volume for each degree rise of temperature. Gases which are easily liquefied deviate from this law as well as from Boyle's law. In the deduction of this law temperatures were measured on or referred to the air-thermometer, and the law therefore asserts that the expansibility or the coefficient of dilatation of perfect gases is the same as that of air. Gay-Lussac's law may be expressed by the equation

$$v = v_0 (1 + \alpha l) \cdot \cdot \cdot \cdot \cdot \cdot \cdot (57)$$

in which  $v_0$  is the original volume at freezing-point,  $\alpha$  is the coefficient of dilatation or the increase of volume for one degree rise of temperature, and v is the volume corresponding to the temperature t measured from freezing-point.

Characteristic Equation. — From equation (57) we may calculate any special volume, such as  $v_0$  getting

$$v_1 = v_0 (1 + \alpha t)$$
.

Assuming that  $p_1$  in equation (56) is the normal pressure of the atmosphere  $p_0$ , and substituting the value just found for  $v_0$  we have for the combination of the laws of Boyle and Gay-Lussac

$$pv = p_0 v_0 \left( \tau + \alpha t \right) = p_0 v_0 \alpha \left( \frac{\tau}{\alpha} + t \right) . . . . (58)$$

If it be assumed that a gas contracts  $\alpha$  part of its volume at freezing-point for each degree of temperature below freezing then the absolute zero of the air-thermometer will be  $\frac{1}{\alpha}$  degrees below freezing, and

$$\frac{1}{\alpha} + \ell$$

may be replaced by T, the absolute temperature by the airthermometer.

The usual form of the characteristic equation for perfect gases may be derived from equation (58) by substituting  $T_0$ , the absolute temperature of freezing-point, for  $\frac{1}{\alpha}$ , giving

$$pv = \frac{p_0 v_0}{T_0} T \bowtie RT \dots \dots (59)$$

where R is a constant representing the quantity

For solution of examples it is more convenient to write equation (59) in the form

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Absolute Temperature. — Recent investigations of the properties of hydrogen by Professor Callender \* indicate that the absolute zero is  $273^{\circ}$ .1 C. below freezing-point. This does not differ much from taking  $\alpha = 0.003665$  as given by Regnault, for which the reciprocal is 272.8. In this work we shall take for the absolute temperature

 $T = t + 273^{\circ}$  centigrade scale.  $T = t + 450^{\circ}$ .5 Fahrenheit scale.

These figures are convenient and sufficiently exact.

Relation of French and English Units. — For the purpose of conversion of units from the metric system (or vice versa) the following values may be used:

one metre = 39.37 inches. one kilogram = 2.2046 pounds.

Specific Pressure. — The normal pressure of the atmosphere is assumed to be equivalent to that of a column of mercury, 760 mm. high at freezing-point. Now Regnault † gives for the weight of a litre, or one cubic decimetre, of mercury 13.5950 kilograms; consequently the specific pressure of the atmosphere under normal conditions is

 $p_0 = 10,333$  kilograms per square metre.

Using the conversion units given above for reducing this specific pressure to the English system of units gives

 $p_o = 2116.32$  pounds per square foot,

which corresponds to

14.697 pounds per square inch,

or to

29.921 inches of mercury.

It is customary and sufficient to use for the pressure of the atmosphere 14.7 pounds to the square inch.

<sup>\*</sup> Phil. Mag., Jan., 1903.

<sup>†</sup> Mômoires de l'Institut de France, vol. xxl.

Specific Volumes of Gases. -- From recent determinations of densities of gases by Leduc, Morley, and Raleigh it appears that the most probable values of the specific volume of the commoner gases are

## VOLUMES IN CUBIC METRES OF ONE KILOGRAM.

Atmospheri	c, i	ıir		•		•			•	•	0.7733
Nitrogen .											0.7955
Oxygen .			•		٠	•					ი, ჩეცნ
Hydrogen											11.123

The corresponding quantitles for English units are given in the next table.

# VOLUMES IN CUBIC FEET OF ONE POUND,

Atmospheric air					,	,	•			14,30
Nitrogen										12.74
Oxygen .								•		11.21
Hydrogen										

To these may be added the value for earbon dioxide, 0.506 cubic metre per kilogram or 8.10 cubic feet per pound; but as the critical temperature for this substance is about 31° C., or 88° F., calculations by the equations for gases are liable to be affected by large errors.

Value of R. - The constant R which appears in the usual form of the characteristic equation for a gas represents the expression

$$\frac{p_0 v_0}{T_0}$$
.

The values for R corresponding to the French and the English system of units may be calculated as follows:

French units, 
$$R = \frac{10333 \times 0.7733}{273} + 29.27 + ... (61)$$
  
English units,  $R = \frac{2116.3 \times 12.39}{491.5} + 53.35 + ... (62)$ 

English units, 
$$R = \frac{2116.3 \times 12.39}{491.5} = 53.35$$
. (62)

Value of R for other gases may be calculated in a like manner.

Solution of Problems. — Many problems involving the properties of air or other gases may be solved by the characteristic equation

pv = RT,

or by the equivalent equation

$$\frac{pv}{T} = \frac{p_0 v_0}{T_0},$$

which for general use is the more convenient.

In the first of these two equations the specific pressure and volume to be used for English measures are pounds per square foot, and the volume in cubic feet of one pound.

For example, let it be required to find the volume of 3 pounds of air at 60 pounds gauge-pressure and at 100° F. Assuming a barometric pressure of 14.7 pounds per square inch,

$$v = \frac{53.35 (459.5 + 100)}{(14.7 + 60) 144} = 2.774$$
 cubic feet

is the volume of 1 pound of air under the given conditions, and 3 pounds will have a volume of

$$3 \times 2.774 = 8.322$$
 cubic feet.

The second equation has the advantage that any units may be used, and that it need not be restricted to one unit of weight.

For example, let the volume of a given weight of gas, at 100° C. and at atmospheric pressure, be 2 cubic yards; required the volume at 200° C. and at 10 atmospheres. Here

$$v = \frac{10 v}{473} = \frac{1 \times 2}{373},$$
 $v = \frac{473 \times 2}{10 \times 373} = 0.2536$  cubic yards.

Specific Heat at Constant Pressure. — The specific heat for true gases is very nearly constant, and may be considered to be

so for thermodynamic equations. Regnault gives for the mean values for specific heat at constant pressure the following results:

Atmosphe	ri	c o	ir							0.2375
Nitrogen										
Oxygen										0.2175
Hydroger	ì									3.400

Ratio of the Specific Heats. -- By a special experiment on the adiabatic expansion of air, Röntgen\* determined for the ratio of the specific heats of air, at constant pressure and at constant volume,

$$R = \frac{t_{\rm B}}{c_{\rm B}} < 1.405.$$

This value agrees well with a computation to follow, which depends on the application of the laws of thermodynamics to a perfect gas, and also with a determination from the theory of gases by Lovef that the ratio for air should be 1.403. If the given value for this ratio be accepted the remainder of the work in this chapter follows without any reference to the laws of thermodynamics.

Application of the Laws of Thermodynamics. The preceding statements concerning the specific heats of perfect gases and their ratio would be satisfactory were it definitely determined by experiment that the specific heat at constant volume is as nearly constant as is the specific heat at constant pressure. None of the experimental determinations (not even that by Joly ‡) can be considered as satisfactory as those for the specific heat at constant pressure; consequently there is considerable importance to be attached to the application of the laws of thermodynamics to the characteristic equation for a perfect gas, and, moreover, this application furnishes one of the most satisfactory determinations of the ratio of the specific heats.

<sup>\*</sup> Poggendorff's Annalen, vol. extvill, p. 580.

<sup>†</sup> Phil. Mag., July, 1809.

<sup>4</sup> Proc. Royal Soc., vol. xii, p. 352, 1886.

It is convenient at this place to make the application of the laws of thermodynamics by aid of equation (55), page 49.

$$c_p - c_v = AT \frac{1}{\delta_l} \frac{1}{\delta_l} \cdot \cdot \cdot \cdot \cdot \cdot \cdot \cdot (63)$$

From the equation

we have

This equation shows conclusively that if the characteristic equation is accepted the differences of the specific heats must be considered to be constant, and if one is treated as constant so also must the other. Conversely, the assumption of constant specific heats for any substance is in effect the assumption of the characteristic equation for a perfect gas.

The solution of equation (64) for the ratio of the specific heats gives

$$\kappa = \frac{c_P}{c_v} = \frac{1}{1 - \frac{AR}{c_h}}$$

$$\kappa = \frac{1}{1 - \frac{10333 \times 0.7733}{426.9 \times 273 \times 0.2375}} = 1.406.$$

For those who have not read Chapter IV, the following derivation of equation (64) may be interesting. In Fig. 26 let ab repre-

sent the change of volume at constant pressure due to the addition of heat  $c_p\Delta t$  where  $\Delta t$  is the increase of temperature; and let cb represent the change of pressure due to the addition of heat  $c_p\Delta t$ ; if ac is an isothermal, the latter change of temperature will

be equal to the former, but the heat applied will be less on account of the external work  $p\Delta v$  (approximately). Consequently,

$$c_p - c_v = A p \frac{\delta v}{\delta t} = A R,$$

the last transformation making use of the partial derivative

$$\frac{\delta v}{\delta t} = \frac{R}{\rho}$$

Thermal Capacities. — The values of the several thermal capacities for a perfect gas were derived on page 12 and may be written

$$l \approx \frac{b}{R} (c_p - c_p) \approx \frac{T}{v} (c_p - c_p) \quad , \quad (66)$$

$$m = -\frac{v}{R}(c_{\mu} - c_{\theta}) = -\frac{T}{P}(c_{\mu} - c_{\theta})$$
 . . (67)

$$\int_{C} n \approx \frac{v}{R} c_{\nu} = \frac{T}{\rho} c_{\nu} , \ldots , \qquad (68)$$

$$\sigma = \frac{p}{R}c_p - \frac{T}{v}c_p$$
 . . . . . . (69)

the transformations in equations (66) and (67) being made by aid of the characteristic equation.

General Equations. — To deduce the general equations for gases from equations (1), (2), and (3), it is only necessary to replace the letters l, m, n, and o by their values just obtained, giving

$$\ell Q = C_{\nu} d + \Delta_{P} d \vee dQ = c_{\nu} dt + (c_{\mu} - c_{\nu}) \frac{T}{\nu} dv \qquad (70)$$

Oľ.

Isothermal Line. — The equation to the isothermal line for a gas is obtained by making T a constant in the characteristic equation, so that

This equation will be recognized as the expression of Boyle's law. It is, of course, the equation to an equilateral hyperbola.

To obtain the external work during an isothermal expansion we may substitute for p in the expression

from the equation to the isothermal line just stated, using for limits the final and initial volumes,  $v_1$  and  $v_1$ ,

$$(W = p_1 v_1 \int_{v_1}^{v_2} \frac{dv}{v} = p_1 v_1 \log_0 \frac{v_2}{v_1}) \cdot \cdot \cdot (74)$$

If the problem in any case calls for the external work of one unit of weight of a gas, then  $v_1$  and  $v_2$  must be the initial and final specific volumes; but in many cases the initial and final volumes are given without any reference to a weight, and it is then sufficient to find the external work for the given expansion from the initial to the final volume without considering whether or not they are specific volumes.

The pressures must always be specific pressures; in the English system the pressures must be expressed in pounds on the square foot before using them in the equation for external work, or, for that matter, in any thermodynamic equation.

For example, the specific volume of air at freezing-point and at 14.7 pounds pressure per square inch is about 12.4 cubic feet; at the same temperature and at 29.4 pounds per square inch the specific volume is 6.2 cubic feet. The external work during an isothermal expansion of one pound of air from 6.2 to 12.4 cubic feet is

$$W = p_1 v_1 \int_{v_1}^{v_2} \frac{dv}{v} = p_1 v_1 \log_6 \frac{v_4}{v_1}$$

$$= 29.4 \times 144 \times 6.2 \log_6 \frac{12.1}{6.2} = 18,190 \text{ foot-pounds.}$$

For example, the external work of isothermal expansion from 3 cubic feet and 60 pounds pressure by the gauge to a volume of 7 cubic feet is

$$W = (60 + 14.7) \text{ 144} \times 3 \log_{\bullet} \frac{1}{3} = 27,340 \text{ foot-pounds.}$$

In both problems the pressure per square inch is multiplied by 144 to reduce it to the square foot. In the first problem the pressures are absolute, that is, they are measured from zero pressure; in the second problem the pressure by the gauge is 60 pounds above the pressure of the atmosphere, which is here assumed to be 14.7 pounds per square inch, and is added to give the absolute pressure. In careful experimental work the pressure of the atmosphere is measured by a barometer and is added to the gauge-pressure.

Isoenergic Line. — The isothermal line for a perfect gas is also the isoenergic line, a fact that may be proved as follows: The heat applied during an isothermal expansion may be calculated by making T a constant in equation (70) and then integrating; thus:

$$Q = (c_p - c_v) T_1 \int_{v_2}^{v_2} \frac{dv}{v} = (c_p - c_v) T_1 \log_{\frac{v_1}{v_1}}^{\frac{v_2}{v_2}}$$

or, substituting for  $c_p - c_\theta$  from equation (64),

$$(\widehat{Q} \sim ART_1 \log_{\sigma} \frac{v_2}{v_1} \sim A p_1 v_1 \log_{\sigma} \frac{v_2}{v_1})$$
. (75)

A comparison of equation (75) with equation (74) shows that the heat applied during an isothermal expansion is equivalent to the external work, or we may say that all the heat applied is changed into external work, so that the intrinsic energy is not changed. This conclusion is based on the assumption that the properties are accurately represented by the characteristic equation and that the specific heats are constant. As both assumptions are approximate so also is the conclusion, as will appear in the discussion of flow through a porous plug.

An interesting corollary of the discussion just given is that an infinite isothermal expansion gives an infinite amount of work. Thus the area contained between the axis OV (Fig. 27), the ordinate ab, and the isothermal line  $a\alpha$  extended without limit is

$$W = p_a v_a \log_a \frac{\infty}{v_a} = \infty.$$



This may also be seen from the consideration that if heat be continually applied, and all changed into work, there will be a limitless supply of work.

Adiabatic Lines. — During an adiabatic change — for example, the expansion of a gas in a non-conducting cylinder — heat is not communicated to, nor abstracted from, the gas; consequently dQ in equations (70), (71), and (72) becomes zero.

From equation (72)

$$\begin{aligned}
\phi &= dQ = c_v \frac{T}{p} dp + c_v \frac{T}{v} dv; \\
\therefore \frac{c_v}{c_v} \frac{dv}{v} &= -\frac{dp}{p}; \\
\therefore \log_\theta \left(\frac{v}{v_i}\right)^{o_v} &= \log_\theta \left(\frac{\rho_1}{p}\right).
\end{aligned}$$

The ratio  $\frac{c_p}{c_o}$  of the specific heats may be represented by  $\kappa$ , and the above equation may be written

$$\left(\frac{v}{v_1}\right)^{\kappa} = \frac{p_1}{\rho} \cdots \cdots (76)$$

$$v^* p = v_1^* p_1 = \text{const.} \qquad (77)$$

This is the adiabatic equation for a perfect gas which is most frequently used. If adiabatic equations involving other variables, such as  $v_1$  and  $T_1$ , are desired, they may be derived from equation (76) by aid of the characteristic equation, which for this purpose may be written

Or equations (78) and (79) may be deduced directly from equation (70) as equations (76) and (77) were from equation (72).

In like manner we may deduce from equation (71)

$$T_{p}^{\underbrace{1-\kappa}{\kappa}} = T_{1}p_{1}^{1-\kappa} \qquad (80)$$

or we may derive it from equation (76).

To find the external work the equation

may be used after substituting for p from equation (77)

In Fig. 28 the area between the axis OV, the ordinate ba, and the adiabatic line  $a\alpha$  extended without limit, becomes

$$W_1 = \frac{p_1 v_1}{\kappa - 1}$$



and not infinity, as is the case with the isothermal line.

Here, as with the calculation of external work during isothermal expansion, specific volumes should be used when the problem involves a unit of weight; but work may be calculated for any given initial and final volumes without considering whether they are specific volumes or not. The pressures are always pounds on the square foot for the English system.

For example, the external work of adiabatic expansion from 3 cubic feet and 60 pounds pressure by the gauge to the volume of 7 cubic feet is

$$W = \frac{74.7 \times 144 \times 3}{3.405 - 1} \left\{ 1 - \left(\frac{3}{7}\right)^{1.405 - 1} \right\} = 23,140 \text{ fool-pounds},$$

which is considerably less than the work for the corresponding isothermal expansion.

Attention should be called to the fact that calculations by this method are subject to a considerable error from the fact that the denominator of the coefficient contains the term  $\kappa - 1$  equal to 0.405; if it be admitted that the last figure is uncertain to the extent of two units, the error of calculation becomes half a parcent.

Intrinsic Energy. — Since external work during an adiabatic expansion is done at the expanse of the intrinsic energy, the work obtainable by an infinite expansion cannot be greater than the intrinsic energy. If it be admitted that such an expansion changes all of the intrinsic energy into external work we have

$$\left( E_1 = W_1 = \frac{p_1 v_1}{\kappa - 1} \dots \dots \right)$$

which gives a ready way of calculating intrinsic energy. As practice we always deal with differences of intrinsic energy, so that even if there be a residual intrinsic energy after an inflation adiabatic expansion the error of our method will be climinally from an equation having the form

$$E_1 - E_2 = \frac{p_1 v_1}{\kappa - 1} - \frac{p_2 v_2}{\kappa - 1} \qquad (33)$$

exponential Equation. — The expansions and compressions and compressions and compressions and other gases in practice are seldom exactly isothermal adiabatic; more commonly an actual operation is intermediate between the two. It is convenient and usually sufficient to represent such expansions by an exponential equation,

$$pv^n = p_1v_1^n \dots \dots$$

in which n has a value between unity and 1.405. The form integration for external work is the same as for that of adiabatic expansion, and the amount of external work is intermediate between that for adiabatic and that for isothermal expansion.

ENTROPY

Change of temperature during such an expansion may be calculated by the equations

$$Tv^{n-1} = T_1v_1^{n-1} \dots (85)$$
  
 $Tp^{\frac{1-n}{n}} = T_1p_1^{\frac{1-n}{n}} \dots (86)$ 

which may be deduced from equation (84) by aid of the characteristic equation pv = RT

as equation (79) is deduced from equation (76).

If it is desired to find the exponent of an equation representing a curve passing through two points, as  $a_1$  and  $a_2$  (Fig. 29), we may proceed by taking logarithms of both sides of the equation

ation 
$$p_1 v_1^n = p_2 v_2^n,$$

giving

$$n \log v_1 + \log p_1 = n \log v_2 + \log p_2,$$

so that

is

$$n = \frac{\log p_1 - \log p_2}{\log v_2 - \log v_1} . . . . . . . . (87)$$

For example, the exponent of an equation to a curve passing through the points

$$p_1 = 74.7$$
,  $v_1 = 3$ , and  $p_2 = 30$ ,  $v_2 = 7$ ,
$$n = \frac{\log 74.7 - \log 30}{\log 7 - \log 3} = 1.104.$$

It should be noted that as n approaches unity the probable error of calculation of external work is liable to be very large.

Entropy. — For any reversible process

$$d\phi = \frac{dQ}{T};$$

consequently from equations (70), (71), and (72) we have

$$d\phi = c_v \frac{dt}{T} + (c_p - c_v) \frac{dv}{v},$$

$$d\phi = c_p \frac{dt}{T} + (c_v - c_p) \frac{dp}{p},$$

$$d\phi = c_v \frac{dp}{p} + c_p \frac{dv}{v};$$

and, integrating between limits,

$$\phi_2 = \phi_1 \approx c_v \log_v \frac{T_2}{T_1} + (c_p - c_v) \log_v \frac{v_2}{v_1}$$
. (8

$$\phi_2 = \phi_1 = c_p \log_p \frac{T_2}{T_1} + (c_p - c_\sigma) \log_\sigma \frac{p_1}{p_2}$$
 . (8)

$$\phi_2 = \phi_1 = c_0 \log_\theta \frac{p_2}{p_1} + c_\mu \log_\theta \frac{v_2}{v_1} + \cdots$$
 (5

which give ready means of calculating changes of entropy These equations give the entropy changes per pound, and are be multiplied by the weight in pounds to give the change the actual conditions.

For example, the change of entropy in passing from the pr sure of 74.7 pounds absolute per square inch and the volu of 3 cubic feet to the pressure of 30 pounds absolute and i volume of 7 cubic feet is

$$\phi_2 = \phi_1 = \frac{0.2375}{1.405} \log_6 \frac{30}{74.7} + 0.2375 \log_6 \frac{7}{3} = 0.0454.$$

Since the pressures form the numerator and denominator a fraction, there is no necessity to reduce them to the squ foot. In this problem the pressures and volumes are taken random; they correspond to a temperature of 146° F., at initial condition. As has already been said, there is seld occasion in practice for using the entropy of a gas.

Comparison of the Air-Thermometer with the Absolute Sca-In connection with the isodynamic line it was shown that intrinsic energy is a function of the temperature only. T conclusion is deduced from the characteristic equation on assumption that the scale of the air thermometer coincides we the thermodynamic scale, and it affords a delicate method testing the truth of the characteristic equation, and of compart the two scales.



The most complete experiments for this purpose were made by Joule and Lord Kelvin, who forced air slowly through a porous plug in a tube in such a manner that no heat was transmitted to or from the air during the process. Also the velocity both before and beyond the plug was so small that the work due to the change of velocity could be disregarded. All the work that would be developed in free expansion from the higher to the lower pressure was used in overcoming the resistance of friction in the plug, and so converted into heat, and as none of this heat escaped, it was retained by the air itself, the plug remaining at a constant temperature. It therefore appears that the intrinsic energy remained the same, and that a change of temperature indicated a deviation from the assumptions of the theory of perfect gases.

In the discussion of results given by Joule and Lord Kelvin\* in 1854 they gave for the absolute temperature of freezing-point 27,3°.7°C. As the result of later experiments† they stated that the cooling for a difference of pressure of 100 inches of mercury was represented on the centigrade scale by

$$\circ \circ_{\mathcal{O}^{1}} \left( \frac{273:7}{T} \right)^{2}$$

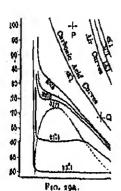
From these experiments and from other considerations concerning the constant volume hydrogen thermometer, Professor Callendar has determined that the most probable value for the absolute temperature of freezing-point is 273°.1°C., as already given, and gives a table of corrections to the hydrogen thermometer to obtain temperatures on the absolute scale. As the correction at any temperature between — 200° and + 450° C, is not more than 180 of a degree this is interesting mainly to physicists. The corrections for the air-thermometer at constant pressure are somewhat larger, but approach 18 of a degree only at 300° C.

<sup>\*</sup> Phil. Trans. vol. cxllv, p. 349.

<sup>† 1</sup>bid. vol. clil, p. 579.

Deviation from Boyle's Law. — Early experiments on the permanent gases (as they were then known) indicated that there were small deviations evident to a physicist, but not of importance to engineers; but now that air is compressed to pressures as high as 2500 pounds per square inch, it becomes necessary to take account of such deviations in engineering practice.

Perhaps the best conception of this subject, and of the four recognized states of fluids, can be had from a consideration of Andrews' \* experiments, which for the present purpose are conveniently represented by his isothermal curves, which are reproduced in Fig. 29a, together with the curves for air. The latter are approximate hyperbolæ referred to the proper axes, that for zero pressure being nearly the whole height of the diagram below the figure as it is drawn. At 48°.1°C., the isothermal for carbonic acid shows a marked deviation from the hyperbola, as may be seen by comparison with the curves for air, or better from the fact that a rectangular hyperbola through P will pass through Q. On the other hand, the isothermal for 13°.1 resembles that for steam, which is commonly known as a saturated



vapor whose pressure is constant at constant temperature; the horizontal part of this line represents a mixture of liquid and vapor which at the left runs into the liquid curve, and as liquid carbonic acid has considerable compressibility, this curve becomes a straight line with an appreciable inclination to the axis of zero volume. At the right, the isothermal shows a decided break and slopes away as the volume becomes larger than that of the saturated vapor. The isothermal for 21°.5 shows similar characteristics, but

the passages from one condition to another are more gradual. The dotted curve is drawn through the points of saturation and liquofaction, and its crest corresponds to the critical temperature.

<sup>\*</sup> Phil. Trans., 1869, part II, p. 575, and 1876, part II, p. 421.

The isothermal for 31. or is clearly above the critical temperature and does not indicate a liquefaction.

The several states of a fluid may be enumerated as

- r. Liquid.
- Saturated vapor, including mixtures of liquid and vapor.
- Superheated vapor characterized by a larger volume than saturated vapor for a given temperature and pressure.
- 4. Gas; near the critical temperature the deviations from Hayle's law are very large, at higher temperature the deviations diminish and become unimportant.

Critical Temperatures. The following table of critical temperatures and of boiling points at atmospheric pressure is taken in part from Preston's "Theory of Heat," 1904.

							Halling Paint.	Cellical Touguerque
Hydrogen							- 281.07 (	'. 234.08 C.
Nitrogen .		,		,	1		1944	1 Ju
Oxygen				٠			182.2	8.811
Air							tot.4	1.10
Carlen monoxid	t-		3			,	∞ tgo	-139.5
Carbon dioxide					•	,	- 78.3	4.31.35
Sulphur dioxide				,			10	+157.0
Ether							44.5	175
Alcohol							78.4	4.18
Carbon bisulphi	ale:						43-3	254
Water							100	30.1

Dansity at High Pressure. If the usual methods (given on page §8) for the solution of problems involving the properties of gases, are applied with very high pressure, errors amounting to two or three per cent are liable to be incurred, owing to the deviation from Hoyle's law. In some cases, this error may be ignored in engineering practice; in some cases the error may be included in a practical factor, as will be indicated in the design of air compressors; and in other cases allowances must be made from the experimental information furnished by Armagat, and which may be found in Landolt and Bornstein's Tables.

Röntgen's Experiments. — Direct experiments to determine  $\kappa$  may be made as follows. Suppose that a vessel is filled with air at a pressure  $p_1$ , while the pressure of the atmosphere is  $p_4$ . Let a communication be opened with the atmosphere sufficient to suddenly equalize the pressure; then let it be closed, and let the pressure  $p_4$  be observed after the air has again attained the temperature of the atmosphere. If the first operation is sufficiently rapid it may be assumed to be adiabatic, and we may use equation (77), from which

The second operation is at constant volume; consequently the specific volume is the same at the final state as after the adiabatic expansion of the first operation. But the initial and final temperatures are the same; consequently

$$v_1 p_1 = v_n p_2;$$

$$\therefore \log v_n - \log v_1 = \log p_1 - \log p_2;$$

which substituted in equation (91) gives

The same experiment may be made by rarefying the air in the vessel, in which case the sign of the second term changes. Röntgen\* employed this method, using a vessel containing 70 litres, and measuring the pressure with a gauge made on the same principle as the aneroid barometer. Instead of assuming the pressure  $p_a$  at the instant of closing the stop-cock to be that of the atmosphere, he measured it with the same instrument. A mean of ten experiments on air gave

<sup>\*</sup> Poggendorff's Annalen, vol. cxivili, p. 580.

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#### EXAMPLES.

1. Find the weight of 4 cubic metres of hydrogen at 30° C., and under the pressure of 800 mm, of mercury. Ans. 0.341 kg.

2. Find the volume of 3 pounds of nitrogen at a pressure of 15 pounds to the square inch by the gauge and at 80° F. Ans. 11.05.

3. Find the temperature at which one kilogram of air will occupy one cubic metre when at a pressure of 20,000 kilograms per square metre. Ans. 410° C.

4. Oxygen and hydrogen are to be stored in tanks 10 inches in diameter and 35 inches long. At a maximum temperature of 110° F., the pressure must not exceed 250 pounds gauge. What weight of oxygen can be stored in one tank? What of hydrogen? Ans, Oxygen 2.21 pounds. Hydrogen 0.138 pound.

- 5. A balloon of 12,000 cubic feet capacity, weighing with car, occupant, etc., 665 pounds, is inflated with 9500 cubic feet hydrogen at 60° F., the barometer reading 30 inches. Find the weight of the hydrogen and the pull on the anchor rope; find also the amount that the balloon must be lightened to reach a height where the barometer reads 20 inches, and the temperature is 10° below zero Fahrenheit. Ans. Weight hydrogen 50.4 pounds; pull on rope 12 pounds; balloon lightened 7.5 pounds.
- 6. A gas-receiver holds 14 ounces of nitrogen at 20° C., and under a pressure of 29.6 inches of mercury. How many will it hold at 32° F., and at the normal pressure of 760 mm.? Ans. 15.18 ounces.
- 7. A gas receiver having the volume of 3 cubic feet contains half a pound of oxygen at 70° F. What is the pressure? Ans. 20.6 pounds per square inch.
- 8. Two cubic feet of air expand at 50° F. from a pressure of 80 pounds to a pressure of 60 pounds by the gauge. What is the external work? Ans. 6464 foot-pounds.
- 9. What would have been the external work had the air expanded adiabatically? Ans. 4450 foot-pounds.

X

10. Find the external work of 2 pounds of air which expand adiabatically until the volume is doubled, the initial pressure being 100 pounds absolute and the initial temperature 100° F. Ans. 36,100 foot-pounds.

11. Find the external work of one kilogram of hydrogen, which, starting with the pressure of 4 atmospheres and with the temperature of 500° C., expands adiabatically till the tempera-

ture becomes 30° C. Ans. 489,000 m.-kg.

12. Find the exponent for an exponential curve passing through the points p = 30, v = 1.9, and  $p_1 = 15$ ,  $v_1 = 9.6$ . Ans. 0.4279.

13. Find the exponent for a curve to pass through the points p = 40, v = 2, and  $p_1 = 12$ ,  $v_1 = 6$ . Ans. 1.0959.

14. In examples 12 and 13 let p be the pressure in pounds on the square inch and v the volume in cubic feet. Find the external work of expansion in each case. Ans. 21,900 and 12,010 foutpounds.

15. Find the intrinsic energy of one pound of nitrogen under the standard pressure of one atmosphere and at freezing-point

of water. Ans. 66,500 foot-pounds.

16. A cubic foot of air at 492.7° F. exerts 14.7 pounds gauge pressure per square inch. How much do its internal energy and boits entropy exceed those of the same air under standard conditions? Ans. 5052 foot-pounds; .00012 units of entropy.

17. Find the increase in entropy of 2 pounds of a perfect gas during isothermal expansion at 100° F. from an initial pressure of 84.3 pounds gauge and a volume of 20 cubic feet to a final volume of 40 cubic feet. Ans. 0.453.

18. A kilogram of oxygen at the pressure of 6 atmospheres. and at 100° C. expands isothermally till it doubles its volume. Find the change of entropy. Ans. 0.0434.

19. Twenty pounds of air are heated at a constant pressure of 200 pounds absolute per square inch until the volume increases from 20 cubic feet to 40 cubic feet. Find the initial and final temperatures, the change in internal energy and the increase in entropy. How much heat is added? Ans. 80° and 620°;

increase of intrinsic energy 1,420,000 foot-pounds; increase in entropy 3.29; heat 2570 B.T.U.

20. Suppose a hot-air engine, in which the maximum pressure is 100 pounds absolute, and the maximum temperature is 600° F., to work on a Carnot cycle. Let the initial volume be 2 cubic feet, let the volume after isothermal expansion be 5 cubic feet, and the volume after adiabatic expansion be 8 cubic feet. Find the horse-power if the engine is double-acting and makes 30 revolutions per minute. Ans. 8.3 horse-power.

## CHAPTER VI.

#### SATURATED VAPOR.

For engineering purposes steam is generated in a boiler which is partially filled with water, and arranged to receive heat from the fire in the furnace. The ebullition is usually energetic, and more or less water is mingled with the steam; but if there is a fair allowance of steam space over the water, and if proper arrangements are provided for with drawing the steam, it will be found when tested to contain a small amount of water, usually between half a per cent and a per cent and a half. Steam which contains a considerable percentage of water is passed through a separator which removes almost all the water. Such steam is considered to be approximately dry.

If the steam is quite free from water it is said to be dry and saturated; steam from a boiler with a large steam space and which is making steam very slowly is nearly if not quite dry.

Steam which is withdrawn from the boiler may be heated to a higher temperature than that found in the boiler, and is then said to be superheated.

Our knowledge of the properties of saturated steam and other vapors is due mainly to the experiments of Regnault,\* who determined the relations of the temperature and pressure, the total heat of vaporization, and the heat of the liquid for many volatile liquids. Since his time, Rowland's determination of the mechanical equivalent of heat, gave a more exact determination of the specific heat of water at low temperatures, and recently Dr. Barnes has given a very precise determination of that property for water. Again, certain work by Knoblauch, Linde, and Klebe, has given us a good knowledge of the properties

Mémoires de l'Institut de France, etc., tome xxvi.





of superhented steam which can be extended to give the specific volume of saturated steam over a considerable range of temperature. At the time when the first edition of this work was prepared it appeared desirable to compute tables of the properties of saturated vapor, taking advantage of Rowland's work, and eliminating some uncertainties due to the way in which Regnault used his empirical equations in computating tables. As all this involved changes of sufficient magnitude to influence engineering computations, it seemed necessary to quote the original data at length and to give computations in detail. introduction to the chapter on saturated vapors was found to be somewhat confusing to students reading it for the first time, and since the main points are now commonly accepted, this work is given only in the introduction to the "Tables of the Properties of Saturated Steam," the reason for printing it being that it is not given elsewhere, as the earlier editions have passed out of print.

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Recent correction of the absolute temperature of the freezing-point of water by Callendar and the determination of the specific heat of water by Barnes make it necessary to recompute the "Tables of the Properties of Saturated Steam" which are intended to accompany this book, and opportunity is taken to introduce further data in those tables, and in addition a table has been prepared which will be found to greatly facilitate calculations of adiabatic changes of steam and water.

Pressure of Saturated Vapors. — Regnault expressed the results of his experiments on the temperature and pressure of saturated vapors in the form of the following empirical equation,

$$\log p = a + b\alpha^n + c\beta^n \qquad (94)$$

where p is the pressure, n is the temperature minus the temperature  $t_0$  of the lowest limit of the range of temperature to which the equation applies, i.e.;

$$n = l - l_0$$

The constants for the above equation as applied to saturated steam have been recomputed and reduced to the latitude of 45°, and are as follow:

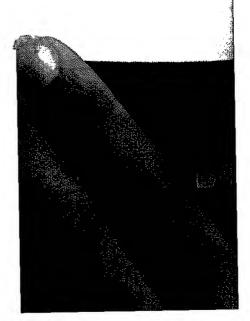
mm, of mercury,

C. For steam from 100° to 220° C. expressing the pressure in mm. of mercury,

B<sub>1</sub>. For steam from 32° to 212° F. in pounds per square inch,

 $C_1$ . For steam from 212° to 428° F. in pounds per square inch,

Pressure of Other Vapors.—Regnault determined also the pressure of a large number of saturated vapors at various temperatures, and deduced equations for each in the form of equation (94). The equations and the constants as determined by him for the commoner vapors are given in the following table:



	log s	c#	ь	
Alcohol	$\begin{array}{c} a \leftarrow b\alpha^n + \epsilon f^n \\ a + b\alpha^n + \epsilon f^n \\ a \leftarrow b\alpha^n + \epsilon f^n \end{array}$	5,4562028 5,0286298 5,2253893 5,4011662 12,0962331	4,9809960 0,0002284 2,9531281 3,4405663 9,1375180	0.0668673

	log a	log #	24	Limite.
Alcohol	T.99708557 0.0145775 T.9974144 T.9977628 T.9997120		1 -1- 20 1 20 1 -1- 20	20°, +- 150° C. 20°, +- 120° C. 20°, +- 164° C. 20°, +- 140° C. 20°, +- 188° C.

Zeuner\* states that there is a slight error in Regnault's calculation of the constants for aceton, and gives instead

$$\log p = a - b\alpha^n + c\beta^n;$$

$$a = 5.3085419;$$

$$\log b\alpha^n = -1.0.5312766 - 0.0026148 t;$$

$$\log c\beta^n = -0.9645222 - 0.0215592 t.$$

Differential Coefficient  $\frac{dp}{dt}$ .— From the general form of equation (94) we have

$$\log_a p = \frac{1}{M} a + \frac{1}{M} b \alpha^n + \frac{1}{M} c \beta^n . . . . . (95)$$

M being the modulus of the common system of logarithms. Differentiating,

$$\frac{dp}{pdt} \approx \frac{1}{M} b \log_{\theta} \alpha \cdot \alpha^{n} + \frac{1}{M} c \log_{\theta} \beta \cdot \beta^{n};$$

or, reducing to common logarithms,

$$\frac{1}{p}\frac{dp}{dt} = \frac{1}{M^2}b\log\alpha \cdot \alpha^n + \frac{1}{M^2}c\log\beta \cdot \beta^n.$$

$$\therefore \quad \frac{1}{p} \frac{dp}{dt} = A\alpha^n + B\beta^n.$$

\* Mechanische Wärmelheorte.

B. For oo to 1000 C., mm. of mercury,

log 
$$A = 8.8512729 - 10$$
;  
log  $B = 6.69305 - 10$ ;  
log  $\alpha_1 = 9.996725828 - 10$ ;  
log  $\beta_1 = 0.0068641$ .

C. For 100° to 220° C., mm. of mercury,

$$\log A = 8.5495158 - 10;$$
  
 $\log B = 6.34931 - 10;$   
 $\log \alpha_1 = 9.997411296 - 10;$   
 $\log \beta_1 = 0.0076418.$ 

#### English Units.

B<sub>1</sub>. For 32° to 212° F., pounds on the square inch,  $\log A = 8.5960005 - 10; \\ \log B = 6.43778 - 10; \\ \log \alpha_2 = 9.998181015 - 10; \\ \log \beta_2 = 0.0038134.$ 

C1. For 212° to 428° F., pounds on the square inch,

$$\log A = 8.2942434 - 10;$$
  
 $\log B = 0.09403 - 10;$   
 $\log \alpha_2 = 9.998561831 - 10;$   
 $\log \beta_2 = 0.0042454.$ 

It is to be remarked that  $\frac{dp}{dt}$  may be found approximately by dividing a small difference of pressure by the corresponding difference of temperature; that is, by calculating  $\frac{\Delta p}{\Delta t}$ . With a table for even degrees of temperature we may calculate the value approximately for a given temperature by dividing the difference of the pressures corresponding to the next higher and the next lower degrees by two.

The following table of constants for the several vapors named were calculated by Zeuner from the preceding equations for temperature and pressure of the same vapors:



differential.	COEFFICIENT	I.	$\frac{dp}{d\hat{t}}$ .
---------------	-------------	----	-------------------------

	Sto	iN.	log (Æu <sup>n</sup> )	log (BA <sup>n</sup> )
Alcohol Ether Chloraform Carbon hisulphide Carlon tetrachloride Accton	# # # # # # # # # # # # # # # # # # #	#;" · + + + +	- 1.1730041 - 0.0039143 / - 1.3106024 - 0.0031221 / - 1.340130 - 0.003856 / - 1.340130 - 0.003856 / - 1.4801078 - 0.00386 / - 1.3268515 - 0.0024174 /	-2 0002701-0 05005151 -4.4616396+0.01457731 -2.0667124-0.01318311 -2.051098-0.0980031 -1.3812105-0.00502201 -1.9064582-0.02155031

Standard Temperature. -- It is customary to refer all calculations for gases to the standard conditions of the pressure of the atmosphere (760 mm, of mercury) and to the freezing-point of water. Formerly the freezing-point was taken as the standard temperature for water and steam as even now it is the initial point for tables of the properties of saturated vapors. But the investigation of the mechanical equivalent of heat by Rowland resulted in a determination of the specific heat of water with much greater delicacy than is possible by Regnault's method of mixtures, and showed that freezing-point is not well adapted for the standard temperature for water. It has been the habit of physicists for many years to take 15° C. as the standard temperature, and this corresponds substantially with 62° F., at which the English units of measure are standard. Professor Callendar recommends 20° C. as the standard temperature which would make a variation of about 1000 in the value of the mechanical equivalent of heat and in the specific heat of water.

Mechanical Equivalent of Heat. — The most authoritative determination of the mechanical equivalent of heat appears to be that by Rowland,\* from which the work required to raise the temperature of one pound of water from 62° to 63° F. is

778 foot-pounds.

This is equivalent to

427 metre kilograms

in the metric system. Since his experiments were made this important physical constant has been investigated by several

\* Proc. Am. Acad., vol. xv (N. S. vil), 1879.

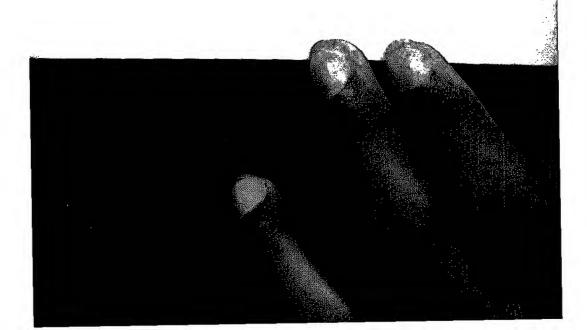
made after a recomparison of his thermometers. The conclusion appears to be that his results may be a little small, but the differences are not important, and it is not certain that the conclusion is valid. There seems, therefore, no sufficient reason for changing the accepted values given above.

Heat of the Liquid. — The most reliable determination of the specific heat of water is that by Dr. Barnes,\* who used an electrical method devised by Professor Callendar and himself, and who extended the method to and below freezing-point by carefully cooling water without the formation of ice, to - 5° C. This method gives relative results with great refinement, and gives also a good confirmation of Rowland's determination of the mechanical equivalent of heat. Dr. Barnes reports values of the specific heat of water up to 95° C. In the following table his results are quoted from 0° to 55° C.; from 55° to 95° his results have been slightly increased to join with results determined by recomputing Regnault's experiments on the heat of the liquid for water (which experiments range from 110° C. to 180° C.) by allowing for the true specific heat at low temperature from Dr. Barnes's experiments. The maximum effect of modifying Dr. Barnes's results is to increase the heat of the liquid at 95° by one-tenth of one per cent.

SPECIFIC HEAT OF WATER.

C. F.		Specific	Tempe	rature.	Specific	Temper	Specific	
		Heat.	c.	F.	Heat.	c.	F.	Specific Heat.
5 10 15 20 25 30 35	32 41 50 59 68 77 86 95	1.0094 1.00530 1.00230 1.00030 0.99895 0.99806 0.99759 0.99735	45 50 55 60 65 70 75 80 85	113 122 131 140 149 158 167 176 185	0.99760 0.99800 0.99850 0.99940 1.00040 1.00150 1.00275 1.00415	90 95 100 120 140 160 180 200	194 203 212 248 284 320 356 392 428	1.0070 1.0085 1.0101 1.0169 1.0223 1.0285 1.0347 1.0410

<sup>\*</sup> Physical Review, vol. xv, p. 71, 1902.



In order to use this equation it would be necessary to obtain an empirical equation connecting the specific heat with the temperature; such an equation has not been proposed and would probably be complex. Another method is to draw a curve with temperatures as abscisse and specific heats as ordinates and integrate graphically. The fact that the specific heat is nearly equal to unity at all temperatures and that consequently the heat of the liquid for the Centigrade thermometer is not very different from the temperature suggests the following method:

Let 
$$c = r + k$$

when k is the difference between the specific heat and unity at any temperature, k being positive or negative as the case may be.

Then 
$$q = t + \int kdt$$
 . . . . . . (97)

which may be obtained by plotting values of k as ordinates and integrating graphically, which will have the advantage that the required curve may be drawn to a large scale and give correspondingly accurate results. The values for the heat of the liquid for water in the "Tables of the Properties of Saturated Steam" were obtained in this way.

The following table gives equations for the heats of the liquids of other substances than water, determined by Regnault.

### HEAT OF THE LIQUID.

					•	•••	•••	•	٠,	•		•••	1/4.50 21.11
Alcohol			•				٠	•		•	•		q == 0.54754 t -1- 0.0011218 t3 -1- 0.00002206 t3
Ether													q = 0.529011 -1- 0.0002959 12
Chloroform								٠				٠	n == 0,23235 f -1 0,0000507 f
Carbon blac	սի	sbl	de	•			,					,	# ## 0,23523 ! - 0.0000815 !*
Carbon tetr	'nċ	hl	orl	de									q == 0.197981 -1- 0.00009001*
Acutou							•						am a ratio tak a manafe !



differentiation; for example, the specific heat for alcohol is

$$c = 0.54754 + 0.00234367 + 0.0000006187^3$$

Total Heat.—This term is defined as the heat required to raise a unit of weight of water from freezing point to a given temperature, and to entirely evaporate it at that temperature. The experiments made by Regnault were in the reverse order; that is, steam was led from a boiler into the calorimeter and there condensed. Knowing the initial and final weights of the calorimeter, the temperature of the steam, and the initial and final temperatures of the water in the calorimeter, he was able, after applying the necessary corrections, to calculate the total heats for the several experiments.

The results from these experiments are represented by the following equations:

For the metric system,

$$H = 606.5 + 0.305 t + ... + (98)$$

For the English system,

An investigation of the original experimental results, allowing for the true specific heat of the water in the calorimeter, showed that the probable errors of the method of determining the total heat were larger than the deviations of the true specific heats from unity, the value assumed by Regnault; and, further, it appeared that his equation represents our best knowledge of the total heat of steam. There appears to be no reason for changing this equation till new experimental values shall be supplied. The deviation of individual experimental results from corresponding computations by the equation is likely to be one in five hundred. There is further some uncertainty whether the method of drawing steam from the holler did not involve some error due to entrained moisture. The best check upon Regnault's results is a comparison with Knoblauch's work on superheated steam.



Regnault gives the equations following for other liquids;

Ether	•	•					II =	94	+	0.451 - 0.000555561
Chloroform	٠	•	٠	٠	•	٠	[[ #a	07	-{-	0.1375 $t$ 0.14601 $t = 0.0004123 t^2$
Carbon tetrachloride	:	•	:	•	•	•	II m	63	.l.	$0.14625 t - 0.000172 t^{2}$
Aceton	:	Ċ		:	Ċ		II m	140.5	÷	$0.36644 t - 0.000516 t^2$

Heat of Vaporization. — If the heat of the liquid be subtracted from the total heat, the remainder is called the heat of vaporization, and is represented by r, so that

Specific Volume of Liquids. — The coefficient of expansion of most liquids is large as compared with that of solids, but it is small as compared with that of gases or vapors. Again, the specific volume of a vapor is large compared with that of the liquid from which it is formed. Consequently the error of neglecting the increase of volume of a liquid with the rise of temperature is small in equations relating to the thermodynamics of a saturated vapor, or of a mixture of a liquid and its vapor when a considerable part by weight of the mixture is vapor. It is therefore customary to consider the specific volume of a liquid  $\sigma$  to be constant.

The following table gives the specific gravities and specific volumes of liquids:

SPECIFIC GRAVITIES AND SPECIFIC VOLUMES OF LIQUIDS.

						Specific Gravity compared	Speelfic V	olume.
						with Water at 4° C.	Cubic Matres.	Cubic Feet
Alcohol Ether		•				0.80625	0 001240	,
Ether				٠		0.736	0 001350	1
Chloroform						1.527	0.000055	ļ
Carbon bisulphide .						1.2022	0 000774	ſ
Carbon tetrachloride						3.6320	0.00013	
Aceton			,			0,8ï	0.00123	1
Sulphur dloxide .						1.4336	0.0006081	0,0111
Ammonia						0.6364	0.001571	0.0252
Water						1	0.001	0.0100

Experiments were made by Hirn\* to determine the volumes of liquid at high temperatures compared with the volume at freezing-point, by a method which was essentially to use them for the expansive substance of a thermometer. The results are given in the following equations:

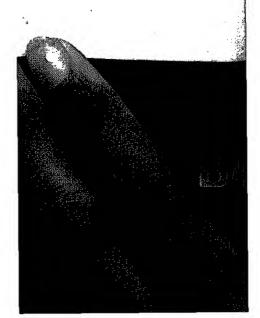
# SPECIFIC VOLUMES OF HOT LIQUIDS.

		Logarithms
Water, 100° C. to 200° C. (Vol. at 4° = unity.)	v = 1 + 0.00010867875 i + 0.0000030073653 i + 0.000000028730422 i - 0.0000000000066457031 ii	6.0361445 - 19 4.4781862 - 19 1.4583419 - 19 8.8225400 - 20
Alcohol, 30° C. to 160° C. (Vol. at 0° = unity.)	υ = 1 + 0.00073892265 t + 0.00001055235 t <sup>3</sup> - 0.000000092180842 t <sup>3</sup> + 0.0000000040413567 t <sup>4</sup>	6.8685091 - 10 3.0233492 - 10 2.0660517 - 10 0.6665278 - 10
Ether, 30° C. to 130° C. (Vol. at 0° = unity.)	v = 1 + 0.0013489050 t + 0.000005537t <sup>3</sup> - 0.00000034490756 t <sup>3</sup> + 0.0000000033773062 t <sup>4</sup>	7.1200817 - 10 4.8164866 - 19 2.5377028 - 10 0.5285571 - 10
Carbon Bisulphide, 30° C. to 160° C. (Vol. at 0° = unity.)	$\begin{array}{c} v = 1 + 0.0011680559 t \\ + 0.0000016489598 t^3 \\ - 0.0000000081119062 t^3 \\ + 0.000000000000046589 t^4 \end{array}$	7.0674636 - 10 4.2173103 - 10 0.0001320 - 10 9.7849494 - 20
Carbon Tetrachloride, 30° C. to 160° C. (Vol. at 0° = unity.)	$ \begin{array}{l} \nu = 1 + 0.0010671883 t \\ + 0.0000035651378 t^3 \\ - 0.000000014949281 t^3 \\ + 0.000000000085182318 t^4 \end{array} $	7.0282400 - 10 4.5520763 - 10 2.174620 - 10 0.0303494 - 20

Quality or Dryness Factor. — All the properties of saturated steam, such as pressure, volume and heat of vaporization, depend on the temperature only, and are determinable either by direct experiment or by computation, and are commonly taken from tables calculated for the purpose.

Many of the problems met in engineering deal with mixtures of liquid and vapor, such as water and steam. In such problems it is convenient to represent the proportions of water and steam by a variable known as the quality or the dryness factor; this

\* Annales de Chimie et de Physique, 1867.



factor, x, is defined as that portion of a pound of the mixture which is steam; the remnant, 1 - x, is consequently water.

Specific Volume of Wet Steam. — Let the specific volume of the saturated vapor be s and that of the liquid be  $\sigma$ ; then the change of volume is  $s-\sigma=u$  on passing from the liquid to the vaporous state. If a pound of a homogeneous mixture of water and steam is w part steam, then the specific volume may be represented by

$$v = xs + (1 - x)\sigma = xu + \sigma$$
, . . . (101)

where u is the increase of volume due to vaporization.

Internal and External Latent Heat. — The heat of vaporization overcomes external pressure, and changes the state from liquid to vapor at constant temperature and pressure. The external work is

$$p(s-\sigma)=pu,$$

and the corresponding amount of heat, or the external latent heat, is

$$Ap(s-\sigma)=Apu.$$

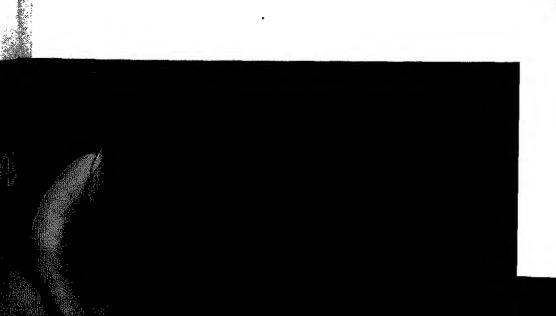
The heat required to do the disgregation work, or the internal latent heat, is

$$\rho = r - A pu$$
 . . . . . (102)

General Equation. — In order to apply the general thermodynamic method to a mixture of a liquid and its vapor, it is customary to write a differential equation involving the temperature t, the quality x, the specific heats of water and steam c and h, and the heat of vaporization r; these three last properties are assumed to be functions of the temperature only.

The principal result of the application of the general method to such an equation is a formula for calculating the specific volume s, as will appear later. Following the general method, a special derivation of the formula for s will be given which may be preferred by some readers.

When a mixture of liquid and its vapor receives heat there is



vapor and in the portion r - x of liquid, and there is a vaporization of part of the liquid. Taking c for the specific heat of the liquid and h for the specific heat of the vapor, while r is the heat of vaporization, we shall have for an infinitesimal change,

NT C

$$dQ = hxdt + c (1 - x) dt + rdx$$
 . . . . (103)

Application of the First Law. — The first law of thermodynamics is applied to equation (103) by combining it with equation (16), so that

$$dQ = A(dE + pdv) = hxdt + c(1 - x)dt + rdx;$$

$$\therefore dE = \frac{1}{A}[hx + c(\tau - x)]dt + \frac{r}{A}dx - pdv.$$

Now v is a function of both t and x, as is evident from equation (101), in which u is a function of t; consequently,

$$dv = \frac{\delta v}{\delta t} dt + \frac{\delta v}{\delta x} dx.$$

$$\therefore dE = \left\{ \frac{1}{A} \left[ hx + c \left( 1 - x \right) \right] - p \frac{\delta v}{\delta \iota} \right\} d\iota + \left[ \frac{r}{A} - p \frac{\delta v}{\delta x} \right] dx.$$

But E being expressed in terms of t and x gives

$$\frac{\delta^2 E}{\delta t \, \delta x} = \frac{\delta^2 E}{\delta x \, \delta t},$$

so that 
$$\frac{\delta}{\delta x} \left\{ \frac{1}{A} [hx + c(1-x)] - p \frac{\delta v}{\delta t} \right\} = \frac{\delta}{\delta t} \left( \frac{r}{A} - p \frac{\delta v}{\delta x} \right)$$
.

Bearing in mind that all the functions but x and v are functions of t only, the differentiation gives

$$\frac{\mathrm{I}}{A}(h-c)-p\,\frac{\delta^2\,v}{\delta t\,\delta x}=\frac{\mathrm{I}}{A}\frac{dr}{dt}-\frac{dp}{dt}\frac{\delta v}{\delta x}-p\,\frac{\delta^2\,v}{\delta x\,\delta t}\;.$$



and

$$\frac{\delta^2 v}{\delta l \, \delta x} = \frac{\delta^2 v}{\delta x \, \delta l};$$

 $\frac{\delta v}{\delta x} = u,$ 

so that the above equation reduces to

$$\frac{dr}{dt} + c - h = Au \frac{dp}{dt} \cdot \cdot \cdot \cdot (104)$$

Application of the Second Law. - The second law of thermodynamics makes

$$\frac{dQ}{T} = d\phi$$

for a reversible process, so that the general equation (103) may be reduced to

$$\frac{dQ}{T} = \frac{hx + c(t - x)}{T} dt + \frac{r}{T} dx.$$

But

$$\frac{\delta^2 \phi}{\delta x \, \delta t} = \frac{\delta^2 \phi}{\delta t \, \delta x}.$$

$$\therefore \quad \frac{\delta}{\delta x} \frac{hx + c}{T} \frac{(1-x)}{T} = \frac{\delta}{\delta t} \frac{r}{T}.$$

$$\therefore \quad \frac{h-c}{T} = \frac{T\frac{dr}{dt}-r}{T^2}.$$

$$\therefore \frac{dr}{dt} + c - h = \frac{r}{T} \quad . \quad . \quad . \quad (105)$$

First and Second Laws Combined. - The combination of equations (104) and (105) gives

F10. 30.

Special Method. — The preceding equation may be obtained by a special method making use of the diagram abed in Fig. 30 which represents Carnot's cycle for a mixture of a liquid and its vapor, the change of temperature  $\Delta T$  being very small. a represent the volume of one pound of water at the temperature T, and b the volume of one pound of steam at the same temperature and pressure. The line ab

therefore represents the vaporization of one pound of water at constant temperature, involving the application of the heat of vaporization r, and the increase of volume

$$u = s - \sigma$$

where s and  $\sigma$  are the specific volumes of steam and water. the second law of thermodynamics the efficiency of this cycle will be

$$\frac{T - (T - \Delta T)}{T} \approx \frac{\Delta T}{T},$$

so that the heat changed into work will be

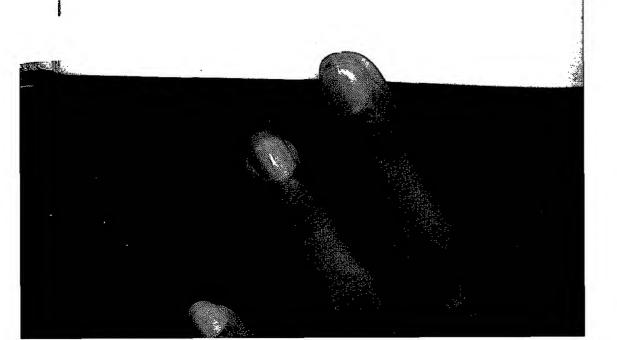
$$\frac{r\Delta T}{T}$$
.

But by the first law of thermodynamics this heat is equivalent to the external work, which in this case is approximately equal to the increase of volume u multiplied by the change of pressure  $\Delta p$ ; consequently,

$$\frac{r\Delta T}{AT}=u\Delta p,$$

or, at the limit as  $\Delta T$  approaches zero,

$$r = AuT \frac{dp}{dt}.$$



Specific Volume and Density. — The most important result of the application of the methods of thermodynamics to the properties of saturated vapor is expressed by equation (106), which gives a method of calculating the specific volume; thus,

$$s = u + \sigma = \frac{r}{AT} \frac{1}{\frac{dp}{dt}} + \sigma . . . . . (107)$$

The numerical value of  $\sigma$  for water for French units is 0.001, and for English units is  $\frac{1}{62.4} = 0.016$ , nearly. The density, or weight of a unit of volume, is of course the reciprocal of the specific volume.

It is of interest to consider the degree of accuracy that may be expected from this method of calculating the density of saturated The value of r depends on H and q, the total heat and the heat of the liquid; the latter is now well known, but the total heat is probably in doubt to the extent of sto and may be more. The absolute temperature T appears to be better known and may be subject to an error of no more than Tobo or 2000; and the mechanical equivalent of heat  $\frac{1}{A}$  is perhaps as well determined as the absolute temperature. The least satisfactory factor in the expression is the differential coefficient  $\frac{dp}{dt}$ , which is derived by differentiating one of the empirical equations on pages 78 and 79. It is true that the resulting equations on pages 79 and 80 afford a ready means of computing values of the coefficient with great apparent accuracy, but some idea of the essential vagueness of the method may be obtained by comparing computations of the specific volume of saturated steam at 212° C., a point for which either equation  $B_i$  or equation  $C_i$  will give the pressure as 14.6967 pounds per square inch. The specific volume by aid of equation (107), using equation  $B_1$  for determining the differential coefficient, is 26.62, while the differential coefficient from equation  $C_1$  gives 26.71; the discrepancy is about 360; or if the mean 26.66 be taken as the probable value, either computed value is subject to an error of voto.



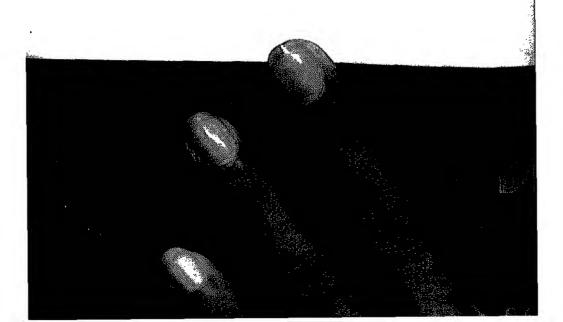
Experimental Determinations of Specific Volume. — By far the best direct determinations of the specific volumes of saturated steam are those reported by Knoblauch, Linde, and Klebe, as expressed by their characteristic equation for superheated steam given on page 110. These experiments determined the pressures for various temperatures at constant volume, and the results were so treated as to give the volume at saturation by exterpolation with great certainty. The following is a comparison of specific volume determined by them and volumes computed by equation (107).

SPECIFIC VOLUMES OF SATURATED STEAM.

By Knoblauch, Linde, and Klebe.

Temper-	Valume	Cu. M.			Cu. M.	Taguas	Voluma Co. M.		
	Experi- mental.	Com- puted.	Temper- ature.	Rxperi- mental.	Com- puted.	Temper- alure.	R's consi- preparat	Cum-	
100	1.674	1.665	130	0.6600	ი, რბიკ	Tộo	0.1071	લ. 1419	
105	T 420	1.412	135	0.5842	0.5747	105	0. 2740	0.1703	
110	t.211	1.212	140	0.5001	0.5011	170	0.1140	0.1411	
115	1.037	1.027	145	0.4466	0.4405	175	0.1170	0.1137	
120	0.8922	0.8826	150	0.3021	0.3880	175 180	0 1943	0.1934	
125	0.7707	0.7617	155	0.3470	0. 3428				

Nature of the Specific Heats. — In the application of the general thermodynamic method on page 88 the term h is introduced to represent the specific heat of saturated steam, and there is some interest in the determination of the true nature of this property, which clearly cannot be a specific heat at constant pressure, nor a specific heat at constant volume, since both pressure and volume change with the temperature. The specific heat of the liquid c properly is affected by the same consideration, but as the increase of volume is small and is neglected in thermodynamic discussions, the importance of the consideration is much less. The specific heat h of saturated vapor is the amount of heat necessary to raise the temperature of one pound of the vapor one degree, under the condition that the pressure shall



increase with the temperature, according to the law for saturated vapor.

Equation (105) gives a ready way of calculating the specific heat for a vapor, for from it

$$h = c + \frac{dr}{dt} - \frac{r}{T}$$

Now r may be readily expressed as a function of t, and then by differentiation  $\frac{dr}{dt}$  may be determined. For steam

$$r = H - q = 606.5 + 0.305 l - [q_1 + c (l - l_1)]$$

in which  $t_i$  is the temperature at the beginning of the range, as given by the table on page 80, within which t may fall. Therefore

$$\frac{dr}{dt} = 0.305 - c,$$

and

$$h = 0.305 - \frac{r}{T}.$$

For other vapors the equations, deduced from the empirical equations for q and H on pages  $8_3$  and  $8_5$ , are somewhat more complicated, but they involve no especial difficulty.

The following table gives the values of h for steam at several absolute pressures:

#### SPECIFIC HEAT OF STEAM.

Pressures, lbs. per sq. in., p 5	50	100	200	300
Temperatures, & F 162.3	280.9	327.6	381 <i>.7</i>	417.4
Specific heat, $h$ $-1.30$	-0.93	-0.82	-0.70	— a,63

The negative sign shows that heat must be abstracted from saturated steam when the temperature and pressure are increased, otherwise it will become superheated. On the other hand, steam, when it suddenly expands with a loss of temperature and pressure, suffers condensation, and the heat thus liberated supplies that required by the uncondensed portion.



a cylinder with glass sides, where then the clear saturated steam suffered partial condensation, as indicated by the formation of a cloud of mist. The reverse of this experiment showed that steam does not condense with sudden compression, as shown by Cash,

Ether has a positive value for h. As the theory indicates, a cloud is formed during sudden correpression, but not during sudden expansion.

The table of values of h for steam shows a notable decrease for higher temperatures, which inclicates a point of inversion at which h is zero and above which h is positive, but the temperature of that point cannot be determined from our experimental knowledge. For chloroform the point of inversion was calculated by Cazin † to be 123°.48, and determined experimentally by him to be between 125° and 120°. The discrepancy is mostly due to the imperfection of the apparatus used, which substituted finite changes of considerable magnitude for the indefinitely small changes required by the theory.

Isothermal Lines. — Since the pressure of saturated vapor is a function of the temperature only, the isothermal line of a mixture of a liquid and its vapor is a line of constant pressure, parallel to the axis of volumes. Steam expanding from the boiler into the cylinder of an engine follows such a line; that is, the steam-line of an automatic cut-off engine with ample ports is nearly parallel to the atmospheric line.

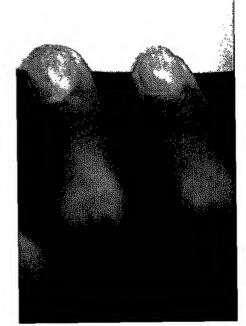
The heat required for an increase of volume at constant pressure is

in which r is the heat required to vaporize one pound of liquid, and  $x_1$  and  $x_2$  are the initial and final qualities, so that  $x_2 - x_1$  is the weight of liquid vaporized.

The external work done during an isothermal expansion is

$$W = p (v_2 - v_1) = pu (x_1 - x_1) \dots (109)$$

\* Bulletin de la Société Ind. de Mulhouse, exxxil. † Comptes rondus de l'Acadêmie des Sciences, ixil.



Intrinsic Energy. — Of the heat required to raise a pound of any liquid from freezing-point to a given temperature and to completely vaporize it at that temperature, a part q is required to increase the temperature, another part  $\rho$  is required to change the state or do disgregation work, and a third part A pu is required to do the external work of vaporization. Consequently for complete vaporization we may have,

$$Q = \Lambda (S + I + W) = q + \rho + A \rho u = H.$$

For partial vaporization the heat required to do the disgregation work will be xp, and the heat required to do the external work will be Apxu. Therefore the heat required to raise a pound of a liquid from freezing-point to a given temperature and to vaporize x part of it will be

$$Q = q + xp + Apxu = A(E + W)$$

where E is the increase of intrinsic energy from freezing-point. It is customary to consider that

$$E = \frac{1}{A}(x\rho + q) \quad . \quad . \quad . \quad . \quad (110)$$

represents the intrinsic energy of one unit of weight of a mixture of a liquid and its vapor.

Isoenergic or Isodynamic Lines. — If a change of a mixture of a liquid and its vapor takes place at constant intrinsic energy, the value of E will be the same at the initial and final conditions, and

$$q_2 - q_1 + x_2 \rho_2 - x_1 \rho_1 = 0$$
 . . . (111)

which equation, with the formulæ

$$v_2 = x_2 u_2 + \sigma$$
;  $v_1 = x_1 u_1 + \sigma$ . . . (112)

enable us to compute the initial and final volumes. If desired, intermediate volume corresponding to intermediate temperature can be computed in the same way, and a curve can be drawn in the usual way with pressures and volumes for the coordinates.

For example, if a mixture of 10 steam and 10 water expands

isoenergically from 100 pounds absolute to 13 pounds absolute, the final condition will be

$$x_2 = \frac{q_1 - q_2 + x_1 \rho_1}{\rho_2} = \frac{207.9 - 181.8 + 0.9 - 803.8}{893.0} = 0.9395,$$

The initial and final specific volumes are

$$v_1 = x_1 u_1 + \sigma = 0.9 (4.403 - 0.016) + 0.016 - 3.964;$$
  
 $v_2 = x_2 u_2 + \sigma = 0.9395 (46.15 - 0.016) + 0.016 = 14.54.$ 

The converse problem requiring the pressure corresponding to a given volume cannot be solved directly. The only method of solving such a problem is to assume a probable final pressure and find the corresponding volume; then, if necessary, assume a new final pressure larger or smaller as may be required, and solve for the volume again; and so on until the desired degree of accuracy is obtained.

This method does not give an explicit equation connecting the pressures and volumes, but it will be found on trial that a curve, drawn by the process given above can be represented fairly well by an exponential equation, for which the exponent can be determined by the method on page 66.

Having given or determined the initial and final volumes, the exponential equation may be determined, and then the external work may be calculated by the equation

$$W = \int p dv = \frac{p_1 v_1}{n-1} \left\{ 1 - \left(\frac{v_1}{v_2}\right)^{n-1} \right\}$$

For example, the exponent for the equation representing the expansion of the above problem is

$$n = \frac{\log p_1 - \log p_2}{\log v_2 - \log v_1} = \frac{\log 100 - \log 15}{\log 24.54 - \log 3.964} = 1.041,$$

and the external work of expansion is

$$W = \frac{100 \times 144 \times 3.964}{1.041 - 1} \left\{ 1 - \left( \frac{3.964}{24.54} \right)^{0.041} \right\} = 100,000 \text{ ft.-lbs.}$$

Since there is no change in the intrinsic energy during an isoenergic expansion, the external work is equivalent to the heat applied. Thus in the example just solved the heat applied is equal to

$$100,000 \div 778 = 120$$
 B.T.U.

There is little occasion for the use of the method just given, which is fortunate, as it is not convenient.

Entropy of the Liquid. — Suppose that a unit of weight of a liquid is intimately mingled with its vapor, so that its temperature is always the same as that of the vapor; then if the pressure of the vapor is increased the liquid will be heated, and if the vapor expands the liquid will be cooled. So far as the unit of weight of the liquid under consideration is concerned, the processes are reversible, for it will always be at the temperature of the substance from which it receives or to which it imparts heat, i.e., it is always at the temperature of its vapor.

The change of entropy of the liquid can therefore be calculated by equation (37),

$$d\phi = \frac{dQ}{T},$$

which may here be written

$$\theta = \int \frac{dq}{T} = \int \frac{cdt}{T} \quad . \quad . \quad . \quad . \quad (113)$$

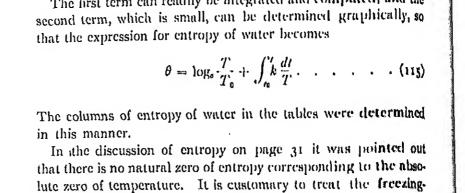
On page 83 it is suggested that the specific heat of water for temperature Centigrade may be expressed as follows:

$$c = i + k$$

where k is a small corrective term that may be positive or negative as the case may be. Using this correction, equation (113) may be written

$$\theta = \int \frac{dl}{T} + \int \frac{kdl}{T} . . . . . . . (114)$$





point of water as the zero of entropy both for that liquid and for other volatile liquids; some liquids therefore have negative entropies at temperatures below freezing-point of water in the

For a liquid like ether which has the heat of the liquid repre-

 $q = 0.52001 t + 0.0002050 t^3$ 

c = 0.52901 + 0.0005918 l.

Then the increase of entropy above that for the freezing-point of water may be obtained by aid of equation (113), which gives for

 $\theta = \int_{273}^{T} \left\{ 0.52901 + 0.0005918 \left( T - 273 \right) \right\} \frac{dt}{T};$ 

 $\therefore \ \theta = 0.0005918 \, l + 0.3670 \, \log_{\theta} \frac{T}{273} \quad . \quad . \quad . \quad . \quad (116)$ 

the specific heat is first obtained by differentiation, giving

 $\therefore \ \theta = \int_{273}^{T} \left( 0.3670 \, \frac{dt}{T} + 0.0005918 \, dt \right);$ 

 $\therefore \theta = 0.0005918 \ (T - 273) + 0.3670 \log_{\theta} \frac{T}{273};$ 

appropriate tables of their properties.

ether with the French system of units,

sented by an empirical equation,

For temperatures below the freezing-point of water, equation (116) gives negative numerical results.

Other liquids for which equations for the heat of the liquid are given on page 83, may be treated in a similar method.

Entropy due to Vaporization. — When a unit of weight of a liquid is vaporized r thermal units, equal to the heat of vaporization, must be applied at constant temperature. Treating such a vaporization as a reversible process, the change of entropy may be calculated by the equation

$$\phi - \phi_0 = \frac{r}{T}$$

This property is given in the "Tables for Saturated Steam," but not in general for other liquids.

Market State Company of the Company

Entropy of a Mixture of a Liquid and its Vapor. — The increase in entropy due to heating a unit of weight of a liquid from freezing-point to the temperature t and then vaporizing x portion of it is

$$\theta + \frac{\alpha r}{T}$$
,

where  $\theta$  is the entropy of the liquid, r is the heat of vaporization, and T is the absolute temperature. For steam  $\frac{r}{T}$  may be taken from the tables; for other vapors it must usually be calculated.

For any other state determined by  $x_1$  and  $t_1$  we shall have, for the increase of entropy above that of liquid at freezing-point,

$$\frac{x_1r_1}{T_1}+\theta_1.$$

The change of entropy in passing from one state to another is

$$\phi - \phi_1 = \frac{xr}{T} + \theta - \frac{x_1r_1}{T_1} - \theta_1 \quad . \quad . \quad (117)$$

When the condition of the mixture of a liquid and its vapor is given by the pressure and value of x, then a table giving the properties at each *pound* may be conveniently used for this work.

gives

$$\frac{N_1 r_1}{T_1} + \theta_1 = \frac{N_2 r_2}{T_2} + \theta_2 + \cdots + (118)$$

When the initial state, determined by  $x_1$  and  $t_1$  or  $p_2$  is known and the final temperature  $t_2$ , or the final pressure  $p_2$  the final value  $x_2$  may be found by equation (118). The initial and final volumes may be calculated by the equations

Tables of the properties of saturated values commonly give the specific volume  $s_i$  but

5 m H + 0.

The value of  $\sigma$  for water is 0.016, and for other liquids will be found on page 85.

For example, one pound of dry steam at 100 pounds absolute pressure will have the values

If the final pressure is 15 pounds absolute, we have

whence

$$\frac{884.0}{788.3} + 0.4733 = \frac{005.1x}{673.7} + 0.3143i$$

$$\therefore x_2 = 0.894.$$

The initial and final volumes are

$$v_1 = s_1 = 4.40$$
  
 $v_2 = x_3 u_2 + \sigma = 23.4$ 

Problems in which the initial condition and the final temperature or pressure are given may be solved directly by aid of the preceding equations. Those giving the final volume instead



mations. An equation to an adiabatic curve in terms of p and v cannot be given, but such a curve for any particular case may be constructed point by point.

Clausius and Rankine independently and at about the same time deduced equations identical with equations (117) and (118), but by methods each of which differed from that given here.

Rankine called the function

$$\theta + \frac{xr}{T}$$

the thermodynamic function; Clausius called it entropy.

In the discussion of the specific heat h of a saturated vapor, it appeared that the expansion of dry saturated steam in a non-conducting cylinder would be accompanied by partial condensation. The same fact may be brought out more clearly by the above problem.

On the other hand, h is positive for ether, and partial condensation takes place during compression in a non-conducting cylinder.

For example, let the initial condition for ether be

$$l_1 = 10^{\circ} \,\mathrm{C}_{\cdot, 1}$$
,  $r_1 = 93.12$ ,  $\theta = 0.0191$ ,  $x_1 = 1$ ,

and let the final conditions be

$$l_2 = 120^{\circ} \text{ C.}, \quad r_2 = 72.26, \quad \theta_2 = 0.2045;$$

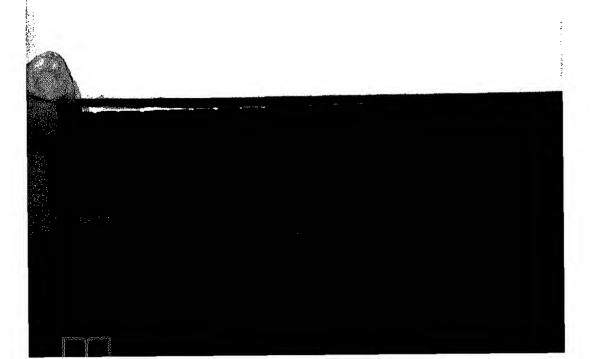
$$\frac{93.12}{283} + 0.0191 = \frac{72.26x_2}{393} + 0.2045,$$

and

then

Equation (118) applies to all possible mixtures of a liquid and its vapor, including the case of  $x_1 = 0$  or the case of liquid without vapor, but at the pressure corresponding to the temperature according to the law of saturated vapor. When applied to hot water, this equation shows that an expansion in a non-conducting cylinder is accompanied by a partial vaporization.

A. = 0.724



There is some initial state of the mixture such that the value of x shall be the same at the beginning and at the end, though x may vary at intermediate states. To find that value make  $x_1 = x_2$  in equation (118) and solve for  $x_1$ , which gives

$$x_1 = \frac{\theta_1 \dots \theta_2}{r_2 \dots r_1}$$

$$T_2 \dots T_1$$

The value of  $w_i$  for steam to fulfil the conditions given varies with the initial and final temperatures chosen, but in any case it will not be much different from one half. It may therefore be generally stated that a mixture of steam and water, when expanded in a non-conducting cylinder, will show partial condensation if more than half is steam, and partial evaporation if more than half water. If the mixture is nearly half water and half steam, the change must be investigated to determine whether evaporation or condensation will occur; but in any case the action will be small.

External Work during Adiabatic Expansion. — Since no heat is transmitted during an adiabatic expansion, all of the intrinsic energy lost is changed into external work, so that, by equation (110),

$$W = E_1 - E_2 = \frac{1}{A} (q_1 - q_2 + x_1 \rho_1 - x_2 \rho_2) . . . (130)$$

For example, the external work of one pound of dry steam is expanding adiabatically from 100 pounds to 15 pounds absolute is

$$W = 778 (297.9 - 181.8 + 1 \times 802.8 - 0.894 \times 892.6)$$
  
 $W = 120.2 \times 778 = 93.500 \text{ foot-pounds.}$ 

Attention should be called to the unavoidable defect of this method of calculation of external work during adiabatic expansion, in that it depends on taking the difference of quantities which are of the same order of magnitude. For example, the above calculation appears to give four places of significant figures.

while, as a matter of fact, the total heat H from which  $\rho$  is derived is affected by a probable error of  $\frac{1}{500}$  or perhaps more. Both the quantities

$$q_1 + x_1 \rho_1$$
 and  $q_2 + x_2 \rho_2$ 

have a numerical value somewhere near 1000, and an error of  $\frac{1}{500}$  is nearly equivalent to two thermal units, so that the probable error of the above calculation is nearly two per cent. For a wider range of temperature the error is less, and for a narrower range it is of course larger. This matter should be borne in mind in considering the use of approximate methods of calculations; for example, the temperature-entropy diagram to be discussed later.

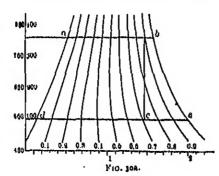
The adiabatic curve cannot be well represented by an exponential equation; for if an exponent be determined for such a curve passing through points representing the initial and final states, it will be found that the exponent will vary widely with different ranges of pressure, and still more with different initial values of x; and that, further, the intermediate points will not be well represented by such an exponential curve even though it passes through the initial and final points.

This fact was first pointed out by Zeuner, who found that the most important element in determining n was  $x_1$ , the initial condition of the mixture. He gives the following empirical formula for determining n, which gives a fair approximation for ordinary ranges of temperature:

There does not appear to be any good reason for using an exponential equation in this connection, for all problems can be solved by the method given, and the action of a lagged steamengine cylinder is far from being adiabatic. An adiabatic line drawn on an indicator-diagram is instructive, since it shows to the eye the difference between the expansion in an actual engine and that of an ideal non-conducting cylinder; but it can

general purposes the hyperbola is the best curve for comparison with the expansion curve of an indicator diagram, for the reason that it is the conventional curve, and is near enough to the curve of the diagrams from good engines to allow a practical engineer to guess at the probable behavior of an engine, from the diagram alone. It cannot in any sense be considered as the theoretical curve.

Temperature-Entropy Diagram.—If the entropies of the liquid and the entropies of vaporization for steam are plotted with temperature for ordinates we get a diagram like 30a; very com-



morely absolute temperatures are taken in drawing the diagram in order to emphasize the rôle played by absolute temperatures in the determination of the efficiency of Carnot's cycle. It would seem better to take the temperature by the centigrade or the Fahrenheit thermometer, as they are the basis of steam-tables,

and the temperature-entropy diagram is the equivalent of such a table.

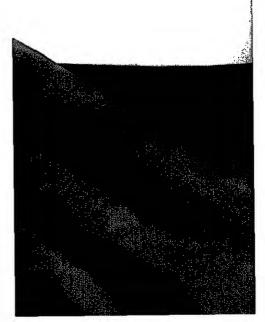
Now the entropy of a mixture containing x part steam is

$$\theta + x \frac{r}{T}$$
;

so that the entropy of a mixture containing x part of steam can be determined by dividing the line such as do (which represents the entropy of vaporization) in the proper ratio.

$$\frac{dc}{ds} = \infty$$

It is convenient to divide the several lines like ab and do into tenths and hundredths, and then, if an adiabatic expansion is



represented by a vertical line like bc, the entropy at c may be determined by inspection of the diagram. Conversely, by noting the temperature at which a given line of constant entropy crosses a line of given quality we may determine the temperature to which it is necessary to expand to attain that quality, a determination which cannot be made directly by the equation.

When a temperature-entropy diagram is used as a substitute for a "Table of the Properties of Saturated Steam," it is customary to draw the lines of constant quality or dryness factor, and other lines like constant volume lines and lines of constant heat contents or values of the expression

$$xr + q$$

the use of which will appear in the discussion of steam-engines and steam-turbines.

To get a series of constant volume lines we may compute the volume for each quality  $x_1 = .1$ ,  $x_2 = .2$ , x = .3, etc., by the equation

and since the volume increases proportionally to the increase in  $\alpha$ , we may readily determine the points on that line for which the volume shall be whole units, such as 2 cubic feet, 3 cubic feet, etc. Points for which the volumes are equal may now be connected by fair curves, so that for any temperature and entropy the volume may readily be estimated.

Curves of equal heat contents can be constructed in a similar way.

各种的人的,我们就是我们的人的人,我们就是一个人的人的人,我们就是一个人的人的人的人,也不是一个人的人的人,也不是一个人的人的人,也是一个人的人的人,也是一个人的人的人的人,也是一个人的人的人,也是一

If desired, a curve of temperatures and pressures can be drawn so that many problems can be solved approximately by aid of the compound diagram.

At the back of this book a temperature-entropy diagram will be found which gives the properties of saturated and superheated steam. It is provided with a scale of temperatures at either side, and a scale of entropies at the bottom, while there is a scale of pressure at the right.

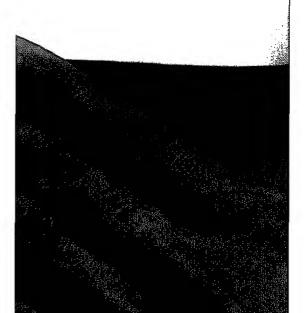


To solve a problem like that on page 100, i.e., to find the quality after an adiabatic expansion from 100 pounds absolute to 16 pounds absolute, and the specific volume at the initial and final states, proceed as follows:

From the curve of temperatures and pressures, select the temperature line which corresponds to 100 pounds and note where it cuts the saturation curve, because it is a saumed that the steam is initially dry. The diagram gives the entropy as approximately 1.61. Note the temperature line which cuts the temperature pressure curve at 15 pounds, and estimate the value of & from its intersection with the entropy line 1.61; by this method the value of x is found to be about 0.89. In like manner the volume may be estimated to be about 23.4 cubic feet.

Temperature-Entropy Table. - Now that the computation of isoentropic changes has ceased to be the diversion of students of theoretical investigations and has become the necessity of engineers who are engaged in such matters as the design of steam-turbines, the somewhat inconvenient methods which were incapable of inverse solutions, have become somewhat burdensome. A remedy has been sought in the use of temperature entropy diagrams just described. Such a diagram to be really useful in practice must be drawn on so large a scale as to be very inconvenient, and even then is liable to lack accuracy. this condition of affairs a temperature-entropy table has been computed and added to the "Tables of the Properties of Saturated Steam." In this table each degree Fahrenhelt from 180° to 430° is entered together with the corresponding pressure. There have been computed and entered in the proper columns the following quantities, namely, quality x, heat contents xr + q, and specific volume v, for each hundredth of a unit of entropy.

In the use of this table it is recommended to take the nearest degree of temperature corresponding to the absolute pressure if pressures are given. Following the line across the table select that column of entropy which corresponds most nearly with the initial condition; the corresponding initial volume may be read directly. Follow down the entropy column to the lower temper-



ature and then find the value of x and the specific volume. The external work for adiabatic expansion may now readily be found by aid of equation (120), page 102. As will appear later, the problems that arise in practice usually require the heat contents and not the intrinsic energy, so that property has been chosen in making up the table.

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For example, the nearest temperature to 100 pounds per square inch is 328° F.; the entropy column 1.59 gives for x, 0.995, which indicates half of one per cent of moisture in the steam. The corresponding volume is 4.39 cubic feet. The nearest temperature to 15 pounds absolute is 213° F., and at 1.59 entropy the quality is 0.888 and the specific volume corresponding is 23.2 cubic feet.

If greater accuracy is desired we must resort to interpolation. Usually it will be sufficient to interpolate between the lines for temperature in a given column of entropy, because the quantity that must be determined accurately is usually the difference

$$x_1r_1 + q_1 - (x_2r_2 + q_2)$$

and this difference for two given temperatures  $t_1$  and  $t_2$  is very nearly the same if taken out of two adjacent entropy columns. A similar result will be found for the difference

$$x_1\rho_1 + q_1 - (x_2\rho_2 + q_2),$$

if computed for values of a found in adjacent columns.

Another way of looking at this matter is that one hundredth of a unit of entropy at 330 pounds corresponds to one per cent of moisture.

Evidently this table can be used to solve problems in which the final volumes are given, or, as will appear later, to determine intermediate pressures for steam-turbines.



#### EXAMPLES.

- 1. Water at 100° F. is fed to a boiler in which the pressure is 120 pounds absolute per square inch. How much heat must be supplied to evaporate each pound? Ans. 1118 a.r.v.
- v2. One pound wet steam at 130 pounds absolute occupies 45 cubic feet. What per cent of moisture is present? What is the "quality" of the steam? Ans. 17.1 per cent of moisture # \*\*
  .820.
- 6.6 steam. What is the increase of entropy above that of water at 32° F.? Ans. 1.144.
- 4. A kilogram of chloroform at 100° C, is 60 % vapor. What ke the increase of entropy above that of the biquid at 6° C.? Ans. 0.1959.
- 5. The initial condition of a mixture of water and steam is  $I = 320^{\circ} \text{ F.}$ , v = 0.8. What is the final condition after adiabate expansion to  $212^{\circ} \text{ F.} ?$  Ans. 0.74.
- 7 6. The initial condition of a mixture of steam and water is per 3000 mm., x = 0.0. Find the condition after an adiabatic expansion to 600 mm. Ans. 0.838.
- 7. A cubic foot of a mixture of water and steam, x = 0.8 is under the pressure of 60 pounds by the gauge. Find its volume after it expands adiabatically till the pressure is reduced to 60 pounds by the gauge; also the external work of expansion. Ans. 2.68 cubic feet and 9980 foot pounds.
- 8. Three pounds of a mixture of steam and water at me pounds absolute pressure occupy 4.5 cubic feet. How much heat must be added to double the volume at the same pressure and what is the change of intrinsic energy? Ans. 1065 1-104 750,400 foot pounds.
- 9. Find the intrinsic energy, heat contents and volume of 5 pounds of a mixture of water and steam which is 80 per cut steam, the pressure being 150 pounds atsociate. Ans. Intrinsic energy, 3,710,000; heat contents, 5095 n.r.c.; volume, 12.1 cubic feet.

10. Three pounds of water are heated from 60° F. and evaporated under 135.3 pounds gauge pressure. Find the heat added, and the changes in volume, and intrinsic energy. Ans. Heat added, 3490 B.T.U.; increase in volume, 8.99 cubic feet; intrinsic energy, 2,520,000.

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cent inste zuble 11. A pound of steam at 337°.7°F. and 100 pounds gauge pressure occupies 3 cubic feet. Find its intrinsic energy and its entropy above 32°F. Ans. Intrinsic energy, 718,000; entropy, 1.336.

12. Two pipes deliver water into a third. One supplies 300 gallons per minute at 70° F.; the other, 90 gallons per minute at 200° F. What is the temperature of the water after the two streams unite? Ans. 100° F.

13. A test of an engine with the cut-off at 0.106 of the stroke, and the release at 0.98 of the stroke, and with 4.5 per cent clearance, gave for the pressure at cut-off 62.2 pounds by the indicator, and at release 6.2 pounds; the mixture in the cylinder at cut-off was 0.465 steam, and at release 0.921 steam. Find (1) condition of the mixture in the cylinder at release on the assumption of adiabatic expansion to release; (2) condition of mixture on the assumption of hyperbolic expansion, or that  $pv = p_1v_1$ ; (3) the exponent of an exponential curve passing through points of cutoff and release; (4) exponent of a curve passing through the initial and final points on the assumption of adiabatic expansion; (5) the piston displacement was 0.7 cubic feet, find the external work under exponential curve passing through the points of cut-off and release; also under the adiabatic curve. Ans. (1) 0.472; (2) 0.524; (3) n = 0.6802; (4) n = 1.0589; (5) 3093 and 2120 footpounds.

# CHAPTER VII.

# SUPERHEATED VAPORS.

A DRY and saturated vapor, not in contact with the liquid from which it is formed, may be heated to a temperature greater than that corresponding to the given pressure for the same vapor when saturated; such a vapor is said to be superheated. When far removed from the temperature of saturation, such a vapor follows the laws of perfect gases very nearly, but near the temperature of saturation the departure from those laws is too great to allow of calculations by them for engineering purposes.

All the characteristic equations that have been proposed, have been derived from the equation

$$pv = RT$$
,

which is very nearly true for the so-called perfect gases at moderate temperatures and pressures; it is, however, well known that the equation does not give satisfactory results at very high pressures or very low temperatures. To adapt this equation to represent superheated steam, a corrective term is added to the right-hand side, which may most conveniently be assumed to be a function of the temperature and pressure, so that calculations by it may be made to join on to those for saturated steam.

The most satisfactory characteristic equation of this sort in that given by Knoblauch,\* Linde, and Klebe,

$$pv = BT - p (1 + ap) \left[ C \left( \frac{373}{T} \right)^3 - D \right] \quad . \quad (121)$$

in it the pressure is in kilograms per square metro,  $\boldsymbol{v}$  is in cubic metres, and T is the absolute temperature by the

\* Mitteilungen über Forschungsarbeiten, etc., Heft 21, S. 33, 1905.

centigrade thermometer. The constants have the following values:

$$B = 47.10$$
,  $a = 0.000002$ ,  $C = 0.031$ ,  $D = 0.0052$ .

In the English system of units, the pressures being in pounds per square foot, the volumes in cubic feet per pound, and the temperatures on the Fahrenheit scale, we have

$$pv = 85.85 T - p(1 - 1-0.00000976 p) \left(\frac{150,300,000}{T^{3}} - 0.0833\right)$$
 (122)

The following equation may be used with the pressure in pounds per square inch:

$$pv = 0.5962 \ T - p (1 + 0.001.1 \ p) \left( \frac{150,300,000}{T^3} - 0.0833 \right) \ . \ (123)$$

The labor of calculation is principally in reducing the corrective term, and especially in the computation of the factor containing the temperature. A table on page 112 gives values of this factor for each five degrees from 100° to 600° F.; the maximum error in the calculation of volume by aid of the table is about 0.4 of one per cent at 336 pounds pressure and 428° F.; that is at the upper limit of our table for saturated steam. At 150 pounds and 358° F., which is about the middle range of our table for saturated steam, the error is not more than 0.2 of one per cent, which is not greater than the probable error of the equation itself under those conditions. At lower pressures and at higher temperatures the error tends to diminish.

The following simple equation is proposed by Tumlirz\*

where p is the pressure in kilograms per square metre, v the specific volume in cubic metres, and T the absolute temperature centigrade. The constants have the values

$$B = 47.70$$
  $C = 0.016$ 

based on the experiments of Knoblauch, Linde, and Klebe.

\* Math. Naturw. Kl. Wlen., 1899, Iln S. 1058.

In the English system with the pressure in pounds per square foot and the volumes in cubic feet, for absolute temperatures Fahrenheit,

 $pv = 85.85 \ T - 0.256 \ p \ . \ . \ . \ . \ (125)$ 

This equation has a maximum error of 0.8 of one per cent as compared with equation (121).

TABLE I.  $Values of the factor \frac{150,300,000}{T^3} \rightarrow 0.0833.$ 

"l'emperature.		Value	Tomporature,		Value	Tamparatura.		Value	Tem	Vebue	
Fahr.	Abs.	Pactor.	Fahr.	Abs.	Factor.	Fahr.	Abs.	factor.	Fahr.	Abe.	Pagast.
200 205 210 215	659.5 664.5 669.5 674.5	0.429	310	759.5 764.5 769.5 774.5	0.260 0.253 0.247 0.240	201 011	859.5 861.5 869.5 874.5	0.149	505 510	959.5 964.5 969.5	0.081
225 230 235	679.5 684.5 689.5 694.5	0.395 0.385 0.375	325 330	779 · 5 784 · 5 789 · 5 794 · 5	0.234	420	870.5 884.5 880.5	0.138 0.134 0.131	515 516 515 536 535	974.5 979.5 984.5 989.5	
240 245 250 255	699.5 704.5 709.5 714.5	0.356	340 345 350 355	799.5 804.5 809.5 814.5	0.211 0.205 0.200 0.105	445 445 450 455	899.5 904.5 904.5 914.5	0.123 0.120 0.117 0.113	540 545 550	999.5 1004.5 1009.5	0.661
260 265 270 275	719.5 724.5 729.5 734.5	0.301	365 365 370 375	819.5 824.5 829.5 834.5		465 465 479 475	019.5 024.5 023.5 034.5	0.101	500 505 570 575	1010.8	0.059
280 585 200 205	739 · 5 744 · 5 749 · 5 754 · 5	0.288	380 385 300 305	839.5 844.5 849.5 854.5	0.171 0.166 0.162 0.158	480 485 490 495	039.5 944.5 949.5 954.5	0.008 0.005 0.000	580 585 590 595	1044.5	0.047

Specific Heat. — Two investigations have been made of the specific heat of superheated steam at constant pressure, one by Professor Knoblauch\* and Dr. Jakob and the other by Professor Thomas and Mr. Short; † the results of the latter's investigation have been communicated for use in this book in anticipation of the publication of the completed report.

<sup>\*</sup> Mittellungen über Porschungsarbeiten, Helt 36, p. 100.

<sup>†</sup> Thosis by Mr. Short, Cornell University

Professor Knoblauch's report gives the results of the investigations made under his direction in the form of a table giving specific heats at various temperatures and pressures and in a diagram, which can be found in the original memoir, and he also gives a table of mean specific heats from the temperature of saturation to various temperatures at several pressures. This latter table is given here in both the metric system and in the English system of units.

SPECIFIC HEAT OF SUPERHEATED STEAM.

Knoblauch and Jakob

/ Kg per	r Sq Cm	1	2	4	6	8	10	12	14	16	18	20
A Lba per Sq In.		14.2	28.4	56.0	85.3	113.8	142.2	170.6	199.1	227.5	156.0	284.4
fe Cont.		990	1200	1430	1580	1600	1700	1870	1940	2000	2000	2110
7. Fahr.		2100	2480	2800	3160	3360	350°	3680	38.0	302°		4120
Fahr. [	Cont.								]			<del></del>
3130		0.463							١	l	l l	
3020	1500	0.461	0.478	0.515								
3020	300a	0.462	0.475	0.502	0.530	0.560	0.597	0.635	0.677			
482°	2500	0.403	0.474	0.495	0.514	0. 532	0.552	0.570	0.588	0.600	0.635	0.664
572°	3000	0.404	0.475	0.402	0.505	0.517	0.530	0.541	0.550	0.561	0.572	0.585
6630	350"	0.408	0.477	0.402	0.503	0.512	0.522	0.520	0.516	0.543	0.550	0.557
752°	400°	0.473	0.481	0.494	0.504	0.512	C. 520	0.526	0.531	0.537	0.542	0.547

The construction of this table is readily understood from the following example: — Required the heat needed to superheat a kilogram of steam at 4 kilograms per square centimetre from saturation to 300° C. The saturation temperature (to the nearest degree) is 143° C.; so that the steam at 300° is superheated 157°, and for this is required the heat

## 157 × 0.492 = 77.2 calories.

The experiments of Professor Knoblauch were made at 2, 4, 6, and 8 kilograms per square centimetre; the remainder of the table was obtained from the diagram which was extended by aid of cross-curves to the extent indicated. Within the limits of the experimental work the table may be used with confidence. Exterpolated results are probably less reliable than those obtained directly by Professor Thomas.

The following table gives the mean specific heat of superheated steam as measured on a facsimile of Professor Thomas's original diagram without exterpolation.

# SPECIFIC HEAT OF SUPERHEATED STEAM

Thomas and Short.

Degrees of	Pressure Lbs. per Sq. In. (Absolute.)									
Superheat Fahr.	6	15	80	50	100	200	400			
20°	0.536	0.547	0.558	0.571	0.503	0.621	0.619			
50°	0.522	0.532	0.542	0.555	0.575	0.000	0.621			
1000	0.503	0.512	0.534	0.537	0.557	0.581	0.599			
150°	0.486	0.496	0.508	0.522	0.544	0.567	0.585			
200 <sup>0</sup>	0.471	0.480	0.494	0.500	0.533	0.550	0.574			
250°	0.456	0.466	0.481	0.496	0.522	0.546	0.564			
300°	0.442	0.453	0.468	0.484	0.511	0.537	0.554			

Here again the arrangement of the table can be made evident by an example: — Required the heat needed to superheat steam 100 degrees at 200 pounds per square inch absolute. The mean specific heat from saturation is 0.581, so that the heat required is 58.1 thermal units.

Total Heat. — In the solution of problems that arise in engineering it is convenient to use the total amount of heat required to raise one pound of water from freezing-point to the temperature of saturated steam at the given pressure and to vaporize it and to superheat it at that pressure to the given temperature. This total heat may be represented by the expression

$$II_{Sup.} = q + r + c_p \left( l - l_a \right)$$

where t is the superheated temperature of the superheated steam,  $t_s$  is the temperature of saturated steam at the given pressure p, and q and r are the corresponding heat of the liquid and heat of vaporization. The mean specific heat  $c_p$ , may usually be selected from one of the given tables without inter-

polation, as a small variation does not have a very large effect.

The total heat or heat contents of superheated steam in the temperature-entropy table were obtained by the following method. From Professor Thomas's diagram giving mean specific heats, curves of specific heats at various temperatures and at a given pressure were obtained, and the curves thus obtained were faired after a comparison with curves constructed with Professor Knoblauch's specific heats at those temperatures. These curves were then integrated graphically and the results checked by comparison with his mean specific heats.

Entropy. — By the entropy of superheated steam is meant the increase of entropy due to heating water from freezing-point to the temperature of saturated steam at the given pressure, to the vaporization and to the superheating at that pressure. This operation may be represented as follows:

$$\theta + \frac{r}{T_{\bullet}} + \int_{T_{\bullet}}^{T} \frac{c_{p}dl}{T}$$

in which T is the absolute temperature of the superheated steam, and  $T_{\bullet}$  is the temperature of the saturated steam at the given pressure;  $\theta$  and  $\frac{\tau}{T_{\bullet}}$  may be taken from the "Tables of Saturated Steam." The last term was obtained for the temperature-entropy table by graphical integration of curves plotted with values of  $\frac{c_p}{T}$  derived from the curves of specific heats at various temperatures just described under the previous section.

If the temperature-entropy table is not at hand, the last term of the above expression may be obtained approximately by dividing the heat of superheating, by the mean absolute temperature of superheating.

This may be expressed as follows:

$$\frac{c_p (t - t_s)}{\frac{1}{2} (t + t_s) + 459.5}$$

where t is the temperature of the superheated steam,  $t_i$  is the temperature of saturated steam at the given pressure, and  $c_p$  is the mean specific heat of superheated steam.

If this method is considered to be too crude, the computation can be broken into two or more parts. Thus if  $t_i$  is an intermediate temperature, the increase of entropy due to superheating may be computed as follows:

$$\frac{c_{p'}(l_1-l_2)}{\frac{1}{2}(l_1+l_2)+459.5}+\frac{c_{p''}(l-l_2)-c_{p'}(l_1-l_2)}{\frac{1}{2}(l+l_1)+459.5}$$

where  $c_{p}'$  is the mean specific heat between  $l_{s}$  and  $l_{t}$ , and  $c_{p}''$  is the specific heat between  $l_{s}$  and  $l_{t}$ . This method may evidently be extended to take in two intermediate temperatures and give three terms.

Adiabatic Expansion. — The treatment of superheated steam in this chapter resembles that for saturated steam in that it does not yield an explicit equation for the adiabatic line. If the steam were strongly superheated during the whole operation it is probable that the adiabatic line would be well represented by an exponential equation, and for such case a mean value of the exponent could be determined that would suffice for engineering work. But even with strongly superheated steam at the initial condition the final condition is likely to show moisture in the steam after adiabatic expansion, or, for that matter, after expansion of the steam in the cylinder of an engine or in a steam-turbine.

Problems involving adiabatic expansion of steam which is initially superheated can be solved by an extension of the method for saturated steam, and this method applies with equal facility to problems in which the steam becomes moist during the expansion. The most ready method of solution is by aid of the temperature-entropy table, which may be entered at the proper pressure (or the corresponding temperature of saturated steam) and the proper superheated temperature, it being in practice sufficient to take the line for the nearest tabular pressure and the column

powing the nearest degree of superheating. Following down e column for entropy to the final pressure, the properties for e final condition will be found; these will be the heat connts, specific volume, and either the temperature of superheated eam or the quality a, depending on whether the steam remains perheated during the expansion or becomes moist.

If the external work of adiabatic expansion of steam initially perheated is desired, it can be had by taking the difference of e intrinsic energies. The heat equivalent of intrinsic energy moist steam is

$$xp + q = x (r - Apu) + q = xr + q - Apxu,$$

d of this expression the quantity ar + q may be taken from e temperature-entropy table, and the quantity Ap.v.a can determined by aid of the steam table. In like manner the at contents of superheated steam

$$q+r+\int c_{\mu}dt$$

nich is computed and set down in the temperature-entropy ble may be made to yield the heat equivalent of the intrinsic ergy by subtracting the heat equivalent of the external work vaporizing and superheating the steam

$$A p (v - \sigma),$$

here v is the specific volume of the superheated steam. thod is subject to some criticism, especially when the steam not highly superheated, because some heat will be required do the disgregation work of superheating. Fortunately the eater part of problems arising in engineering involve the heat ntents, so that this question is a voided,

Proportion of Sulphur Dioxido. - One of the most interesting d important applications of the theory of superhented vapors found in the approximate calculation of properties of certain atile liquids which are used in refrigerating-machines, and for ich we have not sufficient experimental data to construct tubles the manner explained in the chapter on saturated vapors.

For example, Regnault made experiments on the pressures of saturated sulphur dioxide and ammonia, but did not determine the heat of the liquid nor the total heat. He did, however, determine some of the properties of these substances in the gaseous or superheated condition, from which it is possible to, construct the characteristic equations for the superheated vapors. These equations can then be used to make approximate calculations of the saturated vapors, for such equations are assumed to be applicable down to the saturated condition. Of course such calculations are subject to a considerable unknown error, since the experimental data are barely sufficient to establish the equations for the superheated vapors.

The specific heat of gaseous sulphur dioxide is given by Regnault \* as 0.15438, and the coefficient of dilatation as 0.0039028. The theoretical specific gravity compared with air, calculated from the chemical composition, is given by Landolt and Börnstein † as 2.21295. Gmelin ‡ gives the following experimental determinations: by Thomson, 2.222; by Berzelius, 2.247. The figure 2.23 will be assumed in this work, which gives for the specific volume at freezing-point and at atmospheric pressure

$$v_0 = \frac{0.7733}{2.23} = 0.347$$
 cubic metres.

The corresponding pressure and temperature are 10,333 and 273° C.

At this stage it is necessary to assign a probable form for the characteristic equation, and for that purpose the form

$$pv = BT - Cp^a \quad . \quad . \quad . \quad . \quad . \quad (125)$$

proposed by Zeuner has commonly been used, and it is convenient to admit that it may take the form

$$pv = \frac{c_p}{A} aT - Cp^a \dots \dots (126)$$

<sup>\*</sup> Mémoires de l'Institut de France, tome xxi, xxvi.

<sup>†</sup> Physikalische-chemische Tabellen.

<sup>#</sup> Watt's translation, p. 280.

The value of the arbitrary constant a may be determined from the coefficient of dilatation as follows. The coefficient of dilatation is the ratio of the increase of volume at constant pressure, for one degree increase of temperature, to the original volume; so that the preceding equation applied at o° C. and at 1° C. gives

$$p_0 v_0 = \frac{c_p}{A} a T_0 - C p_0^a;$$

$$p_0 v_1 = \frac{c_p}{A} a T_1 - C p_0^a;$$

$$\therefore \frac{v_1 - v_0}{v_0} = \frac{c_p}{A} \frac{a}{p_0 v_0}.$$

The value of a obtained by substituting known values in the above equation is 0.212. Now as a appears in both the first and the last terms of the right-hand side of equation (126), a considerable change in a has but little effect on the computations by aid of that equation. As will appear later an assumption of a value 0.22 for a will make equation (126) agree well with certain experiments on the compressibility of sulphur dioxide, and it will consequently be chosen. If now we reverse the process by which a was calculated from the coefficient of dilatation, the latter constant will appear to have a computed value of 0.004, which is but little different from the experimental value.

To compute C we have

$$0.15438 \times 426.9 \times 0.22 = 14.5$$

and the coefficient of  $p^a$  is

$$\frac{14.5 \times 273 - 10333 \times 0.347}{10333^{0.22}} = 48 \text{ nearly};$$

so that the equation becomes

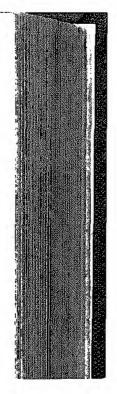
$$pv = 14.5 T - 48 \dot{p}^{0.22} \dots \dots (127)$$

Regnault found for the pressures

$$p_1 = 697.83$$
 mm. of mercury,  $p_2 = 1341.58$  mm. of mercury,

and at 7°.7 C. the ratio

$$\frac{p_1 v_1}{p_2 v_2} = 1.02088.$$



Reducing the given pressures to kilograms on the square metre, and the temperature to the absolute scale, and applying to equation (127), we obtain 1.016 instead of the experimental value for the above ratio.

Regnault gives for the pressure of saturated sulphur dioxide, in mm. of mercury, the equation

$$\log p = a - b\alpha^{n} - c\beta^{n};$$

$$a = 5.6663790;$$

$$\log b = 0.4792425;$$

$$\log c = 9.1659562 - 10;$$

$$\log \alpha = 9.9972980 - 10;$$

$$\log \beta = 9.98729002 - 10;$$

$$n = l + 28^{\circ} C.$$

Applying equation (95), page 76, to this case,

$$\frac{1}{p} \frac{dp}{dt} = A\alpha^{n} + B\beta^{n};$$

$$\log \alpha = 9.9972989;$$

$$\log \beta = 9.98729002;$$

$$\log A = 8.6352146;$$

$$\log B = 7.9945332;$$

$$n = t + 28^{\circ} C.$$

The specific volume of saturated sulphur dioxide may be calculated by inserting in equation (127) for the superheated vapor the pressures calculated by aid of the above equation. The results at several temperatures are as follows:

Andréest \* gives for the specific gravity of suid sulphur dioxide 1.4336; consequently the specific volume of the liquid is

The value of r, the heat of vaporization, may now be calculated at the given temperatures by equation (106), page 89.

$$r = AuT \frac{dp}{dt},$$

in which

The results are

Within the limits of error of our method of calculation, the value of r may be found by the equation

The specific heat of the liquid is derived by the following device. First assume that the entropy of the superheated vapor may be calculated by the equation

$$d\phi = c_p \cdot \frac{d\ell}{\ell} + (\epsilon_r - \epsilon_p) \cdot \frac{d\rho}{\rho}$$

given on page 67 for perfect gases. This may be transformed into  $\frac{dt}{dt} = \frac{\kappa}{2} - \frac{1}{4} \frac{T}{4} \frac{\lambda}{2}$ 

 $d\phi \approx c_p \left(\frac{dt}{T} - \frac{\kappa - 1}{\kappa} \frac{T}{\rho} d\rho\right) \dots \dots$  (139)

But if we introduce into the equation for a perfect gas

the value of R from the equation

the characteristic equation may take the form

Comparison of this equation with equation (126) suggests replacing the term  $\frac{\kappa-1}{\kappa}$  in equation (120) by the arbitrary factor a, so that it may read

The expression for the entropy of a liquid and its vapor is

$$\frac{\Delta r}{T} + \theta$$
 or  $\frac{r}{T} + \int c dt$ 

if the vapor is dry. When differentiated this yields

$$d\phi = \frac{1}{T} \left( cdt + dr - \frac{r}{T} dt \right) . . . . (131)$$

If it be assumed that equations (130) and (131) may both be applied at saturation we have

$$c_p \left( 1 - a \frac{T}{p} \frac{dp}{dt} \right) = c + \frac{dr}{dt} - \frac{r}{T} \cdot \cdot \cdot (132)$$

If it be admitted further that the differential coefficient  $\frac{dp}{dt}$  can be computed by the equation on page 120, the above equation affords a means of estimating the specific heat of the liquid. At  $o^{\circ}$  C., this method gives for the specific heat

In English units we have for superheated sulphur dioxide

$$pv = 26.4 T - 184 p^{0.33} \dots (133)$$

the pressures being in pounds on the square foot, the volumes in cubic feet, and the temperatures in Fahrenheit degrees absolute.

For pressures in pounds on the square inch at temperatures on the Fahrenheit scale,

$$\log p = a - b\alpha^{n} - c\beta^{n};$$

$$a = 3.9527847;$$

$$\log b = 0.4792425;$$

$$\log c = 9.1659562 - 10;$$

$$\log \alpha = 9.9984994 - 10;$$

$$\log \beta = 9.99293890 - 10;$$

$$n = t + 18^{\circ}.4 \text{ F}.$$



For the heat of vaporization

$$r = 176 - 0.27 (t - 32) . . . (134)$$

and for the specific heat of the liquid

In applying these equations to the calculation of a table of the properties of saturated sulphur dioxide the pressures corresponding to the temperatures are calculated as usual. Then the heat of the liquid is calculated by aid of the constant specific heat. The heat of vaporization is calculated by aid of equation (134). Next the specific volume is calculated by inserting the given temperature and the corresponding pressure for the saturated vapor in the characteristic equation (133). Having the specific volume of the vapor and that of the liquid, the heat equivalent (Apu) of the external work is readily found. Finally, the entropy of the liquid is calculated by the equation

If the reader should object that this method is tortuous and full of doubtful approximations and assumptions, he must bear in mind that any method that can give approximations is better than none, and that all the computations for refrigerating-machines, that use volatile fluids, depend on results so obtained. And further, much of the waste and disappointment of earlier refrigerating-machines could have been avoided if tables as good as those computed by this method were then available.

Properties of Ammonia. — The specific heat of gaseous ammonia, determined by Regnault, is 0.50836. The theoretical specific gravity compared with air, calculated from the chemical composition, is given by Landolt and Bornstein as 0.58890. Gmelin gives the following experimental determinations: by Thomson, 0.593x; by Biot and Arago, 0.5967. For this work the figure 0.597 will be assumed, which gives for the specific volume at freezing-point and at atmospheric pressure

$$v_0 = \frac{0.7733}{0.597} = 1.30$$
 cubic metres.

The coefficient of dilatation has not been determined, and consequently cannot be used to determine the value of a in equation (126). It, however, appears that consistent results are obtained if a is assumed to be  $\frac{1}{2}$ . The coefficient of T then becomes

$$0.50836 \times 426.9 \times \frac{1}{2} = 54.3$$

and the coefficient of  $p^{\frac{1}{2}}$  is

$$\frac{54.3 \times 273 - 10333 \times 1.30}{10333^{1}} = 142;$$

so that the equation becomes

$$pv = 54.3 T - 142 p^{\frac{1}{2}} \dots \dots (136)$$

The coefficient of dilatation, calculated by the same process as was used in determining a for sulphur dioxide, is 0.00404, which may be compared with that for sulphur dioxide.

Regnault found for the pressures

$$p_1 = 703.50$$
 mm. of mercury,  
 $p_2 = 1435.3$  mm. of mercury,

and at 8°.1 C. the ratio

$$\frac{p_1v_1}{p_2v_2}=1.0188,$$

while equation (136) gives under the same conditions 1.0200.

For saturated ammonia Regnault gives the equation

$$\log p = a - b\alpha^{n} - c\beta^{n};$$

$$a = 11.5043330;$$

$$\log b = 0.8721769;$$

$$\log c = 9.9777087 - 10;$$

$$\log \alpha = 9.9996014 - 10;$$

$$\log \beta = 9.9939729 - 10;$$

$$n = t + 22^{\circ} C.;$$



by aid of which the pressures in mm. of mercury may be calculated for temperatures on the centigrade scale. The differential coefficient may be calculated by aid of the equation

$$\frac{1}{p} \frac{dp}{dt} = A\alpha^{n} + B\beta^{n};$$

$$\log A = 8.1635170 - 10;$$

$$\log B = 8.4822485 - 10;$$

$$\log \alpha = 9.9996014 - 10;$$

$$\log \beta = 9.9939729 - 10;$$

$$n = t + 22^{\circ} C.$$

The specific volume of saturated ammonia calculated by equation (136) at several temperatures are

$$t - 30^{\circ} \text{ C.}$$
 0 + 30° C.  
 $s - 0.9982$  0.2961 0.1167

Andréess gives for the specific gravity of liquid ammonia at 0° C. 0.6364, so that the specific volume of the liquid is

$$\sigma = 0.0016$$
.

The values of r at the several given temperatures, calculated by equation (128), are

$$t = -30^{\circ}$$
.C. o  $+30^{\circ}$  C.  $r = 325.7$  300.15 277.5

which may be represented by the equation

$$r = 300 - 0.8 t$$
.

The specific heat of the liquid, calculated by aid of equation (132), is

$$c = r.r$$

In English units the properties of superheated or gaseous ammonia may be represented by the equation

$$pv = 99 T - 710 p^3$$

in which the pressures are taken in pounds on the square foot and volumes in cubic feet, while T represents the absolute temperature in Fahrenheit degrees.

The pressure in pounds on the square inch may be calculated by the equation

log  $p = a - b\alpha^n - c\beta^n$ ; a = 9.7907380; log b = 0.8721769 - 10; log c = 9.9777087 - 10; log  $\alpha = 9.9997786 - 10$ ; log  $\beta = 9.9966516 - 10$ ;  $n = t + 7^{\circ}.6 F$ .

The heat of vaporization may be calculated by the equation

$$r = 540 - 0.8(t - 32),$$

and the specific heat of the liquid is

C con I.I.

### EXAMPLES,

1. What is the weight of one cubic foot of superheated steam at 500° F, and at 60 pounds pressure absolute? Knoblauch's equation. Ans. 0.106 pounds.

2. Superheated steam at 50 pounds absolute has half the density of saturated steam at the same pressure. What is the temperature? Tumlirz's equation. Ans. 930° F.

3. What is the volume of 5 pounds of steam at 129.3 pounds gauge pressure and at 359°.5 F.? Ans. 15.8.

4. At 129.3 pounds gauge pressure 2 pounds of steam occupy 7 cubic feet. Find its temperature. Assume value of T for entering Table I, page 112, and solve by trial. Ans. 424° F.

5. A cubic foot of steam at 140 pounds absolute weighs 0.30 pounds. What is its temperature? Ans. 374° F.

6. Two pounds of steam and water at 120.3 pounds pressure above the atmosphere occupy 6 cubic feet. Heat is added and the pressure kept constant till the volume is 8.5 cubic feet. Find the final condition, and the external work done in expanding. Ans. Temperature 681° F.; work 51800.



7. Saturated steam at 150 pounds gauge, containing 2 per cent of water, passes through a superheater on its way to an engine. Its final temperature is 400° F. Find the increase in volume and the heat added per pound. 8. Let the initial temperature of superheated steam be 380° F. at the pressure of 150 pounds absolute. Find the condition after an adiabatic expansion to 20 pounds absolute. Determine also the initial and final volumes. Ans. (1) 0.895; (2) 3.09 cubic feet; (3) 17.8 cubic feet. 9. In example 14, page 109, suppose that the steam at cut-off were superheated 10° F. above the temperature of saturated steam at the given pressure, and solve the example. Ans. (1) 0.887; (2) 87° superheating; (3) same as before; (4) n =1.137; (5) 1972 and 1950 foot-pounds.

### CHAPTER VIII.

### THE STEAM-ENGINE.

THE steam-engine is still the most important heat-engine, though its supremacy is threatened on one hand by the steam-turbine and on the other by the gas-engine. When of large size and properly designed and managed its economy is excellent and can be excelled only by the largest and best gas-engines, and in many cases these engines (even with the advantage of a more favorable range of temperature) depend for their commercial success on the utilization of by-products.

It can be controlled, regulated, and reversed easily and positively — properties which are not possessed in like degree by other heat-engines. It is interesting to know that the theory of thermodynamics was developed mainly to account for the action and to provide methods of designing steam-engines; though neither object is entirely accomplished, on account of the fact that the engine-cylinder must be made of some metal to be hard and strong enough to endure service, for all metals are good conductors of heat, and seriously affect the action of a con-

densable fluid like steam.

Carnot's Cycle for a steam-engine is represented by Fig. 31, in which ab and cd are isothermal lines, representing the application and rejection of heat at constant temperature and at constant pressure. bc and da are adiabatic lines, representing change of temperature and pressure, without transmission of heat through the walls of the cylinder.

The diagram representing Carnot's cycle has an external resemblance to the indicator-diagram from some actual engines, but it differs in essential particulars.



In the condition represented by the point a the cylinder contains a mixture of water and steam at the temperature  $t_1$  and the pressure  $p_1$ . If connection is made with a source of heat at the temperature  $t_1$ , and heat is added, some of the water will be vaporized and the volume will increase at constant pressure as represented by ab. If thermal communication is now interrupted, adiabatic expansion may take place as represented by bc till the temperature is reduced to  $t_2$ , the temperature of the refrigerator, with which thermal communication may now be established. If the piston is forced toward the closed end of the cylinder some of the steam in it will be condensed, and the volume will be reduced at constant pressure as represented by cd. The cycle is completed by an adiabatic compression represented by da.

If the absolute temperature of the source of heat is  $T_1$ , and if that of the refrigerator is  $T_2$ , then the efficiency is

$$e = \frac{T_1 - T_2}{T_1}$$

whatever may be the working fluid.

For example, if the pressure of the steam during isothermal expansion is 100 pounds above the atmosphere, and if the pressure during isothermal compression is equal to that of the atmosphere, then the temperatures of the source of heat and of the refrigerator are 337°.6 F. and 212° F., or 797.1 and 671.5 absolute, so that the efficiency is

$$\frac{797.1 - 671.5}{797.1} = 0.157.$$

The following table gives the efficiencies worked out in a similar way, for various steam-pressures, — both for  $t_2$  equal to  $212^{\circ}$  F., corresponding to atmospheric pressure, and for  $t_2$ , equal to  $116^{\circ}$  F., corresponding to an absolute pressure of 1.5 pounds to the square inch:

### EFFICIENCY OF CARNOT'S CYCLE FOR STEAM-ENGINES.

Initial Pressure by the Gauge, above the Atmosphere.	Atmospheric Pressure.	1.3 Pounds Absolute.
15	0.053	o. 18g
30	0.084	0.215
бо	0.124	0.249
100	0.157	0.278
150	0.186	0.302
200	0,207	0.320
300	0.238	0.347

The column for atmospheric pressure may be used as a standard of comparison for non-condensing engines, and the column for 1.5 pounds absolute may be used for condensing engines.

It is interesting to consider the condition of the fluid in the cylinder at the different points of the diagram for Carnot's cycle. Thus if the fluid at the condition represented by b in Fig. 31 is made up of  $x_b$  part steam and  $1-x_b$  part water, then from equation (118) the condition at the point c is given by

$$x_{o} = \frac{T_{2}}{r_{2}} \left( \frac{r_{1}}{T_{1}} x_{b} + \theta_{1} - \theta_{2} \right) . . . . . (137)$$

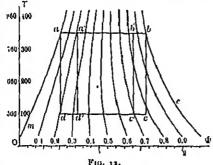
In like manner the condition of the mixture at the point d is

$$x_d = \frac{T_2}{r_2} \left( \frac{r_1}{T_1} x_a + \theta_1 - \theta_2 \right) . . . . . (138)$$

It is interesting to note that if  $x_b$  is larger than one-half, that is, if there is more steam than water in the cylinder at b, then the adiabatic expansion is accompanied by condensation. Again, if  $x_a$  is less than one-half, then the adiabatic compression is also accompanied by condensation. Very commonly it is assumed that  $x_b$  is unity, so that there is dry saturated steam in the cylinder at b; and that  $x_a$  is zero, so that there is water only in the

ylinder at a; but there is no necessity for such assumptions, nd they in no way affect the efficiency.

The temperature-entropy diagram for Carnot's cycle for a team-engine is shown by Fig. 32, on which are drawn also the



he isothermal condensation along cd, and the condensation uring the adiabatic compression da. In the diagram the working substance is shown as water at a and as dry steam at b; he efficiency would clearly be the same for a cycle a' b' c' d', which contains a varying mixture of water and steam under all conditions.

If the cylinder contains M pounds of steam and water, the sat absorbed by the working substance during isothermal spansion is

$$Q_i = Mr_i (x_b - x_a) . . . . . . (139)$$

nd the heat rejected during isothermal compression is

$$Q_1 = Mr_1 (x_0 - x_d)_1$$

that the heat changed into work during the cycle is

$$Q_1 - Q_2 = M[r_1 (x_b - x_a) - r_2 (x_a - x_d)]$$

But from equations (137) and (138)

$$r_2 (x_0 - x_d) = \frac{T_2}{T_1} r_1 (x_b - x_a),$$

and the expression for the heat changed into work becomes

$$Q_1 - Q_2 = Mr_1 (x_b - x_a) \frac{T_1 - T_2}{T_1} \cdot \cdot \cdot (140)$$

This equation is deduced because it is convenient for making comparisons of various other volatile liquids and their vapors, with steam, for use in heat-engines. It is of course apparent that C = C = T = T.

 $e = \frac{Q_1 - Q_2}{Q_1} = \frac{T_1 - T_2}{T_1},$ 

from equations (139) and (140), a conclusion which is known independently, and indeed is necessary in the development of the theory of the adiabatic expansion of steam.

In the discussion thus far it has been assumed that the working fluid is steam, or a mixture of steam and water. But a mixture of any volatile liquid and its vapor will give similar results, and the equations deduced can be applied directly. The principal difference will be due to the properties of the vapor considered, especially its specific pressures and specific volumes for the temperatures of the source of heat and the refrigerator.

For example, the efficiency of Carnot's cycle for a suid working between the temperatures 160° C. and 40° C. is

$$\frac{160 - 40}{160 + 273} = 0.277.$$

The properties of steam and of chloroform at these tempera-

tures are			Sto	am.	Chloroform.		
			40° C.	160° C.	40° C.	160° C.	
Pressure, mm. mercury			54.91	4651.4	369.26	8734.2	
Volume, cubic metres .			19.74	0.3035	0.4449	0.0243	
Heat of vaporization, r			578.7	494.2	63.13	50.53	
Entropy of liquid, 0			0.1364	0.4633	0.03196	0.11041	

For simplicity, we may assume that one kilogram of the fluid is used in the cylinder for Carnot's cycle, and that  $x_b$  is unity while  $x_a$  is zero, so that from equation (140)

$$Q_1 - Q_2 = r_1 \frac{T_1 - T_2}{T_1},$$

and for steam

$$Q_1 - Q_2 = 494.2 \times 0.277 = 137$$
 calories,

while for chloroform

$$Q_1 - Q_2 = 50.53 \times 0.277 = 14$$
 calories.

After adiabatic expansion the qualities of the fluid will be, from equation (137), for steam

$$x_0 = \frac{40 + 273}{578} \left( \frac{494.2}{160 + 273} + 0.4633 - 0.1364 \right) = 0.795.$$

and for chloroform

$$x_o = \frac{40 + 273}{63.13} \left( \frac{50.53}{100 + 273} + 0.11041 - 0.03190 \right) + 0.969.$$

The specific volumes after adiabatic expansion are, consequently, for steam

$$v_c = x_c \mu_1 + \sigma = 0.795 (19.74 - 0.001) + 0.001 = 15.7,$$

and for chloroform

$$v_a = x_a u_a + \sigma = 0.969 (0.4440 - 0.000655) + 0.000655 = 0.431.$$

These values for  $v_o$  just calculated are the volumes in the cylinder at the extreme displacement of the piston, on the assumption that one kilogram of the working fluid is vaporized during isothermal expansion. A better idea of the relative advantages of the two fluids will be obtained by finding the heat changed into work for each cubic metre of maximum piston-displacement, or for a cylinder having the volume of one cubic metre. This is obtained by dividing  $Q_1 - Q_2$ , the heat changed into work for each kilogram by  $v_c$ . For steam the result is

$$(Q_1 - Q_2) + v_0 \approx 137 + 15.7 \approx 8.73$$

and for chloroform it is

from which it appears that for the same volume chloroform can produce more than three and a half times as much power.

Even if we consider that the difference of pressure for chloro, form,

is nearly twice that for steam, which has only

$$4651.4 - 54.9 = 4596.5 \text{ mm}.$$

difference of pressure, the advantage appears to be in favor of chloroform. If, however, the difference of pressures given for chloroform is allowable also for steam, giving

for the superior pressure, then the initial temperature for steam becomes 184°.9 C., and the efficiency becomes

$$\frac{184.9 - 40}{184.9 + 273} = 0.318,$$

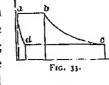
instead of 0.277. On the whole, steam is the more desirable fluid, even if we do not consider the inflammable and poisonous nature of chloroform. Similar calculations will show that on the whole steam is at least as well adapted for use in heat-engines as any other saturated fluid; in practice, the cheapness and incombustibility of steam indicate that it is the preferable fluid for such uses.

Non-conducting Engine. Rankine Cycle. — The conditions required for alternate isothermal expansion and adiabatic expansion cannot be fulfilled for Carnot's cycle with steam any more than they could be for air. The diagram for the cycle with steam, however, is well adapted to production of power; the contrary is the case with air, as has already been shown.

In practice steam from a boiler is admitted to the cylinder of the steam-engine during that part of the cycle which corresponds to the isothermal expansion of Carnot's cycle, thus transferring the isothermal expansion to the boiler, where steam is formed under constant pressure. In like manner the isothermal compression is replaced by an exhaust at constant pressure, during which steam may be condensed in a separate condenser,

oled by cold water. The cylinder is commonly made of cast on, and is always some kind of metal; there is consequently nsiderable interference due to the conductivity of the walls of e cylinder, and the expansion and compression are never liabatic. There is an advantage, however, in discussing first engine with a cylinder made of some non-conducting material, though no such material proper for making cylinders is now own. The diagram representing the operations in a non-conducting

linder for a steam-engine (sometimes called the Rankine cycle) n be represented by Fig. 33. ab represents e admission of dry saturated steam from e boiler; bc is an adiabatic expansion to the haust pressure; cd represents the exhaust; nd da is an adiabatic compression to the itial pressure. It is assumed that the small



plume, represented by a, between the piston and the head of e cylinder is filled with dry steam, and that the steam remains omogeneous during exhaust so that the quality is the same at as at c. These conditions are consistent and necessary, nce the change of condition due to adiabatic expansion (or empression) depends only on the initial condition and the itial and final pressures; so that an adiabatic expansion from to d would give the same quality at d as that found at c after diabatic expansion from b, and conversely adiabatic compreson from d to a gives dry steam at a as required.

The cycle represented by Fig. 33 differs most notably from arnot's cycle (Fig. 32) in that ab represents admission of steam nd cd represents exhaust of steam, as has already been pointed ut. It also differs in that the compression da gives dry steam istead of wet steam. The compression line da is therefore sceper than for Carnot's cycle, and the area of the figure is ightly larger on this account. This curious fact does not dicate that the cycle has a higher efficiency; on the contrary, ne efficiency is less, and the cycle is irreversible.

If the pressure during admission (equal to the pressure in



the boiler) is  $p_{1}$ , and if the pressure during exhaust is  $p_{2}$ , then the heat required to raise the water resulting from the condensation of the exhaust-steam is

$$q_1 - q_2$$

where  $q_1$  is the heat of the liquid at the pressure  $p_1$ , and  $q_2$  is the heat of the liquid at the pressure  $p_2$ . The heat of vaporization at the pressure  $p_1$  is  $r_1$ , so that the heat required to raise the feedwater from the temperature of the exhaust to the temperature in the boiler and evaporate it into dry steam is

$$Q_1 \stackrel{\text{\tiny cos}}{=} r_1 + q_1 - q_2 + \cdots + q_1$$

and this is the quantity of heat supplied to the cylinder per pound of steam.

The steam exhausted from the cylinder has the quality  $x_p$  calculated by aid of the equation

$$x_2 = \frac{T_2}{r_2} \left( \frac{r_1}{T_1} + \theta_1 - \theta_2 \right),$$

and the heat that must be withdrawn when it is condensed is

$$Q_1 = x_2 r_2 \dots \dots (142)$$

this is the heat rejected from the engine. The heat changed into work per pound of steam is

$$Q_1 - Q_2 = r_1 + q_1 - q_2 - x_2 r_2 + \cdots$$
 (143)

The efficiency of the cycle is

$$e = \frac{Q_1 - Q_2}{Q_1} = \frac{x_2 r_2}{r_1 + q_1 - q_2} . . . (144)$$

If values are assigned to  $p_1$  and  $p_2$  and the proper numerical calculations are made, it will appear that the efficiency for a non-conducting engine is always less than the efficiency for Carnot's cycle between the corresponding temperatures.

It should be remarked that the efficiency is not affected by the clearance or space between the piston and the head of the cylinder and the space in the steam-passages of the cylinder, provided that the clearance is filled with dry saturated steam as indicated in Fig. 33. This is evident from the fact that no term representing the clearance, or volume at a, Fig. 33, appears in equation (144). Or, again, we may consider that the steam in the cylinder at the beginning of the stroke, occupying the volume represented by a, expands during the adiabatic expansion and is compressed again during compression, so that one operation is equivalent to and counterbalances the other, and so does not affect the efficiency of the cycle.

Use of the Temperature-Entropy Diagram. The Ranking cycle is drawn with a varying quantity of steam in the cylinder, beginning at a, Fig. 33, with the steam caught in the clearance and finishing at b, with that weight plus the weight drawn from the boiler; consequently a proper temperature entropy diagram, which represents the changes of one pound of the working sub-

stance, cannot be drawn.

We may, however, use the temperature entropy diagram (like Fig. 30, page 104, or the plate at the end of the book) for solving problems connected with that cycle instead of equations (143) and (144).

In the first place we have by equation (96), page 83,

$$q = \int c dt$$

and by equation (113), page 97,

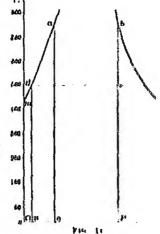
$$\theta = \int \frac{cdt}{T}$$

for a volatile liquid. From the latter we have

therefore

ACCOUNT NO.

$$q = \int T d\theta$$
.



From this last equation it is evident that the heat of the liquid  $q_1$  for water represented by the point a in Fig. 34, is measured by

the area Omao. In like manner the heat of the liquid  $q_1$  corresponding to the point  $d_1$  is represented by the area Omdn. Again, the heat added during the vaporization represented by  $ab_1$  is  $r_1$ , while the increase of entropy is  $\frac{r_1}{T_1}$ . Therefore the heat of vaporization can be represented by the area oabp. In like manner the partial vaporization  $x_2r_2$  can be represented by the area ndcp. Therefore the heat changed into work for the cycle in Fig. 33, which has been represented by

$$r_1 + q_1 - (x_2r_2 + q_2),$$

can equally well be represented by the area

abcd \( \) area Omao + area oabp - (area Omdo + area ndcp).

It will consequently be sufficient to measure the area abcd by any means, for example, by aid of a planimeter, in order to determine the heat changed into work during the operation of the non-conducting engine working on the Rankine cycle. If the planimeter determines the area in square inches, the scale of the drawing for Fig. 34 should be one inch per degree, and one inch per unit of entropy, or, if other and more convenient scales are to be used, proper reductions must be made to allow for those scales.

It must be firmly fixed in mind that the use of a diagram like Fig. 34 is justified because it has been proved that the area abcd (drawn to the proper scale) is numerically equal to the heat changed into work as computed by equation (143), and that the diagram does not represent the operations of the cycle. This is entirely different from the case of the diagram, Fig. 32, which correctly represents the operations of Carnot's cycle.

The illustration of the use of the temperature-entropy diagram for this purpose is chosen for convenience with dry saturated steam at b, Fig. 34. It is evident that it could (with equal propriety) be applied to an engine supplied with moist steam if  $r_i$  is replaced by  $x_i r_i$  in equation (143) and if b is located at the proper place between a and b.

"The actual measurement of areas by a planimeter is seldom

if ever applied, but the diagram is used effectively in the discussion of certain problems of non-reversible flow of steam in nozzles and turbines, with allowance for friction.

It further suggests an approximation that may sometimes be useful, especially if the change of pressure (and temperature) is small. Thus the area abcd may be approximately represented by the expression

$$\frac{1}{2} (ab + dc) bc = \frac{1}{2} \left( \frac{r_1}{T_1} + \frac{x_2 r_2}{T_2} \right) (t_1 - t_2),$$

so that in place of equation (143) we may have

$$Q_1 - Q_2 = \frac{1}{2} \left( \frac{r_1}{T_1} + \frac{x_2 r_2}{T_2} \right) (t_1 - t_2) . . . . (145)$$

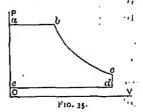
for the heat changed into work by Rankine's cycle.

This approximation depends on treating ab as a straight line, and this assumption is more correct as the difference of temperature is less; that is for those cases in which equation (143) deals with the difference of quantities of about the same magnitude, and may consequently be affected by a large relative error.

Temperature-Entropy Table. — The temperature-entropy table which has been described on page 106 was computed for solution of problems of this nature, more especially in turbine design, and enables us to determine the heat changed into work directly with sufficient accuracy for engineering work, without interpolation; it also gives the quality x and the specific volume.

Incomplete Cycle. — The cycle for a non-conducting engine may be incomplete because the expansion is not carried far

enough to reduce the pressure to that of the back-pressure line, as is shown in Fig. 35. Such an incomplete cycle has less efficiency than a complete cycle, but in practice the advantage of using a smaller cylinder and of reducing friction is sufficient compensation for the



small loss of efficiency due to a moderate drop at the end of

the stroke, as shown in Fig. 35.





The discussion of the incomplete cycle is simplified by ing that there is no clearance and no compression as is in by Fig. 35. It will be shown later that the efficiency will same with a clearance, provided the compression is complete.

The most ready way of finding the efficiency for this to determine the work of the cycle. Thus the work admission is  $p_1(u_1 + \sigma)$ ,

where  $u_1$  is the increase of volume due to vaporization of a of steam, and  $\sigma$  is the specific volume of water. The work expansion is

$$E_b - E_o = \frac{1}{A} (\rho_1 + q_1 - x_c \rho_o - q_o),$$

where  $q_i$  and  $\rho_i$  are the heat of the liquid and the heat-equal of the internal work during vaporization at the press while  $q_o$  and  $\rho_o$  are corresponding quantities for the pressum  $x_o$  is to be calculated by the equation

$$x_o = \frac{T}{r_o} \left( \frac{r_{\perp}}{T_i} + \theta_i - \theta_o \right).$$

The work done by the piston on the steam during exi

$$p_2(x_ou_o + \sigma).$$

The total work of the cycle is obtained by adding the during admission and expansion and subtracting the during exhaust, giving

$$\frac{1}{A} (\rho_1 + A p_1 u_1 - x_0 \rho_0 - A p_2 x_1 u_0 + q_1 - q_0) + (p_1 - p_2)$$

The last term is small, and may be neglected. Addli subtracting  $A p_c x_o u_o$  and multiplying by A, we get for **t**l equivalent of the work of the cycle

$$Q_1 - Q_2 = r_1 - x_c r_o + A(p_c - p_2) u_o x_o + q_1 - q$$

which is equal to the difference between the heat supplied and the heat rejected as indicated. The heat supplied is

$$Q_1 = r_1 + q_1 - q_n$$

as was deduced for the complete cycle; the cost of making the steam remains the same, whether or not it is used efficiently. Finally, the efficiency of the cycle is

$$e = \frac{Q_1 - Q_2}{Q_1} = \frac{r_1 + q_1 - x_1 r_2 \cdots q_c + A (p_c - p_2) x_2 u_c}{r_1 + q_1 - q_2}$$

$$\therefore e = 1 - \frac{x_c r_c + q_c - q_2 - A (p_c - p_2) x_c u}{r_1 + q_1 - q_2} \qquad (1.48)$$

If  $p_{\theta}$  is made equal to  $p_{\theta}$  in the preceding equation, it will be reduced to the same form as equation (1.1.1), because the expansion in such case becomes complete.

Steam-Consumption of Non-conducting Engine. A horse power is 33000 foot-pounds per minute or 60 × 33000 foot pounds per hour. But the heat changed into work per pound of steam by a non-conducting engine with complete expansion is, by equation (143),

$$r_1 + q_1 - q_2 - x_2 r_2$$

so that the steam required per horse-power per hour is

$$\frac{60 \times 33000}{778 (r_1 + q_1 - q_2 - x_2 r_2)}$$

Similarly, the steam per horse-power per hour for an engine with incomplete expansion, by aid of expression (1.16), is

$$\frac{60 \times 33000}{778 (\rho_1 + A \rho_1 u_1 - x_0 \rho_0 - A \rho_2 x_0 u_0 + q_1 - q_0)}$$

The value of  $x_2$  or  $x_4$  is to be calculated by the general equation

$$x = \frac{T}{r} \left( \frac{r_1}{T_1} + \theta_1 - \theta \right).$$

The denominator in either of the above expressions for the steam per horse-power per hour is of course the work done per pound of steam, and the parenthesis without the mechanical



equivalent 778 is equal to  $Q_1 - Q_2$ . If then we multiply and divide by

 $Q_1 = r_1 + q_1 - q_2,$ 

that is, by the heat brought from the boiler by one pound of steam, we shall have in either case for the steam consumption in pounds per hour

$$\frac{60 \times 33000 \times Q_1}{778 (Q_1 - Q_2) Q_1} = \frac{60 \times 33000}{778e (r_1 + q_1 - q_2)} \quad . \quad . \quad (149)$$

where

$$c = \frac{Q_1 - Q_2}{Q_1}$$

is the efficiency for the cycle.



Actual Steam-Engine. — The indicator-diagram from an actual steam-engine differs from the cycle for a non-conclucting engine in two ways: there are losses of pressure between the boiler and the cylinder and between the cylinder and the conclenser, due to the resistance to the flow of steam through pipes, valves, and passages; and there is considerable interference of the metal of the cylinder with the action of the steam in the cylinder. The losses of pressure may be minimized for a slow-moving engine by making the valves and passages direct and large. The interference of the walls of the cylinder cannot be prevented, but may be ameliorated by using superheated steam or by steam-jacketing.

When steam enters the cylinder of an engine, some of it is condensed on the walls which were cooled by contact with exhaust-steam, thereby heating them up nearly to the temperature of the steam. After cut-off the pressure of the steam is reduced by expansion and some of the water on the walls of the cylinder vaporizes. At release the pressure falls rapidly to the back-pressure, and the water remaining on the walls is nearly if not all vaporized. It is at once evident that so much of the heat as remains in the walls until release and is thrown out during exhaust is a direct loss; and again, the heat which is restored during expansion does work with less efficiency,

decause it is reëvaporated at less than the temperature in the coiler or in the cylinder during admission. A complete statement of the action of the walls of the cylinder of an engine, with quantitative results from tests on engines, was first given by Hirn. His analysis of engine tests, showing the interchanges of heat between the walls of the cylinder and the steam, will be given later. It is sufficient to know now that a failure to consider the action of the walls of the cylinder leads to gross errors, and that an attempt to base the design of an engine on the theory of a steam-engine with a non-conducting cylinder can lead only o confusion and disappointment.

The most apparent effect of the influence of the walls of the

cylinder on the indicator-diagram is to change the expansion and the compression lines; the former exhibits this change most clearly. In the first place the fluid in the cylinder at cut-off consists of from twenty to fifty per cent hot water, which is found mainly adhering to the walls of the cylinder. Even if there were no action of the walls during expansion the curve would be much less steep than the adiabatic line for dry saturated steam. But the reëvaporation during expansion still further changes the curve, so that it is usually less steep than the rectangular hyperbola.

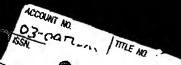
It may be mentioned that the fluctuations of temperature

in the walls of a steam-engine cylinder caused by the condensation and reëvaporation of water do not extend far from the surface, but that at a very moderate depth the temperature remains constant so long as the engine runs under constant conditions.

The performance of a steam-engine is commonly stated in pounds of steam per horse-power per hour. For example, a small Corliss engine, developing 16.35 horse-power when running at 61.5 revolutions per minute under 77.4 pounds boiler-pressure, used 548 pounds of steam in an hour. The steam consumption was

$$548 \div 16.35 = 33.5$$

pounds per horse-power, per hour.



This method was considered sufficient in the earlier history of the steam-engine, and may now be used for comparing simple condensing or non-condensing engines which use saturated steam and do not have a steam-jacket, for the total heat of steam, and consequently the cost of making steam from water at a given temperature increases but slowly with the pressure.

The performance of steam-engines may be more exactly stated in British thermal units per horse-power per minute. This method, or some method equivalent to it, is essential in making comparisons to discover the advantages of superheating, steam-jacketing, and compounding. For example, the engine just referred to used steam containing two per cent of moisture, so that  $x_1$  at the steam-pressure of 77.4 pounds was 0.98. The barometer showed the pressure of the atmosphere to be 14.7 pounds, and this was also the back-pressure during exhaust. If it be assumed that the feed-water was or could be heated to the corresponding temperature of 212° F., the heat required to evaporate it against 77.4 pounds above the atmosphere or 92.1 pounds absolute was

$$x_1 r_1 + q_1 - q_2 = 0.08 \times 888.0 + 202.1 - 180.3 = 982.0 \text{ n.t.u.}$$

The thermal units per horse-power per minute were

Efficiency of the Actual Engine. — When the thermal units per horse-power per minute are known or can be readily calculated, the efficiency of the actual steam-engine may be found by the following method: A horse-power corresponds to the development of 33000 foot-pounds per minute, which are equivalent to

thermal units. This quantity is proportional to  $Q_1 - Q_2$ , and the thermal units consumed per horse-power per minute are proportional to  $Q_1$  so that the efficiency is

For example, the Corliss engine mentioned above had an efficiency of

This same method may evidently be applied to any heatengine for which the consumption in thermal units per horse-

power per hour can be applied.

From the tests reported in Chapter XIII it appears that the engine in the laboratory of the Massachusetts Institute of Technology on one occasion used 13.73 pounds of steam per horse power per hour, of which 10.86 pounds were supplied to the cylinders and 2.87 pounds were condensed in steam jackets on the cylinders. The steam in the supply-pipe had the pressure of 157.7 pounds absolute, and contained 1.2 per cent of moisture. The heat supplied to the cylinders per minute in the steam admitted was

10.86 
$$(x_1r_1 + q_1 - q_2) + 60$$
  
= 10.86  $(0.988 \times 858.6 + 333.9 - 120.0) + 60$   
= 191 B.T.U.;

q<sub>2</sub> being the heat of the liquid at the temperature of the backpressure of 4.5 pounds absolute.

The steam condensed in the steam-jackets was withdrawn at the temperature due to the pressure and could have been returned to the boiler at that temperature; consequently the heat required to vaporize it was  $r_0$ , and the heat furnished by the steam in the jackets was

The heat consumed by the engine was

per horse-power per minute, and the efficiency was

The efficiency of Carnot's cycle for the range of temperatures corresponding to 157.7 and 4.5 pounds absolute, namely, 821°.7 and 617°.2 absolute, is

$$e = \frac{T_1 - T_2}{T_1} = \frac{821.7 - 617.2}{821.7} = 0.248.$$

The efficiency for a non-conducting engine with complete expansion, calculated by equation (144), is for this case

$$e'' = 1 - \frac{x_1 r_2}{r_1 + q_1 - q_2} = 1 - \frac{0.821 \times 1004.1}{858.6 + 333.9 - 126.0} = 0.227$$

where  $x_2$  is calculated by the equation

$$x_2 = \frac{T_2}{r_2} \left( \frac{r_1}{T_1} + \theta_1 - \theta_2 \right)$$

$$= \frac{617.2}{1004.1} \left( \frac{858.6}{821.7} + 0.5189 - 0.2282 \right) = 0.821.$$

During the test in question the terminal pressure at the end of the expansion in the low-pressure cylinder was 6 pounds absolute, which gives

$$x_0 = \frac{T_c}{r_0} \left( \frac{r_1}{T_1} + \theta_1 - \theta_2 \right)$$

$$= \frac{629.6}{995.8} \left( \frac{858.6}{821.7} + 0.5189 - 0.2475 \right) = 0.832,$$

and the efficiency by equation (148) was

$$c''' = 1 - \frac{x_c r_c - q_c + q_2 - A (p_c - p_2) x_0 u_0}{r_1 + q_1 - q_2}$$

$$= 1 - \frac{0.832 \times 995.8 - 138.0 + 126.0 + \frac{11}{11} (6 - 4.5) 0.832 \times 62}{858.6 + 333.9 - 126.0}$$

$$= 0.222.$$

The real criterion of the perfection of the action of an engine is the ratio of its actual efficiency to that of a perfect engine. If for the perfect engine we choose Carnot's cycle the ratio is

$$\frac{c}{c'} = \frac{0.183}{0.2485} = 0.736.$$

But if we take for our standard an engine with a cylinder of nonconducting material the ratio for complete expansion is

$$\frac{e}{e^{\prime\prime}} = \frac{0.183}{0.227} = 0.807.$$

For incomplete expansion the ratio is

$$\frac{e}{e'''} = \frac{0.183}{0.222} = 0.824.$$

To complete the comparison it is interesting to calculate the steam-consumption for a non-conducting steam-engine by equation (149), both for complete and for incomplete expansion. For complete expansion we have

$$\frac{60 \times 33000}{778 \times 0.227 (858.6 + 333.9 - 126.0)} = 10.5 \text{ pounds,}$$

and for incomplete expansion

$$\frac{60 \times 33000}{778 \times 0.222 (858.6 + 333.9 - 126.0)} = 10.7 \text{ pounds}$$

per horse-power per hour.

But if these steam-consumptions are compared with the actual steam-consumption of 13.73 pounds per horse-power per hour, the ratios are

$$10.5 \div 13.73 = 0.766$$
 and  $10.7 \div 13.73 = 0.783$ ,

which are very different from the ratios of the efficiencies. The discrepancy is due to the fact that more than a fourth of the steam used by the actual engine is condensed in the jackets and returned at full steam temperature to the boiler, while the non-conducting engine has no jacket, but is assumed to use all the steam in the cylinder.

From this discussion it appears that there is not a wide margin for improvement of a well-designed engine running under favorable conditions. Improved economy must be sought either by increasing the range of temperatures (raising the steam-pressure or improving the vacuum), or by choosing some other form of heat-motor, such as the gas-engine.

Attention should be called to the fact that the real criterion of the economy of a heat-engine is the cost of producing power by that engine. The cost may be expressed in thermal units per horse-power per minute, in pounds of steam per horse-power per hour, in coal per horse-power per hour, or directly in money. The expression in thermal units is the most exact, and the best for comparing engines of the same class, such as steam-engines. If the same fuel can be used for different engines, such as steam-and gas-engines, then the cost in pounds of fuel per horse-power per hour may be most instructive. But in any case the money cost must be the final criterion. The reason why it is not more frequently stated in reports of tests is that it is in many cases somewhat difficult to determine, and because it is affected by market prices which are subject to change.

At the present time a pressure as high as 150 pounds above the atmosphere is used where good economy is expected. It appears from the table on page 132, showing the efficiency of Carnot's cycle for various pressures, that the gain in economy by increasing steam-pressure above 150 pounds is slow. The same thing is shown even more clearly by the following table:

EFFECT OF RAISING STEAM-PRESSURE.

Boiler- pressure by Gauge.	Efficiency, Carnot'a Cycle,	Non-conduc	ing Engine.	Probable Performance, Actual Engine.			
		KMclency.	H.T.U. per H.P. per Minute.	H.P. per H.P. per Minute.	Steam per II.P. per Hour.		
150 200 300	0, 302 0, 320 0, 347	0,272 0,288 0,300	156 147 135	195 184 169	11.5 10.5 9.0		

In the calculations for this table the steam is supposed to be dry as it enters the cylinder of the engine, and the back-pressure is supposed to be 1.5 pounds absolute, while the expansion for the non-conducting engine is assumed to be complete. The

heat-consumption of the non-conducting engine is obtained by dividing 42.42 by the efficiency; thus for 150 pounds

The heat-consumption of the actual engine is assumed to be one-fourth greater than that of the non-conducting engine. The steam-consumption is calculated by the reversal of the method of calculating the thermal units per horse-power per minute from the steam per horse-power per hour, and for simplicity all of the steam is assumed to be supplied to the cylinder. But an engine which shall show such an economy for a given pressure as that set down in the table must be a triple or a quadruple engine and must be thoroughly steam-jacketed. The actual steam-consumption is certain to be a little larger than that given in the table, as steam condensed in a steam jacket yields less heat than that passed through the cylinder.

It is very doubtful if the gain in fluid efficiency due to increasing steam-pressure above 150 or 200 pounds is not offset by the greater friction and the difficulty of maintaining the engine. Higher pressures than 200 pounds are used only where great power must be developed with small weight and space, as in torpedo-loads.

Condensers. — Two forms of condensers are used to condense the steam from a steam-engine, known as jet-condensers and surface-condensers. The former are commonly used for land engines; they consist of a receptacle having a volume equal to one-fourth or one-third of that of the cylinder or cylinders that exhaust into it, into which the steam passes from the exhaust pipe and where it meets and is condensed by a spray of cold water.

If it be assumed that the steam in the exhaust-pipe is dry and saturated and that it is condensed from the pressure p and cooled to the temperature  $l_k$ , then the heat yielded per pound of steam is  $H = q_k$ 

where H is the total heat of steam at the pressure  $p_i$  and  $q_i$  is the heat of the liquid at the temperature  $\ell_k$ . The heat acquired by each pound of condensing or injection water is

where q' is the heat of the liquid at the temperature l, of the injection-water as it enters the condenser. Each pound of steam will require

$$G = \frac{r+q-q_k}{q_k-q_i} \cdot \cdot \cdot \cdot \cdot \cdot (150)$$

pounds of injection-water.

For example, steam at 4 pounds absolute has for the total heat 1128.6. If the injection-water enters with a temperature of 60° F., and leaves with a temperature of 120° F., then each pound of steam will require

$$\frac{r+q-q_k}{q_k-q_l} = \frac{1128.6-88.0}{88.0-28.12} = 17.3$$

pounds of injection-water. This calculation is used only to aid in determining the size of the pipes and passages leading water to and from the condenser, and the dimensions of the airpump. Anything like refinement is useless and impossible, as conditions are seldom well known and are liable to vary. From 20 to 30 times the weight of steam used by the engine is commonly taken for this purpose.

The jet-condensers cannot be used at sea when the boiler-pressure exceeds 40 pounds by the gauge; all modern steamers are consequently supplied with surface-condensers which consist of receptacles, which are commonly rectangular in shape, into which steam is exhausted, and where it is condensed on horizontal brass tubes through which cold sea-water is circulated. The condensed water is drained out through the air-pump and is returned to the boiler. Thus the feed-water is kept free from salt and other mineral matter that would be pumped into the boiler if a jet-condenser were used, and if the feed-water were drawn from the mingled water and condensed steam from such a condenser. Much trouble is, however, experienced from oil used to lubricate the cylinders of the engine, as it is likely to be pumped into the boilers with the feed-water, even though attempts are made to strain or filter it from the water.

The water withdrawn from a surface-condenser is likely to

have a different temperature from the cooling water when it leaves the condenser. If its temperature is  $t_1$ , then we have instead of equation (150)

$$G = \frac{r+q-q_1}{q_k-q_i}$$
. . . . . (151)

for the cooling water per pound of steam. The difference is really immaterial, as it makes little difference in the actual value of G for any case.

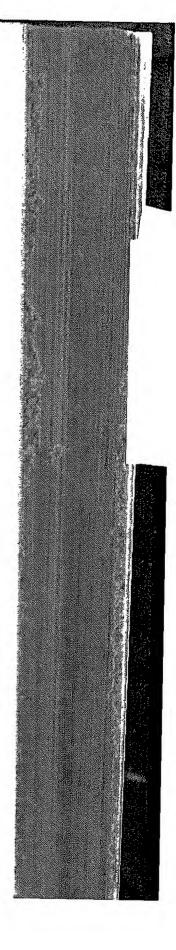
Cooling Surface. — Experiments on the quantity of cooling surface required by a surface-condenser are few and unsatisfactory, and a comparison of condensers of marine engines shows a wide diversity of practice. Seaton says that with an initial temperature of 60°, and with 120° for the feed-water, a condensation of 13 pounds of steam per square foot per hour is considered fair work. A new condenser in good condition may condense much more steam per square foot per hour than his, but allowance must be made for fouling and clogging, especially for vessels that make long voyages.

Seaton also gives the following table of square feet of cooling arface per indicated horse-power:

Absolute Terminal Pressure, Pounds per Square Ingli.										Square Feet per I. II. P.				
	30										1.17			
	15						•				1.57			
•	125										1.50			
	10	,	,	,			,				1.43			
	8		٠								1.37			
	6										1.30			

For ships stationed in the tropics, allow 20 per cent more; or ships which occasionally visit the tropics, allow 10 per cent more; for ships constantly in a cold climate, 10 per cent less may be allowed.

Air-Pump. — The vacuum in the condenser is maintained y the air-pump, which pumps out the air which finds its way here by leakage or otherwise; the condensing water carries



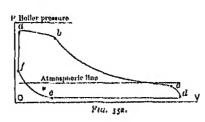
a considerable volume of air into the condenser, and the s of the air-pump can be based roughly on the average percents of air held in solution in water; the air which finds its way is a surface-condenser enters mainly by leakage around the le pressure piston-rod and elsewhere.

It is customary to base the size of the air-pump on the  $\epsilon$  placement of the low-pressure piston (or pistons); for example the capacity of a single-acting vertical air-pump for a merch steamer, with triple-expansion engines, may be about  $\frac{1}{10}$  of capacity of the low-pressure cylinder.

With the introduction of steam-turbines, the importance a good vacuum becomes more marked, and the duty of the pump, which commonly removes air and also the water of c densation from the condenser, is divided between a dry pump, which removes air from the condenser, and a wapump, which removes the water of condensation. Air-pur are treated more at length on page 374, in connection with discussion of compressed air.

Designing Engines. — The only question that is propodiscussed here is the probable form of the indicator-diagraphich gives immediately the method of finding the mean effect pressure, and, consequently, the size of the cylinder of the eng

The most reliable way of finding the expected mean effect pressure in the design of a new engine is to measure an indicat diagram from an engine of the same or similar type and stand working under the same conditions.



If a new engine varies much from the type on what the design is based that diagram from the latter car be used directly, the follow method may be used to a for moderate changes of he pressure or expansion.

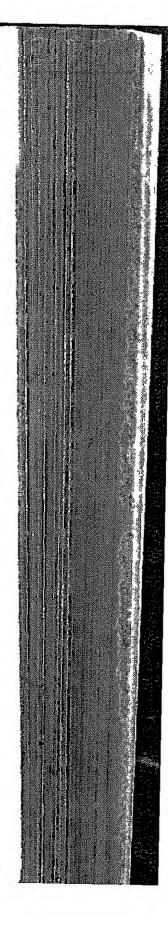
type diagram either on the original card or redrawn to a la scale, may have added to it the axis of zero pressure and

the atmospheric line and at a distance to represent the pressure of the atmosphere, using the scale for measuring pressure on the diagram. The latter is drawn vertical and at a distance from af which shall bear the same ratio to the length of the diagram as the clearance space of the cylinder has to the piston-displacement. The boiler-pressure line may be drawn as shown. The absolute pressure may now be measured from OV with the proper cale and volume from OP with any convenient scale.

Choosing points b and c at the beginning and end of expansion determine the exponent for an exponential equation by the nethod on page 66; do the same for the compression curve ef.

Draw a diagram like Fig. 35 for the new engine, making the proper allowance for change of boiler-pressure or point of cutoff, using the probable clearance for determining the position of the line af. Allowing for loss of pressure from the boiler to the cylinder, and for wire-drawing or loss of pressure in the valves and passages, locate the points a and b. The back-pressure line de can be drawn from an estimate of the probable vacuum. The volumes at c and e are determined by the action of the valve gear. By aid of the proper exponential equations ocate a few points on be and ef and sketch in those curves. Finish the diagram by hand by comparison with the type diagram. If necessary draw two such diagrams for the head and crank ends of the cylinder. The mean effective pressure can now be determined by aid of the planimeter and used in the design of the new engine.

Usually the refinements of the method just detailed are avoided, and an allowance is made for them in the lump by a practical factor. The following approximations are made: (1) the pressure in the cylinder during admission is assumed to be the boiler pressure, and during the exhaust the vacuum in the condenser; (2) the release is taken to be at the end of the stroke; (3) both expansion and compression lines are treated as hyperbolæ. The mean effective pressure is then readily computed as indicated in the following example.



**Problem.** — Required the dimensions of the cylinder of an engine to give 200 horse-power; revolutions 100; gauge pressure 80 pounds; vacuum 28 inches; cut-off at  $\frac{1}{4}$  stroke; release at end of stroke; compression at  $\frac{1}{10}$  stroke; clearance 5 per cent.

The absolute boiler-pressure is 94.7 pounds, and the absolute pressure corresponding to 28 inches of mercury is nearly one pound. It is convenient to take the piston displacement as one cubic foot and the stroke as one foot for the purpose of determining the mean effective pressure. The volume of cut-off is consequently \(\frac{1}{2}\) cubic foot due to the motion of the piston plus \(\frac{1}{10}\) cubic foot due to the clearance or 0.35 cubic foot; the volume at release is 1.05 cubic foot, and at compression is 0.15 cubic foot.

The work during admission (corresponding to ab, Fig. 35a) is  $04.7 \times 144 \times 0.35$  foot-pound,

and during expansion is

$$p_1 v_1 \log_e \frac{v_2}{v_1} = 94.7 \times 1.14 \times 0.35 \log_e \frac{1.05}{0.35}$$

The work during exhaust done by the piston in expelling the steam is

$$1 \times 144 \times (1 - 0.15),$$

and the work during compression is

$$1 \times 144 \times 0.15 \log_{e} \frac{0.15}{0.05}$$

The mean effective pressure in pounds per square inch is obtained by adding the first two works and subtracting the last two and then dividing by 144, so that

M.E.P. = 
$$94.7 \times 0.25 + 94.7 \times 0.35 \log_6 \frac{1.05}{0.35}$$
  
-  $1 \times 0.85 - 1 \times 0.15 \log_6 \frac{0.15}{0.05} = 59.1$ .

The probable mean effective pressure may be taken as  $r_{\sigma}$  of this computed pressure, or 53.2 pounds per square inch.

Given the diameter and stroke of an engine together with the mean effective pressure, and revolutions, we may find the horsepower by the formula

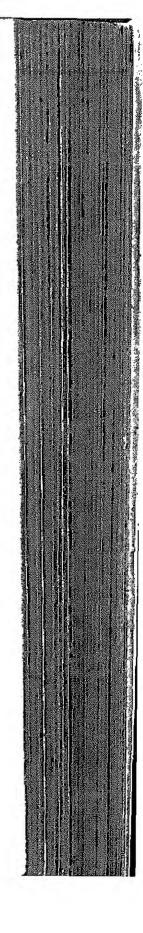
I.H.P. = 
$$\frac{2 \ plan}{33000}$$

where p is the mean effective pressure, l is the stroke in feet, a is the area of the circle for the given diameter in square inches, and n is the number of revolutions per minute. For our case we may assume that the stroke is twice the diameter, whence

$$200 = \frac{2 \times 53.2 \times \frac{2d}{12} \times \frac{\pi d^3}{4} \times 100}{33000}.$$

:. 
$$d = 16.8$$
 inches,  $s = 33.6$  inches.

In practice the diameter would probably be made 162 inches and the stroke 332 inches.



## CHAPTER IX.

## COMPOUND ENGINES.

A COMPOUND engine has commonly two cylinders, one of which is three or four times as large as the other. Steam from a boiler is admitted to the small cylinder, and after doing work in that cylinder it is transferred to the large cylinder, from which it is exhausted, after doing work again, into a condenser or against the pressure of the atmosphere. If we assume that the steam from the small cylinder is exhausted into a large receiver, the back-pressure in that cylinder and the pressure during the admission to the large cylinder will be uniform. If, further, we assume that there is no clearance in either cylinder, that the back-pressure in the small cylinder and the forward pressure in the large cylinder are the same, and that the expansion in the small cylinder reduces the pressure down to the back-pressure in that cylinder, the diagram for the small cylinder will be ABCD,

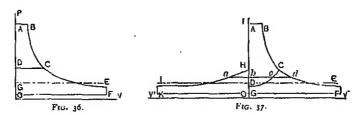


Fig. 36, and for the large cylinder DCFG. The volume in the large cylinder at cut-off is equal to the total volume of the small cylinder, since the large cylinder takes from the receiver the same weight of steam that is exhausted by the small cylinder, and, in this case, at the same pressure.

The case just discussed is one extreme. The other extreme occurs when the small cylinder exhausts directly into the large

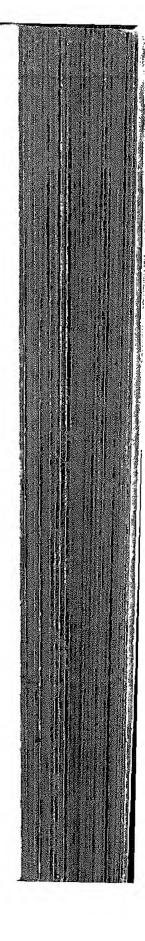
cylinder without an intermediate receiver. In such engines the pistons must begin and end their strokes together. They may both act on the beam of a beam engine, or they may act on one crank or on two cranks opposite each other.

For such an engine, ABCD, Fig. 37, is the diagram for the small cylinder. The steam line and expansion line AB and BC are like those of a simple engine. When the piston of the small cylinder begins the return stroke, communication is opened with the large cylinder, and the steam passes from one to the other, and expands to the amount of the difference of the volume, it being assumed that the communication remains open to the end of the stroke. The back-pressure line CD for the small cylinder, and the admission line HI for the large cylinder, gradually fall on account of this expansion. The diagram for the large cylinder is HIKG, which is turned toward the left for convenience.

To combine the two diagrams, draw the line abcd, parallel to V'OV, and from b lay off bd equal to ca; then d is one point of the expansion curve of the combined diagram. The point C corresponds with H, and E, corresponding with I, is as far to the right as I is to the left.

For a non-conducting cylinder, the combined diagram for a compound engine, whether with or without a receiver, is the same as that for a simple engine which has a cylinder the same size as the large cylinder of the compound engine, and which takes at each stroke the same volume of steam as the small cylinder, and at the same pressure. The only advantage gained by the addition of the small cylinder to such an engine is a more even distribution of work during the stroke, and a smaller initial stress on the crank-pin.

Compound engines may be divided into two classes—those with a receiver and those without a receiver; the latter are called "Woolf engines" on the continent of Europe. Engines without a receiver must have the pistons begin and end their strokes at the same time; they may act on the same crank or on cranks 180° apart. The pistons of a receiver compound engine may make strokes in any order. A form of receiver compound engine with

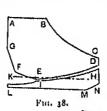


two cylinders, commonly used in marine work, has the cranks a 90° to give handiness and certainty of action. Large marinengines have been made with one small cylinder and two large or low-pressure cylinders, both of which draw steam from the receiver and exhaust to the condenser. Such engines usual have the cranks at 120°, though other arrangements have been made.

Nearly all compound engines have a receiver, or a spa between the cylinders corresponding to one, and in no case the receiver of sufficient size to entirely prevent fluctuations pressure. In the later marine work the receiver has been masmall, and frequently the steam-chests and connecting pipes ha been allowed to fulfil that function. This contraction of sl involves greater fluctuations of pressure, but for other reasons appears to be favorable to economy.

Under proper conditions there is a gain from using a corpound engine instead of a simple engine, which may amount ten per cent or more. This gain is to be attributed to the divisi of the change of temperature from that of the steam at admissi to that of exhaust into two stages, so that there is less fluction of temperature in a cylinder and consequently less into change of heat between the steam and the walls of the cylind

Compound Engine without Receiver. — The indicator-cl grams from a compound engine without a receiver are rep:



sented by Fig. 38. The steam line and expassion line of the small cylinder, AB and BC, not differ from those of a simple engine. At the exhaust opens, and the steam sudder expands into the space between the cylindrand the clearance of the large cylinder, and the pressure falls from C to D. During the return of the large cylinder, and the cylindrane falls from C to D.

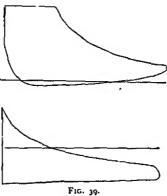
stroke the volume in the large cylinder increases more rapic than that of the small cylinder decreases, so that the back-pre ure line DE gradually falls, as does also the admission line i of the large cylinder, the difference between these two lines be: due to the resistance to the flow of steam from one to the oth

At E the communication between the two cylinders is closed by the cut-off of the large cylinder; the steam is then compressed in the small cylinder and the space between the two cylinders to F, at which the exhaust of the small cylinder closes; and the remainder of the diagram FGA is like that of a simple engine. From I, the point of cut-off of the large cylinder, the remainder of the diagram IKLMNH is like the same part of the diagram of a simple engine.

The difference between the lines ED and HI and the "drop" CD at the end of the stroke of the small piston indicate waste or losses of efficiency. The compression EFG and the accompanying independent expansion IK in the large cylinder show a loss of power when compared with a diagram like Fig. 37 for an engine which has no clearance or intermediate space; but compression is required to fill waste spaces with steam. The compression EF is required to reduce the drop CD, and the compression FG fills the clearance in anticipation of the next supply from

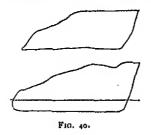
the boiler. Neither compression is complete in Fig. 38.

Diagrams from a pumping engine at Lawrence, Massachusetts, are shown by Fig. 39. rounding of corners due to the indicator makes it difficult to determine the location of points like D, E, F, and I on Fig. 38. The low-pressure diagram is taken with a weak spring, and so has an exaggerated height.



Compound Engine with Receiver. — It has already been pointed out that some receiver space is required if the cranks of a compound engine are to be placed at right angles. When the receiver space is small, as on most marine engines, the fluctuations of pressure in the receiver are very notable. This is exhibited by the diagrams in Fig. 40, which were taken from a yacht engine. An intelligent conception of the causes and meaning

of such fluctuations can be best obtained by constructing ideal diagrams for special cases, as explained on page 164.



Triple and Quadruple Expansion-Engines. — The same influences which introduced the compound engines, when the common steam-pressure changed from forty to eighty pounds to the square inch, have brought in the successive expansion through three cylinders (the high-pressure, intermediate, and

low-pressure cylinders) now that 150 to 200 pounds pressure are employed. Just as three or more cylinders are combined in various ways for compound engines, so four, five, or six cylinders have been arranged in various manners for triple-expansion engines; the customary arrangement has three cylinders with the cranks at 180°.

Quadruple engines with four successive expansions have been employed with high-pressure steam, but with the advisable pressures for present use the extra complication and friction make it a doubtful expedient.

Total Expansion. - In Figs. 36 and 37, representing the diagrams for compound engines without clearance and without drop between the cylinders, the total expansion is the ratio of the volumes at E and at B; that is, of the low-pressure piston displacement to the displacement developed by the high-pressure piston at cut-off. The same ratio is called the total or equivalent expansion for any compound engine, though it may have both clearance and drop. Such a conventional total expansion is commonly given for compound and multiple-expansion engines, and is a convenience because it is roughly equal to the ratio of the initial and terminal pressures; that is, of the pressure at cut-off in the high-pressure cylinder and at release in the lowpressure cylinder. It has no real significance, and is not equivalent to the expansion in the cylinder of a simple engine, by which we mean the ratio of the volume at release to that at cut-off, taking account of clearance. And further, since the clearance of the high- and the low-pressure cylinders are different there can be no real equivalent expansion.

If the ratio of the cylinders is R and the cut-off of the high-pressure cylinder is at  $\frac{1}{e}$  of the stroke, then the total expansion is represented by

$$E = eE$$

and

$$\frac{1}{e} = R \div E.$$

This last equation is useful in determining approximately the cut-off of the high-pressure cylinder.

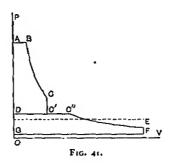
For example, if the initial pressure is 100 pounds absolute and the terminal pressure is to be 10 pounds absolute, then the total expansions will be about 10. If the ratio of the cylinders is 3½, then the high-pressure cut-off will be about

$$\frac{1}{e} = 3\frac{1}{2} \div 10 = 0.35$$

of the stroke.

Low-pressure Cut-off. — The cut-off of the low-pressure cylinders in Figs. 36 and 37 is controlled by the ratio of the cylinders, since the volumes in the low-pressure cylinder at cut-off is in each case made equal to the high-pressure piston displacement; this is done to avoid a drop. If the cut-off were lengthened there would be a loss of pressure or drop at the end

of the stroke of the high-pressure piston, as is shown by Fig. 41, for an engine with a large receiver and no clearance. Such a drop will have some effect on the character of the expansion line C"F of the low-pressure cylinder, both for a non-conducting and for the actual engine with or without a clearance. Its principal effect will, however, be on



the distribution of work between the cylinders; for it is evident that if the cut-off of the low-pressure cylinder is shortened the

pressure at C'' will be increased because the same weight of steam is taken in a smaller volume. The back-pressure DC' of the high-pressure cylinder will be raised and the work will be diminished; while the forward pressure DC'' of the low-pressure cylinder will be raised, increasing the work in that cylinder.

Ratio of Cylinders. — In designing compound engines, more especially for marine work, it is deemed important for the smooth action of the engine that the total work shall be evenly distributed upon the several cranks of the engines, and that the maximum pressure on each of the cranks shall be the same, and shall not be excessive. In case two or more pistons act on one crank, the total work and the resultant pressure on those pistons are to be considered; but more commonly each piston acts on a separate crank, and then the work and pressure on the several pistons are to be considered.

In practice both the ratio of the cylinders and the total expansions are assumed, and then the distribution of work and the maximum loads on the crank-pins are calculated, allowing for clearance and compression. Designers of engines usually have a sufficient number of good examples at hand to enable them to assume these data. In default of such data it may be necessary to assume proportions, to make preliminary calculations, and to revise the proportions till satisfactory results are obtained. For compound engines using 80 pounds steam-pressure the ratio is 1:3 or 1:4. For triple-expansion engines the cylinders may be made to increase in the ratio 1:2 or 1:2.

Approximate Indicator-Diagrams.—The indicator-diagrams from some compound and multiple-expansion engines are irregular and apparently erratic, depending on the sequence of the cranks, the action of the valves, and the relative volumes of the cylinders and the receiver spaces. A good idea of the effects and relations of these several influences can be obtained by making approximate calculations of pressures at the proper parts of the diagrams by a method which will now be illustrated.

For such a calculation it will be assumed that all expansion

lines are rectangular hyperbolæ, and in general that any change of volume will cause the pressure to change inversely as the volume. Further, it will be assumed that when communication is opened between two volumes where the pressures are different, the resultant pressure may be calculated by adding together the products of each volume by its pressure, and dividing by the sum of the volumes. Thus if the pressure in a cylinder having the volume  $v_o$  is  $p_o$ , and if the pressure is  $p_r$  in a receiver where the volume is  $v_r$ , then after the valve opens communication from the cylinder to the receiver the pressure will be

$$p = \frac{p_c v_c + p_r v_r}{v_c + v_r} \cdot$$

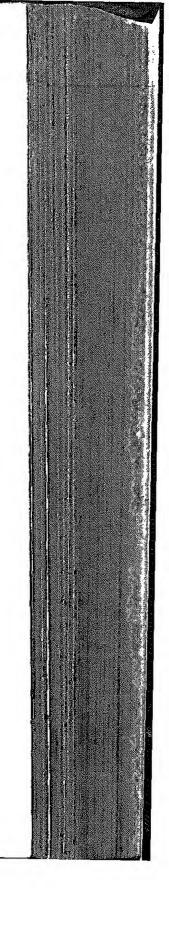
The same method will be used when three volumes are put into communication.

It will be assumed that there are no losses of pressure due to throttling or wire-drawing; thus the steam line for the high-pressure cylinder will be drawn at the full boiler-pressure, and the back-pressure line in the low-pressure cylinder will be drawn to correspond with the vacuum in the condenser. Again, cylinders and receiver spaces in communication will be assumed to have the same pressure.

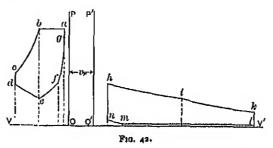
For sake of simplicity the motions of pistons will be assumed to be harmonic.

Diagrams constructed in this way will never be realized in any engine; the degree of discrepancy will depend on the type of engine and the speed of rotation. For slow-speed pumping-engines the discrepancy is small and all irregularities are easily accounted for. On the other hand the discrepancies are large for high-speed marine-engines, and for compound locomotives they almost prevent the recognition of the events of the stroke.

Direct-expansion Engine. — If the two pistons of a compound engine move together or in opposite directions the diagrams are like those shown by Fig. 42. Steam is admitted to the high-pressure cylinder from a to b; cut-off occurs at b, and bc represents expansion to the end of the stroke; bc being a rectangular



hyperbola referred to the axes OV and OP, from which a, b, c are laid off to represent absolute pressures and volumes, incling clearance.



At the end of the stroke release from the high-pres cylinder and admission to the low-pressure cylinder are assu to take place, so that communication is opened from the 1 pressure cylinder through the receiver space into the low-p ure cylinder. As a consequence the pressure falls from  $e^{-t}$  and rises from n to h in the low-pressure cylinder. The O'P' is drawn at a distance from OP, which corresponds to volume of the receiver space, and the low-pressure diagra referred to O'P' and O'V' as axes.

The communication between the cylinders is maintained cut-off occurs at i for the low-pressure cylinder. The line and hi represent the transfer of steam from the high-pre to the low-pressure cylinder, together with the expansion define increased size of the large cylinder. After the cut-off the large cylinder is shut off from the receiver, and the steat it expands to the end of the stroke. The back-pressure compression lines for that cylinder are not affected by competing, and are like those of a simple engine. Meanwhile the piston compresses steam into the receiver, as represente ef, till compression occurs, after which compression into clearance space is represented by fg. The expansion and pression lines ik and mn are drawn as hyperbolic referred axes O'P' and O'V'. The compression line ef is drawn as an i bola referred to O'V and O'P', while fg is referred to OV and

In Fig. 42 the two diagrams are drawn with the same scale for volume and pressure, and are placed so as to show to the eye the relations of the diagrams to each other. Diagrams taken from such an engine resemble those of Fig. 30, which have the same length, and different vertical scales depending on the springs used in the indicators.

Some engines have only one valve to give release and compression for the high-pressure cylinder and admission and cut off for the low-pressure cylinder. In such case there is no receiver space, and the points v and f coincide.

When the receiver is closed by the compression of the highpressure cylinder it is filled with steam with the pressure represented by f. It is assumed that the pressure in the receiver remains unchanged till the receiver is opened at the end of the stroke. It is evident that the drop ed may be reduced by short ening the cut-off of the low-pressure cylinder so as to give more compression from e to f and consequently a higher pressure at f when the receiver is closed.

Representing the pressure and volume at the several points by p and v with appropriate subscript letters, and representing the volume of the receiver by  $v_r$ , we have the following equations:

```
\begin{aligned} p_a &= p_b = \text{initial pressure;} \\ p_l &= p_m = \text{back-pressure;} \\ p_o &= p_b v_b + v_c; \\ p_n &= p_m v_m + v_n; \\ p_d &= p_h = (p_c v_o + p_n v_n + p_r v_r) + (v_o + v_n + v_r); \\ p_o &= p_l = p_d (v_o + v_n + v_r) + (v_o + v_l + v_r); \\ p_f &= p_o (v_o + v_r) + (v_f + v_r); \\ p_t &= p_l v_f + v_g; \\ p_k &= p_l v_l + v_k. \end{aligned}
```

The pressures  $p_0$  and  $p_n$  can be calculated directly. Then the equations for  $p_{di}$ ,  $p_{di}$ , and  $p_f$  form a set of three simultaneous equations with three unknown quantities, which can be easily solved. Finally,  $p_g$  and  $p_k$  may be calculated directly.

For example, let us find the approximate diagram for a direct-expansion engine which has the low-pressure piston displacement equal to three times the high-pressure piston displacement. Assume that the receiver space is half the smaller piston displacement, and that the clearance for each cylinder is one-tenth of the corresponding piston displacement. Let the cut-off for each cylinder be at half-stroke, and the compression at nine-tenths of the stroke; let the admission and release be at the end of the stroke. Let the initial pressure be 65.3 pounds by the gauge or 80 pounds absolute, and let the back-pressure be two pounds absolute.

If the volume of the high-pressure piston displacement be taken as unity, then the several required volumes are:

$$v_b = 0.5 + 0.1 = 0.6$$
  $v_h = v_n = 3 \times 0.1 = 0.3$   $v_c = v_d = 1.0 + 0.1 = 1.1 \cdot v_l = 3 (0.5 + 0.1) = 1.8$   $v_b = 0.5 + 0.1 = 0.6$   $v_k = v_l = 3 (1.0 + 0.1) = 3.3$   $v_f = 0.1 + 0.1 = 0.2$   $v_m = 3 (0.1 + 0.1) = 0.6$   $v_r = 0.5$ 

The pressures may be calculated as follows:

$$p_{a} = p_{b} = 80; \quad p_{l} = p_{m} = 2;$$

$$p_{c} = p_{b}v_{b} \div v_{o} = 80 \times 0.6 \div 1.1 = 43.6;$$

$$p_{n} = p_{m}v_{m} \div v_{n} = 2 \times 0.6 \div 0.3 = 4;$$

$$p_{e} = p_{d} (v_{c} + v_{n} + v_{r}) \div (v_{e} + v_{l} + v_{r}) = p_{d} (1.1 \div 0.3 \div 0.5)$$

$$\div (0.6 \div 1.8 \div 0.5) = 0.655 p_{d};$$

$$p_{f} = p_{e} (v_{e} + v_{r}) \div (v_{f} + v_{r}) = p_{e} (0.6 \div 0.5) + (0.2 \div 0.5)$$

$$= 1.57 p_{e} = 1.57 \times 0.655 p_{d} = 1.03 p_{d};$$

$$p_{d} = (p_{c}v_{c} + p_{n}v_{n} + p_{f}v_{r}) \div (v_{e} + v_{n} + v_{r})$$

$$= (80 \times 0.6 + 4 \times 0.3 \div 0.5 p_{f}) \div (0.6 \div 0.3 \div 0.5)$$

$$= 25.89 \div 0.26 p_{f};$$

$$p_{d} = 25.89 \div 0.26 \times 1.03 p_{d}; \quad p_{d} = 35.36;$$

$$p_{e} = p_{t} = 0.655 p_{d} = 0.655 \times 35.36 = 23.2;$$

$$p_{f} = 1.03 p_{d} = 1.03 \times 35.36 = 36.5;$$

$$p_{g} = p_{f}v_{f} + v_{g} = 36.5 \times 0.2 \div 0.1 = 73;$$

$$p_{k} = p_{i}v_{i} \div v_{k} = 23.2 \times 1.8 \div 3.3 = 12.6.$$



As the pressures and volumes are now known the diagrams of Fig. 42 may be drawn to scale. Or, if preferred, diagrams like Fig. 39 may be drawn, making them of the same length and using convenient vertical scales of pressure. If the engine runs slowly and has abundant valves and passages the diagrams thus obtained will be very nearly like those taken from the engine by indicators. If losses of pressure in valves and passages are allowed for, a closer approximation can be made.

The mean effective pressures of the diagrams may be readily obtained by the aid of a planimeter, and may be used for estimating the power of the engine. For this purpose we should either use the modified diagrams allowing for losses of pressure, or we should affect the mean effective pressures by a multiplier obtained by comparison of the approximate with the actual diagrams from engines of the same type. For a slow-speed pumping-engine the multiplier may be as large as 0.9 or even more; for high-speed engines it may be as small as 0.6.

The mean effective pressures of the diagrams may be calculated from the volumes and pressures if desired, assuming, of course, that the several expansion and compression curves are hyperbolæ. The process can be best explained by applying it to the example already considered. Begin by finding the mean pressure during the transfer of steam from the high-pressure cylinder to the low-pressure cylinder as represented by de and hi. The net effective work during the transfer is

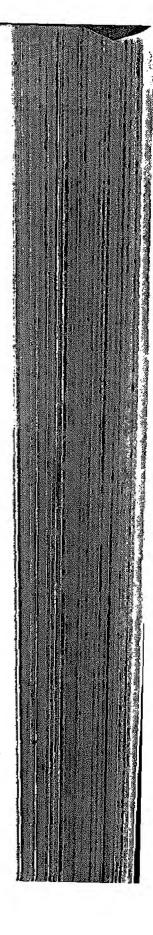
$$\int p dv = p_1 v_1 \log_e \frac{v_2}{v_1} = 144 p_d (v_d + v_h + v_r) \log_e \frac{v_e + v_1 + v_r}{v_d + v_h + v_r}$$

$$= 144 \times 35.4 (1.1 + 0.3 + 0.5) \log_e \frac{0.6 + 1.8 + 0.5}{1.1 + 0.3 + 0.5}$$

$$= 4120 \text{ foot-pounds}$$

for each cubic foot of displacement of the high-pressure piston. This corresponds with our previous assumption of unity for the displacement of that piston. The increase of volume is

$$v_e + v_i + v_r - (v_d + v_h + v_r) = 0.6 + 1.8 + 0.5 - (1.1 + 0.3 + 0.5) = 1$$
;



so that the mean pressure during the transfer is

$$4120 + 1 \times 144 = 28.6 = p_x$$

pounds per square inch, which acts on both the high- and the low-pressure pistons.

The effective work for the small cylinder is obtained by adding the works under ab and be and subtracting the works under de, ef, and fg. So that

$$WH = 1.1.1 \left\{ p_a \left( v - v_a \right) + p_b v_b \log_b \frac{v_e}{v_b} - p_a \left( v_d - v_e \right) \right.$$

$$\left. - p_e \left( v_e + v_r \right) \log_e \frac{v_e + v_r}{v_f + v_r} - p_f v_f \log_e \frac{v_f}{v_e} \right\}$$

$$= 144 \left\{ 80 \left( 0.6 - 0.1 \right) + 80 \times 0.6 \log_e \frac{1.1}{0.6} - 28.6 \left( 1.1 - 0.6 \right) \right.$$

$$\left. - 23.2 \left( 0.6 + 0.5 \right) \log_e \frac{0.6 + 0.5}{0.2 + 0.5} - 36.5 \times 0.2 \log_e \frac{0.2}{0.1} \right\}$$

$$= 144 \times 33.26 = 4789 \text{ foot-pounds.}$$

This is the work for each cubic foot of the high-pressure piston displacement, and the mean effective pressure on the small piston is evidently 33.26 pounds per square inch.

In a like manner the work of the large piston is

$$WL = 144 \left\{ p_{\bullet}(v_{i} - v_{h}) + p_{i}v_{i}\log_{e}\frac{v_{h}}{v_{i}} - p_{i}(v_{i} - v_{m}) - p_{m}v_{m}\log_{e}\frac{v_{m}}{v_{h}} \right\}$$

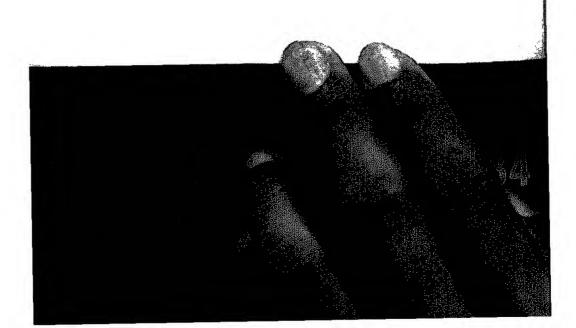
$$= 144 \left\{ 28.6 \left( 1.8 - 0.3 \right) + 23.2 \times 1.8 \log_{e}\frac{3.3}{1.8} - 2 \left( 3.3 - 0.6 \right) - 2 \times 0.6 \log_{e}\frac{0.6}{0.3} \right\} = 144 \times 61.92 = 8916 \text{ fool-pounds.}$$

Since the ratio of the piston displacements is 3, the work for each cubic foot of the low-pressure piston displacement is one-third of the work just calculated; and the mean effective pressure on the large piston is

$$61.92 + 3 = 20.64$$

pounds per square inch.

The proportions given in the example lead to a very uneven distribution of work; that of the large cylinder being nearly twice as much as is developed in the small cylinder. The dis-

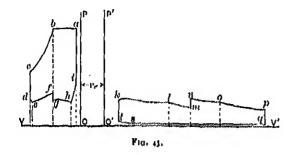


tribution can be improved by lengthening the cut-off of the large cylinder, or by changing the proportions of the engine.

As has already been pointed out, the works just calculated and the corresponding mean effective pressures are in excess of those that will be actually developed, and must be affected by multipliers which may vary from 0.6 to 0.9, depending on the type and speed of the engine.

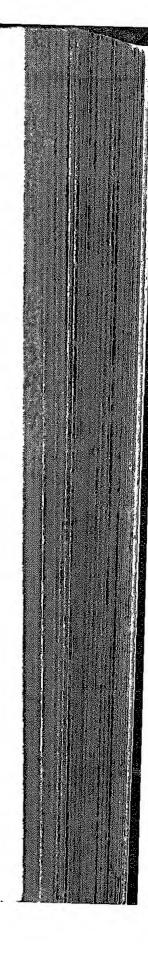
Cross-compound Engine. — A two-cylinder compound engine with pistons connected to cranks at right angles with each other is frequently called a cross-compound engine. Unless a large receiver is placed between the cylinders the pressure in the space between the cylinders will vary widely.

Two cases arise in the discussion of this engine according as



he cut-off of the large cylinder is carlier or later than half-stroke; n the latter case there is a species of double admission to the ow-pressure cylinder, as is shown in Fig. 43. For sake of implicity the release, and also the admission for each cylinder, s assumed to be at the end of the stroke. If the release is early he double admission occurs before half-stroke,

The admission and expansion of steam for the high-pressure ylinder are represented by ab and bc. At c release occurs, outling the small cylinder in communication with the internediate receiver, which is then open to the large cylinder. There is a drop at cd and a corresponding rise of pressure mn on the large piston, which is then at half-stroke; it will be assumed that the pressures at d and at n are identical. From d to c the



steam is transferred from the small to the large cylinder, and the pressure falls because the volume increases; no is the corresponding line on the low-pressure diagram. The cut-off at o for the large cylinder interrupts this transfer, and steam is then compressed by the small piston into the intermediate receiver with a rise of pressure as represented by cf. The admission to the large cylinder, tk, occurs when the small piston is at the middle of its stroke, and causes a drop, fg, in the small cylinder. From g to h steam is transferred through the receiver from the small to the large cylinder. The pressure rises at first because the small piston moves rapidly while the large one moves slowly until its crank gets away from the dead-point; afterwards the pressure falls. The line kl represents this action on the lowpressure diagram. At h compression occurs for the small cylinder, and hi shows the rise of pressure due to compression. For the large cylinder the line *lm* represents the supply of steam from the receiver, with falling pressure which lasts till the double admission at mn occurs.

The expansion, release, exhaust, and compression in the large cylinder are not affected by compounding.

Strictly, the two parts of the diagram for the low-pressure cylinder, mnopq and stklm, belong to opposite ends of the cylinder, one belonging to the head end and one to the crank end. With harmonic motion the diagrams from the two ends are identical, and no confusion need arise from our neglect to determine which end of the large cylinder we are dealing with at any time. Such an analysis for the two ends of the cylinder, taking account of the irregularity due to the action of the connecting-rod, would lead to a complexity that would be unprofitable.

A ready way of finding corresponding positions of two pistons connected to cranks at right angles with each other is by aid of the diagram of Fig. 44. Let O be the centre of the crankshaft and  $pR_{\nu}R_{x}q$  be the path of the crank-pin. When one piston has the displacement py and its crank is at  $OR_{\nu}$ , the other crank may be 90° ahead at  $OR_{x}$  and the corresponding piston displacement will be px. The same construction may be used if the

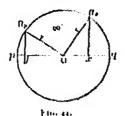


crank is 90° behind or if the angle RyORx is other than a right The actual piston position and crank angles when

affected by the irregularity due to the connecting-rod will differ from those found by this method, but the positions found by such a diagram will represent the average positions very nearly.

The several pressures may be found as





$$\begin{aligned} p_b &= p_a = \text{initial pressure}; \\ p_s &= p_q = \text{back-pressure}; \\ p_c &= p_b v_b + v_c; \\ p_t &= p_t v_s + v_t; \\ p_d &= p_n = \{p_c v_c + p_m (v_m + v_r)\} \rightarrow (v_c + v_s + v_r); \\ p_s &= p_o = p_d (v_c + v_m + v_r) \rightarrow (v_s + v_s + v_r); \\ p_f &= p_o (v_o + v_r) \rightarrow (v_f + v_r); \\ p_\theta &= p_k = \{p_f (v_f + v_r) + p_t v_t + (v_f + v_t + v_r); \\ p_h &= p_t = p_\theta (v_f + v_t + v_r) + (v_h + v_t + v_r); \\ p_m &= p_t (v_t + v_r) \rightarrow (v_m + v_r); \\ p_t &= p_h v_h \rightarrow v_t; \\ p_p &= p_o v_o \rightarrow v_p. \end{aligned}$$

The pressures  $p_e$  and  $p_n$  can be found directly from the initial pressure and the back-pressure, and finally the last two equations give direct calculations for  $p_i$  and  $p_n$  so soon as  $p_k$  and  $p_n$ are found. There remain six equations containing six unknown quantities, which can be readily solved after numerical values are assigned to the known pressures and to all the volumes.

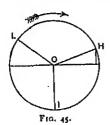
The expansion and compression lines, be and hi, for the high pressure diagrams are hyperbolic referred to the axes O1' and OP; and in like manner the expansion and compression lines op and st, for the low-pressure diagram, are hyperbolic referred to O'V' and O'P'. The curve of is an hyperbola referred to O'V' and O'P', and the curve Im is an hyperbola referred to OF' and OP. The transfer lines de and no, gh and M, are not hyper bole. They may be plotted point by point by finding corresponding intermediate piston positions,  $p_x$  and  $p_y$ , by aid of Fig. 44, and then calculating the pressure for these positions by the equation

$$p_x = p_y = p_d (v_d + v_m + v_r) + (v_x + v_y + v_r).$$

The work and mean effective pressure may be calculated in a manner similar to that given for the direct-expansion engine; but the calculation is tedious, and involves two transfers, de and no, and gh and kl. The first involves only an expansion, and presents no special difficulty; the second consists of a compression and an expansion, which can be dealt with most conveniently by a graphical construction. All things considered, it is better to plot the diagrams to scale and determine the areas and mean effective pressures by aid of a planimeter.

If the cut-off of the low-pressure is earlier than half-stroke so as to precede the release of the high-pressure cylinder the transfer represented by de and no, Fig. 43, does not occur. Instead there is a compression from d to f and an expansion from l to m. The number of unknown quantities and the number of equations are reduced. On the other hand, a release before the end of the stroke of the high-pressure piston requires an additional unknown quantity and one more equation.

Triple Engines. — The diagrams from triple and other multiple-expansion engines are likely to show much irregularity, the



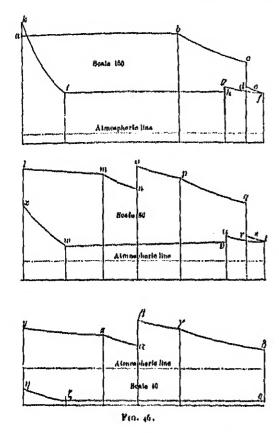
form depending on the number and arrangement of the cylinders and the sequence of the cranks. A common arrangement for a triple engine is to have three pistons acting on cranks set equidistant around the circle, as shown by Fig. 45. Two cases arise depending on the sequence of the cranks, which may be in the order, from one end of the engine, of

high-pressure, low-pressure, and intermediate, as shown by Fig. 45; or in the order of high-pressure, intermediate, and low-pressure.

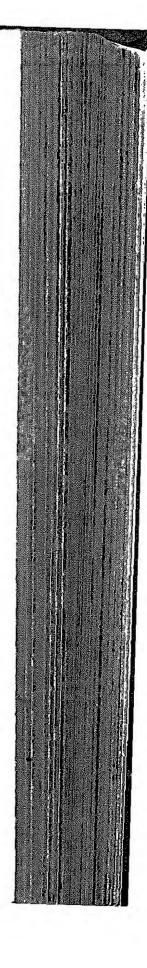
With the cranks in the order, high-pressure, low-pressure, and



intermediate, as shown by Fig. 45, the diagrams are like those given by Fig. 46. The admission and expansion for the high-pressure cylinder are represented by abc. When the high-pressure piston is at release, its crank is at II, Fig. 45, and the intermediate crank is at I, so that the intermediate piston is near half-stroke. If the cut-off for that cylinder is later than



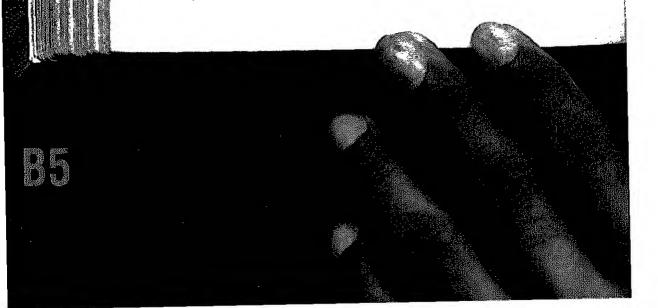
half-stroke, it is in communication with the first receiver when its crank is at *I*, and steam may pass through the first receiver from the high-pressure to the intermediate cylinder, and there is a drop *cd*, and a corresponding rise of pressure *no* in the intermediate cylinder. The transfer continues till cut-off for the



intermediate cylinder occurs at p, corresponding to the piston position e for the high-pressure cylinder. From the position e the high-pressure piston moves to the end of the stroke at f. causing an expansion, and then starts to return, causing the compression fg. When the high-pressure piston is at g the intermediate cylinder takes steam at the other end, causing the drop gh and the rise of pressure xl. Then follows a transfer of steam from the high-pressure to the intermediate cylinder represented by hi and lm. At i the high-pressure compression ik begins, and is carried so far as to produce a loop at k. After compression for the high-pressure cylinder shuts it from the first receiver, the steam in that receiver and in the intermediate cylinder expands as shown by mn. The expansion in the intermediate cylinder is represented by pq and the release by qr, corresponding to a rise of pressure  $\alpha\beta$  in the low-pressure cylinder. rs and By represent a transfer of steam from the intermediate cylinder to the low-pressure cylinder. The remainder of the back-pressure line of the intermediate cylinder and the upper part of the low-pressure diagram for the low-pressure cylinder correspond to the same parts of the high-pressure and the intermediate cylinders, so that a statement of the actions in detail does not appear necessary.

The equations for calculating the pressure are numerous, but they are not difficult to state, and the solution for a given example presents no special difficulty. Thus we have

```
p_{a} \approx p_{b} \approx \text{initial pressure}; \qquad v_{p} = \text{vol. first receiver};
p_{b} \approx p_{b}v_{b} + v_{b}; \qquad v_{R} = \text{vol. acc and receiver};
I. \quad p_{d} \approx p_{e} \approx \left\{p_{c}v_{e} + p_{n}\left(v_{b} + v_{p}\right)\right\} + \left(v_{d} + v_{b} + v_{r}\right);
p_{f} \approx p_{p} \approx p_{d}\left(v_{d} + v_{b} + v_{p}\right) + \left(v_{s} + v_{p} + v_{p}\right);
p_{f} \approx p_{f}\left(v_{f} + v_{p}\right) + \left(v_{f} + v_{p}\right);
p_{g} \approx p_{f}\left(v_{f} + v_{p}\right) + \left(v_{g} + v_{p}\right);
p_{l} \approx p_{h} \approx p_{h}\left(v_{h} + v_{h} + v_{h}\right) + \left(v_{h} + v_{h} + v_{h}\right);
p_{h} \approx p_{h}\left(v_{h} + v_{h}\right) + \left(v_{h} + v_{h} + v_{h}\right);
p_{h} \approx p_{h}\left(v_{h} + v_{h}\right) + \left(v_{h} + v_{h}\right);
p_{h} \approx p_{h}\left(v_{h} + v_{h}\right) + \left(v_{h} + v_{h}\right);
p_{h} \approx p_{h}\left(v_{h} + v_{h}\right) + \left(v_{h} + v_{h}\right);
p_{h} \approx p_{h}\left(v_{h} + v_{h}\right) + \left(v_{h} + v_{h}\right);
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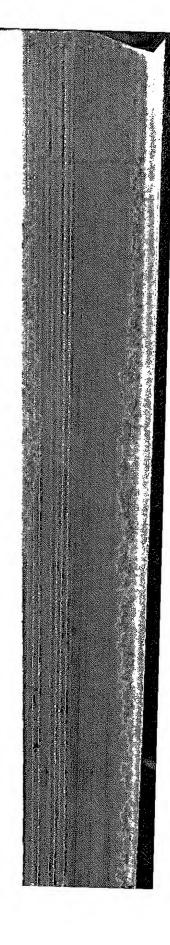
III. 
$$p_s = p_\beta = \{p_4v_4 + v_4 (v_4 + v_B)\} \div (v_r + v_4 + v_R);$$
 $p_0 = p_Y = p_r (v_r + v_4 v_R) \div (v_5 + v_Y + v_R);$ 
 $p_1 = p_5 (v_5 + v_R) \div (v_4 + v_R);$ 
 $p_2 = p_4 (v_4 + v_R) \div (v_2 + v_R);$ 

IV.  $p_3 = \{p_3 (v_2 + v_R) + p_3v_3\} \div (v_3 + v_3 + v_R);$ 
 $p_4 = p_3 (v_2 + v_3 + v_R) + (v_2 + v_3 + v_R);$ 
 $p_4 = p_2v_3 + v_3;$ 
 $p_5 = p_7v_7 + v_5;$ 
 $p_6 = p_5 = \text{back-pressure};$ 
 $p_7 = p_5v_5 \div v_7.$ 

The pressures at c and at  $\eta$  can be calculated immediately from the initial pressure and from the back-pressure. Then it will be recognized that there are four individual equations for finding  $p_f$ ,  $p_k$ ,  $p_n$  and  $p_s$ . The fourteen remaining equations, solved as simultaneous equations, give the corresponding fourteen required pressures, some of which are used in calculating the four pressures which are determined by the four individual equations. The most ready solution may be made by continuous substitution in the four equations which are numbered at the left hand. Thus for  $p_g$  in equation II, we may substitute,

$$p_{q} = p_{r} \frac{v_{r} + v_{\rho}}{v_{o} + v_{\rho}} = p_{e} \frac{v_{e} + v_{\rho}}{v_{r} + v_{\rho}} \frac{v_{r} + v_{\rho}}{v_{o} + v_{\rho}} = p_{d} \frac{v_{d} + v_{o} + v_{\rho}}{v_{e} + v_{\rho} + v_{\rho}} \frac{v_{e} + v_{\rho}}{v_{o} + v_{\rho}}.$$

In the actual computation the several volumes and the proper sums of volumes are to be first determined; consequently the factors following  $p_d$  will be numerical factors which may be conveniently reduced to the lowest terms before introduction in the equation. This system of substitution will give almost immediately four equations with four unknown quantities which may readily be solved; after which the determination of individual pressures will be easy. In handling these equations the letters representing smaller pressures should be eliminated first, thus giving values of higher pressure like  $p_d$  to tenths of a pound; afterward the lower pressure can be determined to a like degree



of accuracy. A skilled computer may make a complete solution of such a problem in two or three hours, which is not excessive for an engineering method.

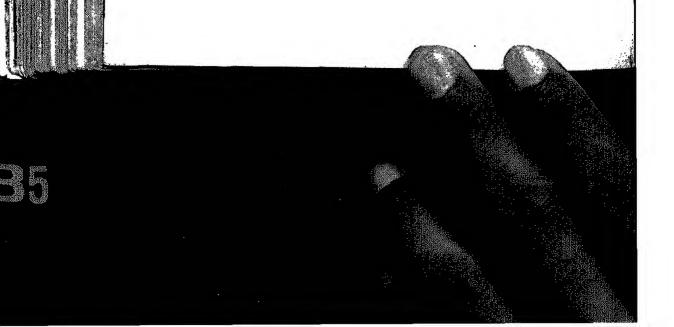
If the cut-off for the intermediate cylinder occurs before the release of the high-pressure cylinder, then the transfer represented by de and op does not occur. In like manner, if the cut-off for the low-pressure cylinder occurs before the release for the intermediate cylinder, the transfer represented by rs and  $\beta\gamma$  does not occur. The omission of a transfer of course simplifies the work of deducing and of solving equations.

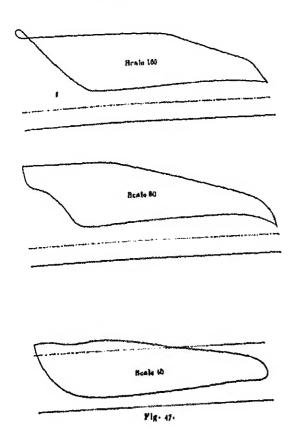
In much the same way, equations may be deduced for calculating pressures when the cranks have the sequence highpressure, intermediate, and low-pressure. The diagrams take forms which are distinctly unlike those for the other sequence of cranks. In general, the case solved, i.e., high-pressure, lowpressure, and intermediate, gives a smoother action for the engine.

For example, the engines of the U.S.S. Machias have the following dimensions and proportions:

	High- prossure.	Inter- Low- mediate, pressur	
Diameter of piston, inches	151	22 } 35	
Piston displacement, cubic feet	2.71	5.53 13.3	ß
Clearance, per cent	11	I-I 7	
Cut-off, per cent stroke	66	66 66	
Release, per cent stroke	01	93 93	
Compression, per cent stroke	r8	18 18	
Ratio of piston displacements	t	2.04 4.9	14
Volume first receiver, cubic feet			
Volume accord resolver wilds for	• •	2,22	
Volume second receiver, cubic feet	• •	6. 26	
Ratio of receiver volumes to high-pressure piston of	lin-		
placement	0.81	2.3	I
Stroke, inches		2.1	
Boiler-pressure, absolute, pounds per sq. in		180	
Pressure in condenser, pounds per sq. in.	•	•	
the self the	•	2	

If the volume of the high-pressure piston displacement is taken to be unity, then the volumes required in the equations for





calculating pressures, when the cranks have the order highpressure, low-pressure, and intermediate, are as follows:

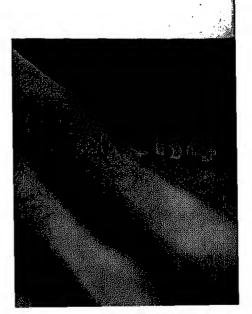
$v_b = 0.79$ $v_a = v_d = 1.06$ $v_e = 1.10$ $v_f = 1.13$ $v_g = v_h = 0.88$ $v_i = 0.31$ $v_k = v_a = 0.13$	V <sub>1</sub> = 0.29 V <sub>m</sub> = 0.08 V <sub>n</sub> = 0.08 V <sub>n</sub> = 0.03 V <sub>n</sub> = 0.03 V <sub>n</sub> = 0.03 V <sub>n</sub> = 0.28 V <sub>n</sub> = 0.03 V <sub>n</sub> = 0.03 V <sub>n</sub> = 0.03	υ, σου υ, που 0.35 υ, που 2.02 υα και υμ που 2.72 υγ του 3.60 υδ και υ, που 4.94 υζ του 1.23
	V 0103	

The required pressures are.

$p_a = p_b = 150$	$p_k = 165$	$p_{\omega} = p_{\varepsilon} = 25.6$
$p_c = 112$	$p_n = 60.0$	$p_x = 52.3$
$p_d = p_o = 76.5$	$p_q = 50.5$	$p_a = 22.1$
$p_e = p_p = 67.5$	$p_r = p_\beta = 28.3$	$p_{\delta} = 18.5$
$p_f = 67.5$	$p_s = p_{\gamma} = 25.3$	$p_{\bullet} = p_{\zeta} = 5$
$p_{g} = 76.9$	$p_t = 25.1$	$p_{\eta} = 17.6$
$p_h = p_l = 73.5$	$p_u = 29.0$	
$p_i = p_m = 69.3$	$p_v = p_y = 28.2$	

Diagrams with the volumes and pressures corresponding to this example are plotted in Fig. 46 with convenient vertical scales. Actual indicator-diagrams taken from the engine are given by Fig. 47. The events of the stroke come at slightly different piston positions on account of the irregularity due to the connecting-rod, and the drops and other fluctuations of pressure are gradual instead of sudden; moreover, there is considerable loss of pressure from the boiler to the engine, from one cylinder to another, and from the low-pressure cylinder to the condenser. Nevertheless the general forms of the diagrams are easily recognized, and all apparent erratic variations are accounted for.

Designing Compound Engines. — The designer of compound and multiple-expansion engines should have at hand a well-systematized fund of information concerning the sizes, proportions, and powers of such engines, together with actual indicator-diagrams. He may then, by a more or less direct method of interpolation or exterpolation, assign the dimensions and proportions to a new design, and can, if deemed advisable, draw or determine a set of probable indicator-diagrams for the new engines. If the new design differs much from the engines for which he has information, he may determine approximate diagrams both for an actual engine from which indicator-diagrams are at hand, and for the new design. He may then sketch diagrams for the new engine, using the approximate



diagrams as a basis and taking a comparison of the approximate and actual diagrams from the engine already built, as a guide. It is convenient to prepare and use a table showing the ratios of actual mean effective pressures and approximate mean effective pressures. Such a table enables the designer to assign mean effective pressures to a cylinder of the new engine and to infer very closely what its horse-power will be. It is also very useful as a check in sketching probable diagrams for a new engine, which diagrams are not only useful in estimating the power of the new engine, but in calculating stresses on the members of that engine.

A rough approximation of the power of an engine may be made by calculating the power as though the total or equivalent expansion took place in the low-pressure cylinder, neglecting clearance and compression. The power thus found is to be affected by a factor which according to the size and type of the engine may vary from 0.6 to 0.9 for compound engines and from 0.5 to 0.8 for triple engines. Seaton and Rounthwaite \* give the following table of multipliers for compound marine engines:

MULTIPLIERS FOR FINDING PROBABLE M.E.P. COMPOUND AND TRIPLE MARINE ENGINES,

Description of Engine.			Jacksted.	Unjacksted.			
Dondres consumit were and the						0.674.0.72	
Receiver-compound, scrow-engines. Receiver-compound, paddie-engines						0.67 ta 0.73	0.58 to 0.68 0.55 to 0.65
Direct expansion							0.71 to 0.75
Three-cyfinder triple, merchant ships Three-cylinder triple, naval vessels.	٠	•	•	•	٠	0.64 (0.0,68	a.60 to a.66
Three-cylinder triple, gunboats and tor	110	el.	i.l	XIII	14	0.55 to 0.65	0.60 to 0.67

For example, let the holler-pressure be 80 pounds by the gauge, or 94.7 pounds absolute; let the back-pressure be 4 pounds absolute; and let the total number of expansions be six, so that the volume of steam exhausted to the condenser is six times the

<sup>\*</sup> Pocket Book of Marine Engineering.

volume admitted from the boiler. Neglecting the effect of clearance and compression, the mean effective pressure is

If the large cylinder is 30 inches in diameter, and the stroke is 4 feet, the horse-power at 60 revolutions per minute is

$$\frac{\pi \cdot 30^3}{4} \times 40.06 \times 2 \times 4 \times 60 + 33000 \approx 412 \text{ H.P.}$$

If the factor to be used in this case is 0.75, then the actual horse-power will be about

Binary Engines. — Another form of compound engines using two fluids like steam and ether, was proposed by du Trembly \* in 1850, to extend the lower range of temperature of vapor-engines. At that time the common steam-pressure was not far from thirty pounds by the gauge, corresponding to a temperature of 250° F. If the back-pressure of the engine be assumed to be 1.5 pounds absolute (115° F.), the efficiency for Carnot's cycle would be approximately

$$\frac{250 - 115}{250 + 460} = 0.19.$$

If, however, by the use of a more volatile fluid the result at lower temperature could be reduced to 65° F., the efficiency could be increased to

$$\frac{250-65}{250+460}$$
 = 0.26.

At the present time when higher steam-pressures are common, the comparison is less favorable. Thus the temperature of steam at 150 pounds by the gauge is 365° F., so that with 1.5

\*Manuel du Conducteur des Machines à Vaporous combinées au Machines Binaires, also Rankine Steam Engine, p. 444.



pounds absolute (or 115° F.) for the back-pressure the efficiency for Carnot's cycle is

$$\frac{365 - 115}{365 + 460} = 0.30,$$

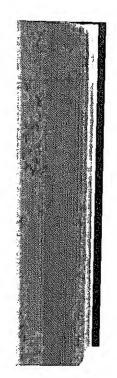
and for a resultant temperature of 65° F., the efficiency would be

$$\frac{365-65}{365+460} = 0.36$$

If a like gain of economy could be obtained in practice, it would represent a saving of 17 per cent, which would be well worth while. Further discussion of this matter of economy will be given in Chapter XI, in connection with experiments on binary engines using steam and sulphur-dioxide.

The practical arrangement of a binary engine substitutes for the condenser an appliance having somewhat the same form as a tubular surface-condenser, the steam being condensed on the outside of the tubes and withdrawn in the form of water of condensation at the bottom. Through the tubes is forced the more volatile fluid, which is vaporized much as it would be in a "water-tube" boiler. The vapor is then used in a cylinder differing in no essential from that for a steam-engine, and in turn is condensed in a surface-condenser which is cooled with water at the lowest possible temperature.

An ideal arrangement for a binary engine avoiding the use of air-pumps would appear to be the combination of a compound non-condensing steam-engine with a third cylinder on the binary system which should have for its working substance a fluid that would give a convenient pressure at 212° F., and a pressure somewhat above the atmosphere at 60° F. There is no known fluid that gives both these conditions; thus ether at 212° F. gives a pressure of about 96 pounds absolute, but its boiling point at atmospheric pressure is 94° F., consequently it would from necessity require a vacuum and an air-pump unless the ether could be entirely freed from air, and leakage into the vacuum space entirely prevented. Sulphur-dioxide gives a pressure of 41



pounds absolute at 00° P., so that it can always be worked at a pressure above the atmosphere; but 212° F. would give an inconvenient pressure, and in practice it has been found convenient to run the steam-engine with a vacuum of 22 inches of mercury or about 4 pounds absolute, which gives a temperature of 155° F, at which sulphur-dioxide has a pressure of 180 pounds per square inch by the gauge. The attempt of du Trembly to use ether for the second fluid in a binary engine did not result favorably, as his fuel-consumption was not less than that of good engines of that time, which appears to indicate that he could not secure favorable conditions.

# CHAPTER X.

### TESTING STEAM-ENGINES.

THE principal object of tests of steam-engines is to determine the cost of power. Series of engine tests are made to determine the effect of certain conditions, such as superheating and steam-jackets, on the economy of the engine. Again, tests may be made to investigate the interchanges of heat between the steam and the walls of the cylinder by the aid of Hirn's analysis, and thus find how certain conditions produce effects that are favorable or unfavorable to economy.

The two main elements of an engine test are, then, the measurement of the power developed and the determination of the cost of the power in terms of thermal units, pounds of steam, or pounds of coal. Power is most commonly measured by aid of the steam-engine indicator, but the power delivered by the engine is sometimes determined by a dynamometer or a friction brake; sometimes, when an indicator cannot be used conveniently, the dynamic or brake power only is determined. When the engine drives a dynamo-electric generator the power applied to the generator may be determined electrically, and thus the power delivered by the engine may be known.

When the cost of power is given in terms of coal per horsepower per hour, it is sufficient to weigh the coal for a definite period of time. In such case a combined boiler and engine test is made, and all the methods and precautions for a careful boiler test must be observed. The time required for such a test depends on the depth of the fire on the grate and the rate of combustion. For factory boilers the test should be twenty-four hours long if exact results are desired.

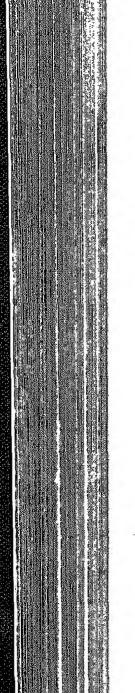
When the cost of power is stated in terms of steam per horsepower per hour, one of two methods may be followed. When

the engine has a surface-condenser the steam t engine is condensed, collected, and weight usually sufficient for tests under favorable c intervals, ten or fifteen minutes, give fairly The chief objection to this method is that the to leak water at the tube packings. Under fa the results of tests by this method and by deta water supplied to the boiler are substantially t] on non-condensing and on jet-condensing e1 consumption is determined by weighing or me water supplied to the boiler or boilers that ful engine. Steam used for any other purpose engine, for example, for pumping, heating, or nations of the quality of the steam, must be allowed for: The most satisfactory way is weigh such steam; but small quantities, as quality by a steam calorimeter, may be gaugec flow through an orifice. Tests which depend feed-water should be long enough to minimize uncertainty of the amount of water in a boiler an apparent height of water in a water-gauge: height of the water-level depends largely on the tion and the activity of convection currents. When the cost of power is expressed in the necessary to measure the steam-pressure, the ar in the steam supplied to the cylinder, and the t condensed steam when it leaves the condenser. in jackets or reheaters it must be accounted But it is customary in all engine tests to ta temperatures, so that the cost may usually thermal units, even when the experimenter is c in pounds of steam. For a Hirn's analysis it is necessary to weig condensing water, and to determine the tempe sion to and exit from the condenser. Important engines, with their boilers and other are commonly built under contract to give a certain economy, and the fulfilment of the terms of a contract is determined by a test of the engine or of the whole plant. The test of the entire plant has the advantage that it gives, as one result, the cost of power directly in coal; but as the engine is often watched with more care during a test than in regular service, and as auxiliary duties, such as heating and banking fires, are frequently omitted from such an economy test, the actual cost of power can be more justly obtained from a record of the engine in regular service, extending for weeks or months. The tests of engine and boilers, though made at the same time, need not start and stop at the same time, though there is a satisfaction in making them strictly simultaneous. This requires that the tests shall be long enough to avoid drawing the fires at beginning and end of the boiler test.

In anticipation of a test on an engine it must be run for some time under the conditions of the test, to climinate the effects of starting or of changes. Thus engines with steam-jackets are commonly started with steam in the jackets, even if they are to run with steam excluded from the jackets. An hour or more must then be allowed before the effect of using steam in the jackets will entirely pass away. An engine without steam-jackets, or with steam in the jackets, may come to constant conditions in a fraction of that time, but it is usually well to allow at least an hour before starting the test.

It is of the first importance that all the conditions of a test shall remain constant throughout the test. Changes of steampressure are particularly bad, for when the steam-pressure rises the temperature of the engine and all parts affected by the steam must be increased, and the heat required for this purpose is charged against the performance of the engine; if the steampressure falls a contrary effect will be felt. In a series of tests one element at a time should be changed, so that the effect of that element may not be confused by other changes, even though such changes have a relatively small effect. It is, however, of more importance that steam-pressure should remain constant





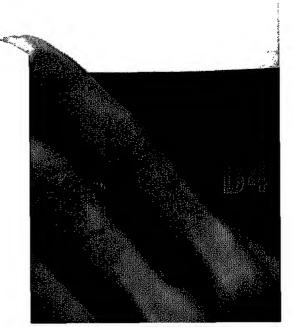
than that all tests at a given pressure should have identically the same steam-pressure, because the total heat of steam varies more slowly than the temperature.

All the instruments and apparatus used for an engine test should be tested and standardized either just before or just after the test; preferably before, to avoid annoyance when any instrument fails during the test and is replaced by another.

Thermometers. — Temperatures are commonly measured by aid of mercurial thermometers, of which three grades may be distinguished. For work resembling that done by the physicist the highest grade should be used, and these must ordinarily be calibrated, and have their boiling- and freezing-points determined by the experimenter or some qualified person; since the freezing-point is liable to change, it should be redetermined when necessary. For important data good thermometers must be used, such as are sold by reliable dealers, but it is preferable that they should be calibrated or else compared with a thermometer that is known to be reliable. For secondary data or for those requiring little accuracy common thermometers with the graduation on the stem may be used, but these also should have their errors determined and allowed for. Thermometers with detachable scales should be used only for crude work.

Gauges. — Pressures are commonly measured by Bourdon gauges, and if recently compared with a correct mercury column these are sufficient for engineering work. The columns used by gauge-makers are sometimes subject to minor errors, and are not usually corrected for temperature. It is important that such gauges should be frequently retested.

Dynamometers. — The standard for measurement of power is the friction-brake. For smooth continuous running it is essential that the brake and its band shall be cooled by a stream of water that does not come in contact with the rubbing surfaces. Sometimes the wheel is cooled by a stream of water circulating through it, sometimes the band is so cooled, or both may be. A rubbing surface which is not cooled should be of nonconducting material. If both rubbing surfaces are metallic they



nust be freely lubricated with oil. An iron wheel running in a pand furnished with blocks of wood requires little or no lubrication.

To avoid the increase of friction on the brake-bearings due to the load applied at a single brake-arm, two equal arms may be used with two equal and opposite forces applied at the ends of form a statical couple.

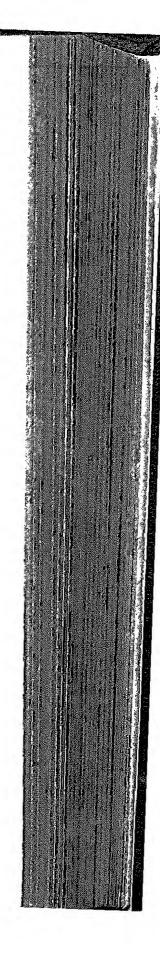
With care and good workmanship a friction-brake may be made an instrument of precision sufficient for physical investigations, but with ordinary care and workmanship it will give esults of sufficient accuracy for engineering work.

An engine which drives an electric-generator may readily have he dynamic or brake-power determined from the electric outout, provided that the efficiency of the generator is properly letermined.

The only power that can be measured for a steam-turbine is the dynamic or brake-power; when connected with an electric-enerator this involves no difficulty. For marine propulsion it is customary to determine the power of steam-turbines by some orm of torsion-metre applied to the shaft that connects the arbine to the propeller. This instrument measures the angle if torsion of the shaft while running, and consequently, if the modulus of elasticity has been determined, gives a positive etermination of the power delivered to the propeller. Under avorable conditions a torsion-metre may have an error of not more than one per cent.

Indicators. — The most important and at the same time the east satisfactory instrument used in engine-testing is the indicator. Even when well made and in good condition it is liable to have an error which may amount to two per cent when used a moderate speeds. At high speeds, three hundred revolutions for minute and over, it is likely to have two or three times as such error. As a rule, an indicator cannot be used at more tan four hundred revolutions per minute.

The mechanism for reducing the motion of the crosshead of the engine and transferring it to the paper drum of an indicator



should require only a very short cord leading to the paper drum, because all the errors due to the paper drum are proportional to the length of the cord and may be practically eliminated by making the cord short.

The weighing and recording of the steam-pressure by the indicator-piston, pencil-motion, and pencil are affected by errors which may be classified as follows:

- t. Scale of the spring.
- 2. Design of the pencil-motion.
- 3. Inertia of moving parts.
- Friction and backlash.

Good indicator-springs, when tested by direct loads out of the indicator, usually have correct and uniform scales; that is, they collapse under pressure the proper amount for each load applied. When enclosed in the cylinder of an indicator the spring is heated by conduction and radiation to the temperature of the cylinder, and that temperature is sensibly equal to the mean temperature in the engine-cylinder. But a spring is appreciably weaker at high temperatures, so that when thus enclosed in the indicator-cylinder, it gives results that are too large; the error may be two per cent or more.

Outside spring-indicators avoid this difficulty and are to be preferred for all important work. They have only one disadvantage, in that the moving parts are heavier, but this may be overcome by increasing the area of the piston from half a square inch to one square inch.

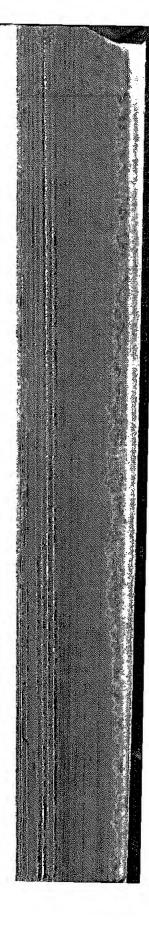
The motion of the piston of the indicator is multiplied five or six times by the pencil-motion, which is usually an approximate parallel motion. Within the proper range of motion (about two inches) the pencil draws a line which is nearly straight when the paper drum is at rest, and it gives a nearly uniform scale provided that the spring is uniform. The errors due to the geometric design of this part of the indicator are always small.



When steam is suddenly let into the indicator, as at admission to the engine-cylinder, the indicator-piston and attached parts forming the pencil-motion are set into vibration, with a natural time of vibration depending on the stiffness of the spring. A weak spring used for indicating a high-speed engine may throw the diagram into confusion, because the pencil will give a few deep undulations which make it impossible to recognize the events of the stroke of the engine, such as cut-off and release. A stiffer spring will give more rapid and less extensive undulations, which will be much less troublesome. As a rule, when the undulations do not confuse the diagram the area of the diagram is but little affected by the undulations due to the inertia of the piston and pencil-motion.

The most troublesome errors of the indicator are due to friction and backlash. The various joints at the piston and in the pencil-motion are made as tight as can be without undue friction, but there is always some looseness and some friction at those joints. There is also some friction of the piston in the cylinder and of the pencil on the paper. Errors from this source may be one or two per cent, and are liable be excessive unless the instrument is used with care and skill. A blunt pencil pressed up hard on the paper will reduce the area of the diagram five per cent or more; on the other hand, a medium pencil drawing a faint but legiblé line will affect the area very little. Any considerable friction of the piston of the indicator will destroy the value of the diagram.

Errors of the scale of the spring can be readily determined and investigated by loading the spring with known weights, when properly supported, out of the indicator. This method is probably sufficient for outside spring indicators. Those that have the spring inside the cylinder are tested under steam pressure, measuring the pressure either by a gauge or a mercury column. Considerable care and skill are required to get good results, especially to avoid excessive friction of the piston as it remains at rest or moves slowly in the cylinder. It must be borne in mind that the indicator cylinder heats readily when subjected to



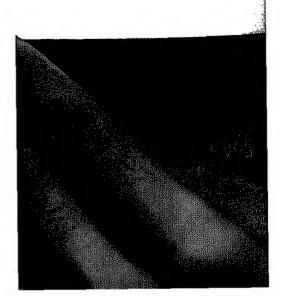
slowly, and that consequently tests made with falling steam pressures are not valuable.

Scales. — Weighing should be done on scales adapted to the load; overloading leads to excessive friction at the knife-edges and to lack of delicacy. Good commercial platform scales, when tested with standard weights, are sufficient for engineering work.

Coal and ashes are readily weighed in barrows, for which the tare is determined by weighing empty. Water is weighed in barrels or tanks. The water can usually be pumped in or allowed to run in under a head, so that the barrel or tank can be filled promptly. Large quick-opening valves must be used to allow the water to run out quickly. As the receptacle will seldom drain properly, it is not well to wait for it to drain, but to close the exit-valve and weigh empty with whatever small amount of water may be caught in it. Neither is it well to try to fill the receptacle to a given weight, as the jet of water running in may affect the weighing. With large enough scales and tanks the largest amounts of water used for engine tests may be readily handled.

Measuring Water. — When it is not convenient to weigh water directly, it may be measured in tanks or other receptacles of known volume. Commonly two are used, so that one may fill while the other is emptied. The volume of a receptacle may be calculated from its dimensions, or may be determined by weighing in water enough to fill it. When desired a receptacle may be provided with a scale showing the depth of the water, and so partial volumes can be determined. A closed receptacle may be used to measure hot water or other fluids.

Water-Meters of good make may be used for measuring water when other methods are not applicable, provided they are tested and rated under the conditions for which they are used, taking account of the amount and temperature of the water measured. Metres are most convenient for testing marine engines because water cannot be weighed at sea on account of the motion of the ship, and arrangements for measuring water in tanks are expensive and inconvenient. For such tests the metre may be placed

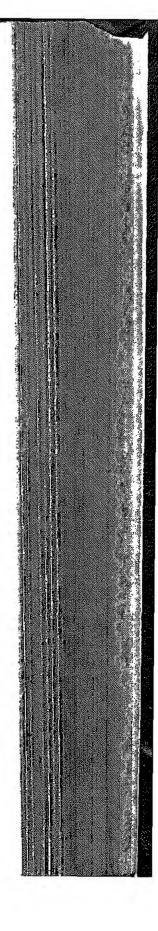


on a by-pass through which the feed-water from the surfacecondenser can be made to pass by closing a valve on the direct line of feed-pipe. If necessary the metre can be quickly shut off and the direct line can be opened. The chief uncertainty in the use of a metre is due to air in the water; to avoid error from this source, the metre should be frequently vented to allow air to escape without being recorded by the metre.

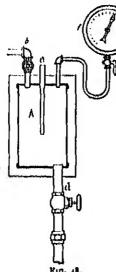
Weirs and Orifices. — So far as possible the use of weirs and orifices for water during engine tests should be avoided, for, in addition to the uncertainties unavoidably connected with such hydraulic measurements, difficulties are liable to arise from the temperature of the water and from the oil in it. A very little oil is enough to sensibly affect the coefficient for a weir or orifice. The water flowing from the hot-well of a jet-condensing engine is so large in amount that it is usually deemed advisable to measure it on a weir; the effect of temperature and oil is less than when the same method is used for measuring condensed steam from a surface-condenser.

Priming-Gauges. — When superheated steam is supplied to an engine it is sufficient to take the temperature of the steam in the steam-pipe near the engine. When moist steam is used the amount of moisture must be determined by a separated test. Originally such tests were made by some form of calorimeter, and that name is now commonly attached to certain devices which are not properly heat-measurers. Three of these will be mentioned: (1) the throttling-calorimeter, which can usually be applied to all engine tests; (2) the separating-calorimeter, which can be applied when the steam is wet; and (3) the Thomas electric calorimeter, intended for use with steam-turbines to determine the moisture in steam at any stage of the turbine whatever may be the pressure or quality of the steam.

Throttling-Calorimeter. — A simple form of calorimeter, devised by the author, is shown by Fig. 48, where  $\Lambda$  is a reservoir about 4 inches in diameter and about 12 inches long to which steam is admitted through a half-inch pipe b, with a throttle-valve near the reservoir. Steam flows away through an



there is a deep cup for a thermometer to measure the temperature. The boiler-pressure may be taken



ature. The boiler-pressure may be taken from a gauge on the main steam-pipe near the calorimeter. It should not be taken from a pipe in which there is a rapid flow of steam as in the pipe b, since the velocity of the steam will affect the gauge-reading, making it less than the real pressure. The reservoir is wrapped with hair-felt and lagged with wood to reduce radiation of heat.

When a test is to be made, the valve on the pipe d is opened wide (this valve is frequently omitted), and the valve at b is opened wide enough to give a pressure of five to fifteen pounds in the reservoir. Readings are then taken of the boiler-

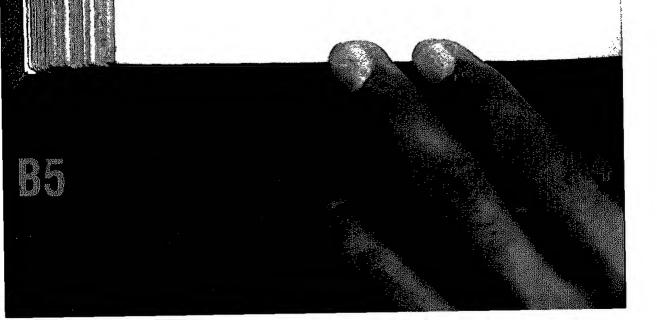
gauge, of the gauge at f, and of the thermometer at e. It is well to wait about ten minutes after the instrument is started before taking readings so that it may be well heated. Let the boller-pressure be p, and let r and q be the latent heat and heat of the liquid corresponding. Let  $p_i$  be the pressure in the calorimeter,  $r_i$  the heat of vaporization,  $q_i$  the heat of the liquid, and  $t_i$  the temperature of saturated steam at that pressure, while  $t_i$  is the temperature of the superheated steam in the calorimeter. Then

$$c_r + q = r_1 + q_1 + c_{p_1} (l_1 - l_1);$$

$$c_r = \frac{r_1 + q_1 + c_{p_1} (l_1 - l_1) - q}{r}.$$
 (152)

Example. — The following are the data of a test made with this calorimeter:

Pressure of the atmosphere . . . . 14.8 pounds; Steam-pressure by gauge . . . 69.8 '' Pressure in the calorimeter, gauge . 12.0 '' Temperature in the calorimeter . . 268°.2 F.



Specific heat of superheated steam for the condition of the 1st 0.48.

$$x = \frac{943.8 + 212.7 + 0.48 (268.2 - 243.9) - 285.9}{892.3} = 0.988;$$

Per cent of priming, 1.2.

A little consideration shows that this type of calorimeter an be used only when the priming is not excessive; otherwise he throttling will fail to superheat the steam, and in such case withing can be told about the condition of the steam either before is after throttling. To find this limit for any pressure t, may be nade equal to t, in equation(152); that is, we may assume that he steam is just dry and saturated at that limit in the calorimeter. Ordinarily the lowest convenient pressure in the calorimeter is he pressure of the atmosphere, or 14.7 pounds to the square inch. The table following has been calculated for several pressures in he manner indicated. It shows that the limit is higher for higher pressures, but that the calorimeter can be applied only where the priming is moderate.

When this calorimeter is used to test steam supplied to a condensing-engine the limit may be extended by connecting the exhaust to the condenser. For example, the limit at 100 pounds absolute, with 3 pounds absolute in the calorimeter, is 0.064 instead of 0.040 with atmospheric pressure in the calorimeter.

LIMITS OF THE THROTTLING-CALORIMETER.

Pressure.		Priming	
Absolute.	Cauge.	, ,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,	
300 285.3		0.077	
250	235-3	0.070	
200	185.3	0.061	
175	160.3	0.058	
150	135.3	0.052	
125	110.3	0.046	
100	85.3	0.040	
75	60.3	0.032	
50	35.3	0.023	

In case the calorimeter is used near its limit — that is, when the superheating is a few degrees only — it is essential that the thermometer should be entirely reliable; otherwise it might happen that the thermometer should show superheating when the steam in the calorimeter was saturated or moist. In any other case a considerable error in the temperature will produce an inconsiderable effect on the result. Thus at 100 pounds absolute with atmospheric pressure in the calorimeter, 10° F, of superheating indicates 0.035 priming, and 15° F, indicates 0.032 priming. So also a slight error in the gauge-reading has little effect. Suppose the reading to be apparently 100.5 pounds absolute instead of 100, then with 10° of superheating the priming appears to be 0.033 instead of 0.032.

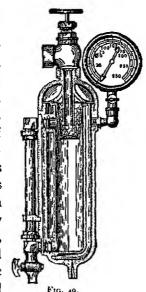
It has been found by experiment that no allowance need be made for radiation from this calorimeter if made as described, provided that 200 pounds of steam are run through it per hour. Now this quantity will flow through an orifice one-fourth of an inch in diameter under the pressure of 70 pounds by the gauge, so that if the throttle-valve be replaced by such an orifice the question of radiation need not be considered. In such case a stop-valve will be placed on the pipe to shut off the calorimeter when not in use; it is opened wide when a test is made. If an orifice is not provided the throttle-valve may be opened at first a small amount, and the temperature in the calorimeter noted; after a few minutes the valve may be opened a trifle more, whereupon the temperature may rise, if too little steam was used at first. If the valve is opened little by little till the temperature stops rising, it will then be certain that enough steam is used to reduce the error from radiation to a very small amount.

Separating-Calorimeter. — If steam contains more than three per cent of moisture the priming may be determined by a good separator which will remove nearly all the moisture. It remains to measure the steam and water separately. The water may be best measured in a calibrated vessel or receiver, while the steam may be condensed and weighed, or may be gauged by allowing it to flow through an orifice of known size.



A form of separating-calorimeter devised by Professor Carpenter \* is shown by Fig. 49.

Steam enters a space at the top which has sides of wire gauze and a convex cup at the bottom. The water is thrown against the cup and finds its way through the gauze into an inside chamber or receiver and rises in a water-glass outside. The receiver is calibrated by trial, so that the amount of water may be read directly from a graduated scale. The steam meanwhile passes into the outer chamber which surrounds the inner receiver and escapes from an orifice at the bottom. The steam may be determined by condensing, collecting, and weighing it; or it may be calculated from the pressure and the size of the When the steam is weighed there is no radiation error, since the

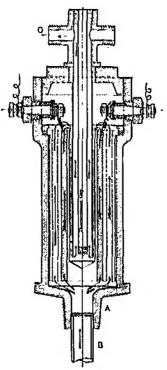


inner chamber is protected by the steam in the outer chamber. This instrument may be guarded against radiation by wrapping and lagging, and then if steam enough is used the radiation will be insignificant, just as was found to be the case for the throttling-calorimeter.

The Thomas Electric Calorimeter. — The essential feature of this instrument (Fig. 50) is the drying and superheating of the steam by a measured amount of electric energy. Steam is admitted at B and passes through numerous holes in a block of soapstone which occupies the middle of the instrument; these holes are partially filled with coils of German silver wire which are heated by an electric current that enters and leaves at the binding-screws. The steam emerges dry or superheated at the upper part of the chamber and passes down through wire gauze, which surrounds the central escape pipe; this central pipe surrounds

<sup>\*</sup> Trans. Am. Soc. Mech. Engs., vol. xvii, p. 608.

the thermometer cup, and leads to the exit at the top, which has two orifices, either of which may be piped to a condenser or elsewhere.



F10. 50.

To use the instrument it is properly connected by a sampling-tube to the space from which steam is drawn, and valves are adjusted to supply a convenient amount of steam which is assumed to be uniform for steady pressure; this last is a matter of some importance.

The current of electricity is then adjusted to dry the steam; this may be determined by noting the temperature by the thermometer in the central thermometer cup, because that thermometer will show a slight rise corresponding to a very small degree of superheating which is sufficient to indicate the disappearance of moisture, but not enough to affect the determination of quality by the instrument. The wire gauze

surrounding the thermometer is an essential feature of this operation, as it insures the homogeneity of the steam, which, without the gauze, would be likely to be a mixture of superheated steam and moist steam. Readings are taken of the proper electrical instruments from which the electrical energy imparted can be determined in watts; let this energy required to dry the steam be denoted by  $E_1$ . Now let the electric current be increased till the steam is superheated 30°, and let  $E_2$  be the increase of electric input which is required to superheat the steam.

If W is the weight of steam slowing per hour through the



instrument under the first conditions, the weight when superheated will be CW, where C is a factor less than unity which has been determined by exhaustive tests on the instrument. The amount of electric energy required to superheat one pound of steam 30° from saturation at various pressures has also been determined and may be represented by S; this constant has been so determined as to include an allowance for radiation, and is more convenient than the specific heat of superheated steam, in this place. Making use of the factors C and S, we may write

$$E_2 = CSW$$
, or  $W = \frac{E_2}{CS}$ ,

which affords a means of climinating the weight of steam used; this is an important feature in the use of the instrument.

Returning now to the first condition of the instrument when steam is dried by the application of  $E_i$ , watts of electric energy, we have for the equivalent heat

and dividing by the expression for the weight of steam flowing per hour, we have for the heat required to dry one pound of steam

$$\frac{3.42 E_1}{W} = 3.42 CS \frac{E_1}{E_2} = (1 - x) r,$$

where r is the heat of vaporization and 1 - x is the amount of water in one pound of moist steam.

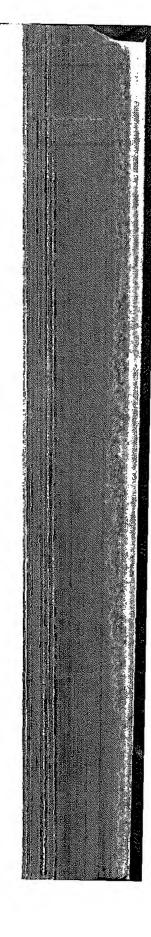
Solving the above equation for x, we have

$$x = 1 - \frac{3.42 CS}{r} \frac{E_1}{E_2}.$$

If desired, the constant factors may be united into one term, and the equation may be written

$$x = 1 - \frac{K}{r} \frac{E_1}{E_2}.$$

With each instrument is furnished a diagram giving values of K for all pressures, so that the use of the instrument involves



only two readings of a wattmeter and the application of the above simple equation.

For example, suppose that the use of the instrument in a particular case gave the values  $E_1 = 240$ , and  $E_2 = 93.0$  for the absolute pressure 100 pounds per square inch. The value of K from the diagram is 54.2, and r from the steam-tables is 884, consequently

$$x = 1 - \frac{54.2}{884} \frac{240}{93.0} = 0.84.$$

Method of Sampling Steam. — It is customary to take a sample of steam for a calorimeter or priming-gauge through a small pipe leading from the main steam-pipe. The best method of securing a sample is an open question; indeed, it is a question whether we ever get a fair sample. There is no question but that the composition of the sample is correctly shown by any of the calorimeters described, when the observer makes tests with proper care and skill. It is probable that the best way is to take steam through a pipe which reaches at least halfway across the main steam-pipe, and which is closed at the end and drilled full of small holes. It is better to have the sampling-pipe at the side or top of the main, and it is better to take a sample from a pipe through which steam flows vertically upward. The sampling-pipe should be short and well wrapped to avoid radiation.



### CHAPTER XI.

#### INFLUENCE OF THE CYLINDER WALLS.

In this chapter a discussion will be given of the discrepancy between the theory of the steam-engine as detailed in the previous chapter, and the actual performance as determined by tests on engines. It was early evident that this discrepancy was due to the interference of the metal of the cylinder walls which abstracted heat from the steam at high pressure and gave it out at low pressure. In consequence there followed a long struggle to determine precisely what action the walls exerted and how to allow for that action in the design of new engines. The first part has been accomplished; we can determine to a nicety the influence of the cylinder walls for any engine already built and tested; but as yet all attempts to systematize the information derived from such tests in such a manner that it can be used in the design of new engines has been utterly futile. Consequently the discussion in this chapter is important mainly in that it allows us to understand the real action of certain devices that are intended to improve the economy of engines, and to form a just opinion on the probability of future improvements.

As soon as the investigations by Clausius and Rankine and the experiments by Regnault made a precise theory of the steam engine possible, it became evident that engines used from quarter to half again as much steam as the adiabatic theory indicated, and in particular that expansion down to the back-pressure was inadvisable. An early and a satisfactory exposition of these points was made by Isherwood after his tests on the U. S. S. Michigan, which are given in Table III.

# TABLE III.

TESTS ON THE ENGINE OF THE U. S. S. MICHIGAN.

CYLINDER DIAMETER, 30 INCHES; STROKE, 8 PEET.

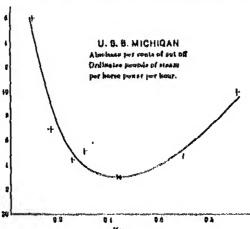
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Programme contract and the contract of the con						
gabooning or other or the				1.	n.   m	IV. V. VI. VII.
Duration, hours				73	74 7	2 72 72 72 72 0 3/10 1/4 1/6 4/45 3 1 3 7 1 3 9 1 1 . 2 14 1
Cut-off			• • •{	11/13	7/10 4/	1/3/10 1/4 1/6 1/4c
Revolutions per	intitute	1		20.6	15.017.	31.1.7113.911.214
Holler-pressure, ntmosphere .	Ignitional Isea	mil 1111	KIKIYU	21.0	10.5 21.	911 911 921 9
Harometer, Inche				10.0	20.8120.	2130 1120 0120 0120
Vacuum, Inches				201.5	20.1136.	3135.8125.8125.6121 .
Steam per horse-	finact bet p	our, pour	ula .	18. ol	22. XI22.	2 2 1 2 2 2 2 2 2 2 2
Let cent of witer	r in cylluder	ut teleuse	1	10.7	15.3127.	2 41 . 7 39 . 6 42 . 1 45 . 1

In the first place the best economy for this engine was 32.7 pounds instead of 26.5 pounds as calculated by the expression

$$\frac{60 \times 33000}{778 (r_1 + q_1 - x_2 r_2 - q_2)}$$

deduced on page 141 for the steam-consumption for a non-con-



ducting engine with complete expansion. This result was obtained with cut-off at four-ninths of the stroke which gave a terminal pressure of one pound above the atmosphere.

The manner of the variation of the steam consumption with the cut-off is clearly shown by Fig. 51, in

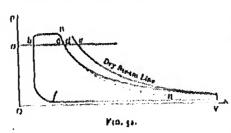
which the fraction of stroke at cut-off is taken for abscisso and the steam-consumptions as ordinates.

To make the diagram clear and compact, the axis of abscissæ is taken at 30 pounds of steam per horse-power per hour. An inspection of this diagram and of the figures in the table shows a regularity in the results which can be attained only when tests are made with care and skill. The only condition purposely varied is the cut-off; the only condition showing important accidental variation is the vacuum, and consequently the back-pressure in the cylinder. To allow for the small variations in the back-pressure Isherwood changed the mean effective pressure for each test by adding or subtracting, as the case might require, the difference between the actual back-pressure and the mean back-pressure of 2.7 pounds per square inch, as deduced from all the tests.

An inspection of any such a series of tests having a wide range of expansions will show that the steam-consumption decreases as the cut-off is shortened till a minimum is reached, usually at 1/3 to 1/2 stroke; any further shortening of the cut-off will be accompanied by an increased steam-consumption, which may become excessive if the cut-off is made very short. Some insight into the reason for this may be had from the per cent of water in the cylinder, calculated from the dimensions of the cylinder and the pressures in the cylinder taken from the indicator-diagram. The method of the calculation will be given in detail a little later in connection with Hirn's analysis. It will be sufficient now to notice that the amount of water in the cylinder of the engine of the Michigan at release increased from 10.7 per cent for a cut-off at 11 of the stroke to 45.1 per cent for a cut-off at 45 of the stroke. Now all the water in the cylinder at release is vaporized during the exhaust, the heat for this purpose being abstracted from the cylinder walls, and the heat thus abstracted is wasted, without any compensation. The walls may be warmed to some extent in consequence of the rise of pressure and temperature during compression, but by far the greater part of the heat abstracted during exhaust must be supplied by the incoming steam at admission. There is, therefore, a large condensation of steam during admission and up to cut-off, and the greater part

of the steam thus condensed remains in the form of water and does little if anything toward producing work. This may be seen by inspection of the table of results of Dixwell's tests on page 270. With saturated steam and with cut-off at 0,217 of the stroke, 52.2 per cent of the working substance in the cylinder was water. Of this 19.8 per cent was reëvaporated during expansion, and 32.4 per cent remained at release to be reëvaporated during exhaust. When the cut-off was lengthened to 0.680 of the stroke, there was 27.9 per cent of water at cut-off and 23.0 per cent at release. The statement in percentages gives a correct idea of the preponderating influence of the cylinder walls when the cut-off is unduly shortened; it is, however, not true that there is more condensation with a short than with a long cut-off. On the contrary, there is more water condensed in the cylinder when the cut-off is long, only the condensation does not increase as fast as do the weight of steam supplied to the cylinder and the work done, and consequently the condenantion has a less effect.

Graphical Representation. - The divergence of the actual



expansion line from the adiabatic line can be shown in a striking manner by plotting the former on the temperature-entropy diagram as shown in Fig. 53 which is constructed from the indicator-

diagram in Fig. 52, shown with the axes of zero pressure and zero volume drawn in the usual manner, allowing for clearance and for the pressure of the atmosphere.

In order to undertake this construction the weight of steam per stroke W as determined from the test of the engine during which the diagrams were taken, must be determined, and the weight of steam  $W_n$  caught in the clearance must be computed from the pressure and volume  $f_n$  the beginning of compression.

The dry steam line (Fig. 52) is drawn by the following process:

a line as is drawn at a convenient pressure, and on it is laid off the volume of  $W + W_0$  pounds of dry steam as determined from the steam-table to the proper scale of the drawing. Thus if  $s_e$  is the specific volume of the steam at the pressure  $p_e$  the volume of steam present if dry and saturated would be

But the length of the diagram L, in inches is proportional to the piston displacement D in cubic feet. The latter is obtained by multiplying the area of the piston in square feet by its stroke in feet. For the crank end the net area of the piston is to be used, allowing for the piston-rod. Consequently the proper abscissa, representing the volume is obtained by multiplying by  $\frac{L}{D}$ , giving

$$s = \frac{(W + W_0) L}{D}$$
;

and of this all except s is a constant for which a numerical result can be found.

The diagram shown by Fig. 52 was taken from the head end of the high-pressure cylinder of an experimental engine in the laboratory of the Massachusetts Institute of Technology. The value of  $W + W_0$  was found to be 0.075 of a pound; the piston displacement was 1.102 cubic feet, and the length of the diagram was 3.69 inches; consequently

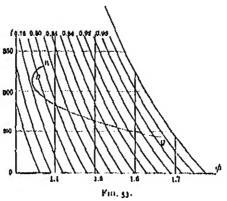
$$\frac{(W + W_0) L}{D}$$
 0.251.

The line as was drawn at 90 pounds absolute at which s = 4.86 cubic feet; the length of the line as was consequently

Neglecting the volume of the water present, the volume of steam actually present hore the same ratio to the volume of the steam when saturated, that ac had to ac. This gave in the figure at c

$$x_4 = \frac{ac}{ac} = \frac{0.94}{1.219} = 0.771.$$

To plot the point e on the temperature-entropy die Fig. 53, we may find the temperature at 90 pounds ab namely, 320° F., and on a line with that temperature as at nate we may interpolate between the lines for constant



of v. Other poir be drawn in a like ner, and the curve be sketched in; s' that the steam co to yield heat to the der walls from cut-is reached on Fig. perhaps a trifle Beyond c the ste ceives heat from the until exhaust oper

The same feature is exhibited in Fig. 52, by draw adiabatic line xdn from the point of cut-off. The point a located by multiplying the length ae, which represents the of steam in the cylinder when dry by the value of x aft batic expansion from the point of cut-off n. This poreadily included in the preceding investigation, so that x, determined. Locating n on the temperature-entropy d Fig. 53, we may draw through it a vertical constant entrand note where it cuts the lines corresponding to the lines like ae in Fig. 52, and interpolate for the value For example, the entropy at n in Fig. 53 appears to and at  $320^{\circ}$  F., which corresponds to 90 pounds, this line gives by interpolation 0.78, so that the length of ad

In this discussion no attempt is made to distinguish the which may be in contact with the wall from the rema steam and water in the cylinder. In reality that mois furnished the heat which the cylinder walls acquire admission, and it abstracts heat from the walls during th

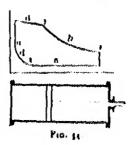
sion. The mixture, moreover, is not homogeneous, because the moisture on the cylinder walls is likely to be colder than the steam, though naturally it cannot be warmer.

Finally, the indicator-pencil is subject to a friction lng that operates to produce the effect shown by Figs. 52 and 53 and is liable to exaggerate them. That is to say, the pencil draws a horizontal line and tends to remain at the same height after the steam-pressure falls. It then lets go and falls sharply some little time after the valve has closed at cut-off. Afterwards it lags behind and shows a higher pressure than it should.

Hirn's Analysis. — Though the methods just illustrated give a correct idea of the influence of the walls of the cylinder of a steam-engine, our first clear insight into the action of the walls is due to Hirn,\* who accompanied his exposition by quantitative results from certain engine tests. The statement of his method which will be given here is derived from a memoir by Dwelshauvers-Dery.†

Let Fig. 54 represent the cylinder of a steam-engine and the diagram of the actual cycle. For sake of simplicity the diagram

is represented without lead of admission or release, but the equations to be deduced apply to engines having either or both. The points 1, 2, 3, and o are the points of cut-off, release, compression, and admission. The part of the cycle from o to 1, 1 that is, from admission to cut-off, is represented by a; in like manner, b, c, and d represent the parts of the cycle during expansion,



exhaust, and compression. The numbers will be used as subscripts to designate the properties of the working fluid under the conditions represented by the points indicated, and the letters will be used in connection with the operations taking place during the several parts of the cycle. Thus at cut-off the

<sup>\*</sup> Bulletin do la Soc. Ind. do Mulhouse, 1873; Théorie Méchanique de la Chalene, vol. il, 1876.

<sup>†</sup> Revue universelle des Mines, vol. vill, p. 362, 1880.

pressure is  $p_i$ , and the temperature, heat of the liquid, heat of vaporization, quality, etc., are represented by  $t_i$ ,  $q_i$ ,  $r_i$ ,  $x_i$ , etc. The external work from cut-off to release is  $W_i$ , and the heat yielded by the walls of the cylinder due to reëvaporation is  $Q_b$ .

Suppose that M pounds of steam are admitted to the cylinder per stroke, having in the supply-pipe the pressure p and the condition x; that is, each pound is x part steam mingled with 1 - x of water. The heat brought into the cylinder per stroke, reckoned from freezing-point, is

$$Q = M (q + xr) \dots \dots (153)$$

Should the steam be superheated in the supply-pipe to the temperature  $t_0$ , then

$$Q = M (r + q + \int cdl) . . . . . (154)$$

for which a numerical value can be found in the temperatureentropy table.

Let the heat-equivalent of the intrinsic energy of the entire weight of water and steam in the cylinder at any point of the cycle be represented by I; then at admission, cut-off, release, and compression we have

$$I_{0} = M_{0} (q_{0} + x_{0}\rho_{0}); ... ... ... (155)$$

$$I_{1} = (M + M_{0}) (q_{1} + x_{1}\rho_{1}); ... ... ... (156)$$

$$I_{2} = (M + M_{0}) (q_{2} + x_{2}\rho_{2}); ... ... ... (157)$$

$$I_{3} = M_{0} (q + x_{3}\rho_{3}); ... ... ... ... (158)$$

in which  $\rho$  is the heat-equivalent of the internal work due to vaporization of one pound of steam, and  $M_0$  is the weight of water and steam caught in the cylinder at compression, calculated in a manner to be described hereafter.

At admission the heat-equivalent of the fluid in the cylinder is  $I_o$ , and the heat supplied by the entering steam up to the point of cut-off is Q. Of the sum of these quantities a part,  $AW_a$ , is used in doing external work, and a part remains as intrinsic energy at cut-off. The remainder must have been absorbed by

the walls of the cylinder, and will be represented by  $Q_a$ . Hence

$$Q_a = Q + I_0 - I_1 - AW_a.$$

From cut-off to release the external work  $W_b$  is done, and at release the heat-equivalent of the intrinsic energy is  $I_2$ . Usually the walls of the cylinder, during expansion, supply heat to the steam and water in the cylinder. To be more explicit, some of the water condensed on the cylinder walls during admission and up to cut-off is evaporated during expansion. This action is so energetic that  $I_2$  is commonly larger than  $I_1$ . Since heat absorbed by the walls is given a positive sign, the contrary sign should be given to heat yielded by them; it is, however, convenient to give a positive sign to all the interchanges of heat in the equations, and then in numerical problems a negative sign will indicate that heat is yielded during the operation under consideration. For expansion, then,

$$Q_b = I_1 - I_2 - AW_b.$$

During the exhaust the external work  $W_e$  is done by the engine on the steam, the water resulting from the condensation of the steam in the condenser carries away the heat  $Mq_4$ , the cooling water carries away the heat  $G(q_k - q_i)$ , and there remains at compression the heat-equivalent of intrinsic energy  $I_2$ . So that

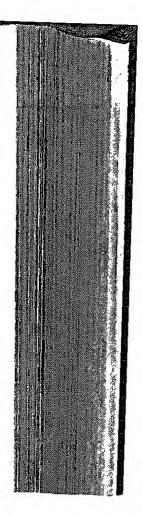
$$Q_0 = I_2 - I_4 - Mq_1 - G(q_k - q_1) + AW_0$$

in which  $q_i$  is the heat of the liquid of the condensed steam, and G is the weight of cooling water per stroke which has on entering the heat of the liquid  $q_i$ , and on leaving the heat of the liquid  $q_k$ .

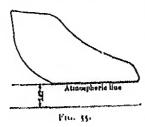
During compression the external work  $W_d$  is done by the engine on the fluid in the cylinder, and at the end of compression, i.e., at admission, the heat-equivalent of the intrinsic energy is  $I_0$ . Hence

$$Q_d = I_0 - I_0 + AW_d$$
.

It should be noted (Fig. 54) that the work  $W_a$  is represented



by the area which is bounded by the steam line, the ordinates through o and r and by the base line. And in like manner the works Wt, We, and Wa are represented by areas which extend to the base line. In working up the analysis from a test the



line of absolute zero of pressure may be drawn under the atmospheric line as in Fig. 55, or proper allowance may be made after the calculation has been made with reference to the atmospheric line.

For convenience these four equations will be assembled as follows:

$$Q_{\sigma} \cdots Q + I_{\sigma} \cdots I_{\tau} \sim AW_{\sigma} \qquad (150)$$

$$Q_{b} = I_{1} + I_{2} + AW + \dots$$

$$Q_{c} + I_{2} = I_{3} + Mq_{4} + G(q_{k} + q_{l}) + AW_{c}$$
(160)

$$Q_e - I_2 = I_3 - Mq_4 - G(q_4 - q_6) + AW_c$$
. (161)

$$Q_d = I_3 - I_0 + AW_d$$
 . . . . . . (162)

A consideration of these equations shows that all the quantities of the right-hand members can be obtained directly from the proper observations of an engine test except the several values of I, the heat equivalents of the intrinsic energies in the cylinder. These quantities are represented by equations (155) to (158), in which there are five unknown quantities, namely,  $x_0$ ,  $x_1$ ,  $x_2$ ,  $x_3$ , and  $M_0$ .

Let the volume of the clearance space between the valve and the piston when it is at the end of its stroke be Vo; and let the volumes developed by the piston up to cut-off and release be  $V_1$  and  $V_{2i}$  finally, let  $V_2$  represent the corresponding volume at compression. The specific volume of one pound of mixed water and steam is

and the volume of M pounds is

At the points of admission, cut-off, release, and compression,

There is sufficient evidence that the steam in the cylinder at compression is nearly if not quite dry, and as there is comparatively little steam present at that time, there cannot be much error in assuming

This assumption gives, by equation (166),

$$M_0 = \frac{V_0 + V_0}{u_0 + \sigma} = \frac{V_0 + V_0}{S_0} = (V_0 + V_0) \gamma_0 \quad . \quad (107)$$

in which  $\gamma_s$  is the density or weight of one cubic foot of dry steam at compression.

Applying this result to equations (263) to (265) gives

$$w_0 = \frac{V_0}{M_0 u_0} - \frac{\sigma}{u_0} \quad . \quad . \quad . \quad . \quad (168)$$

$$x_1 = \frac{V_0 + V_1}{(M + M_0)u_1} - \frac{\sigma}{u_1} \quad . \quad . \quad . \quad (thg)$$

$$x_2 = \frac{V_0 + V_2}{(M + M_0) u_1 - u_2} - \dots$$
 (170)

We are now in condition to find the values of  $I_{a_1}$   $I_{a_2}$  and  $I_{a_3}$  and consequently can calculate all the interchanges of heat by equations (159) to (162).

Should the value of x in any case appear to be greater than unity it indicates that the steam is superheated; this may happen for  $x_0$ , and then as the weight of steam  $M_0$  is relatively small, and as the superheating is usually slight, it will be sufficient to make  $x_0$  equal to unity. It is unlikely to be the case for  $x_1$  or  $x_2$ , even though the steam is strongly superheated in the steam-pipe;

should the computation give a value slightly larger than unity the steam may be assumed to be dry without appreciable error, and the work may proceed as indicated. If in the use of very strongly superheated steam a computed value of  $x_i$  is appreciably larger than unity, we may replace the equation (166) by

$$V_0 + V_2 = (M + M_0) v_2,$$

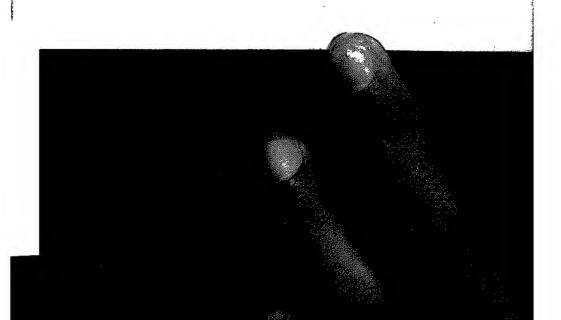
where  $v_2$  is the specific volume of superheated steam; consequently

 $v_2 = \frac{V_0 + V_1}{M + M_0}.$ 

By aid of the temperature-entropy table we may find (by interpolation if necessary) the corresponding temperature  $t_2$  and the value of the heat-contents or total heat. The heat-equivalent of the intrinsic energy is then equal to this quantity minus  $A p_2 v_2$ .

In the diagram, Fig. 54, the external work during exhaust is all work done by the piston on the fluid, since the release is assumed to be at the end of the stroke. If the release occurs before the end of the stroke, some of the work, namely, from release to the end of the stroke, will be done by the steam on the piston, and the remainder, from the end of the stroke back to compression, will be done by the piston on the fluid. In such case  $W_e$  will be the difference between the second and the first quantities. If an engine has lead of admission, a similar method may be employed; but at that part of the diagram the curves of compression and admission can be distinguished with difficulty, if at all, and little error can arise from neglecting the lead.

The several pressures at admission, cut-off, release, and compression are determined by the aid of the indicator-diagram, and the pressures in the steam-pipe and exhaust-pipe or condenser are determined by gauges. The weight M of steam supplied to the cylinder per stroke is best determined by condensing the exhaust-steam in a surface-condenser and collecting and weighing it in a tank. If the engine is non-condensing, or if it has a jet-condenser, or if for any reason this method cannot



be used, then the feed-water delivered to the boiler may be determined instead. The cooling or condensing water, either on the way to the condenser or when flowing from it, may be weighed, or for engines of large size may be measured by a metre or gauged by causing it to flow over a weir or through an orifice. The several temperatures  $l_4$ ,  $l_6$ , and  $l_8$  must be taken by proper thermometers. When a jet-condenser is used, and the condensing water mingles with the steam,  $l_4$  is identical with  $l_8$ . The quality x of the steam in the supply-pipe must be determined by a steam-calorimeter. A boiler with sufficient steam-space will usually deliver nearly dry steam; that is, x will be nearly unity. If the steam is superheated, its temperature  $l_6$  may be taken by a thermometer.

Let the heat lost by radiation, conduction, etc., be  $Q_e$ ; this is commonly called the radiation. Let the heat supplied by the jacket be  $Q_f$ . Of the heat supplied to the cylinder per stroke, a portion is changed into work, a part is carried away by the condensed steam and the cooling or condensing water, and the remainder is lost by radiation; therefore

$$Q_{e} = Q + Q_{j} - Mq_{i} - G(q_{k} - q_{i}) - A(W_{a} + W_{b} - W_{c} - W_{d}). (171)$$

The heat  $Q_i$  supplied by a steam-jacket may be calculated by the equation

$$Q_j = m (x'r' + q' - q'') \dots (172)$$

in which m is the weight of water collected per stroke from the jacket; x', r', and q' are the quality, the heat of vaporization, and the heat of the liquid of the steam supplied; and q'' is the heat of the liquid when the water is withdrawn. When the jacket is supplied from the main steam-pipe, x' is the same as the quality in that pipe. When supplied direct from the boiler, x' may be assumed to be unity. If the jacket is supplied through a reducing-valve, the pressure and quality may be determined either before or after passing the valve, since throttling does not change the amount of heat in the steam. Should

the steam applied to the jacket be superheated from any cause, we may use the equation

$$Q_f = m [r' + q' + c_p (t_{x'} - t') - q''], , . (173)$$

in which r' and q' are the heat of vaporization and heat of the liquid of saturated steam at the temperature l', and  $l_{z'}$  is the temperature of the superheated steam.

Equation (171) furnishes a method of calculating the heat lost by radiation and conduction; but since  $Q_s$  is obtained by subtraction and is small compared with the quantities on the right-hand side of the equation, the error of this determination may be large compared with  $Q_s$  itself. The usual way of determining  $Q_s$  for an engine with a jacket is to collect the water condensed in the jacket for a known time, an hour for example, when the engine is at rest, and then the radiation of heat per hour may be calculated. If it be assumed that the rate of radiation at rest is the same as when the engine is running, the radiation for any test may be inferred from the time of the test and the determined rate. But the engine always loses heat more rapidly when running than when at rest, so that this method of determining radiation always gives a result which is too small.

If a steam-engine has no jacket it is difficult or impossible to determine the rate of radiation. The only available way appears to infer the rate from that of some similar engine with a jacket. Probably the best way is to get an average value of  $Q_{\mathfrak{a}}$  from the application of equation (171) to a series of carefully made tests.

It is well to apply equation (171) to any test before beginning the calculation for Hirn's analysis, as any serious error is likely to be revealed, and so time may be saved.

When the radiation  $Q_s$  is known from a direct determination of the rate of radiation, we may apply Hirn's analysis to a test on an engine even though the quantities depending on the condenser have not been obtained. For from equation (171)



$$-Mq_{i}-G(q_{k}-q_{i})=Q_{e}-Q-Q_{i}+A(W_{a}+W_{b}-W_{c}-W_{d}),$$

and consequently

$$Q_c = I_2 - I_3 - Q - Q_I + Q_a + A (W_a + W_b - W_d) . . (174)$$

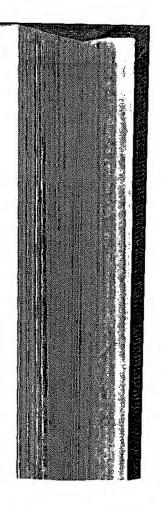
Thus it is possible to apply the analysis to a non-condensing engine or to the high-pressure cylinder of a compound engine.

It is apparent that the heat Q<sub>o</sub>, thrown out from the walls of the cylinder during exhaust, passes without compensation to the condenser, and is a direct loss. Frequently it is the largest source of loss, and for this reason Hirn proposed to make it a test of the performance and perfection of the engine; but such a use of this quantity is not justifiable, and is likely to lead to confusion.

The heat Q<sub>b</sub> that is restored during expansion is supplied at a varying and lower temperature than that of the source of heat, namely, the boiler, and, though not absolutely wasted, is used at a disadvantage. It has been suggested that an early compression, as found in engines with high rotative speed, warms up the cylinder and so checks initial condensation, thereby reducing Qa and finally Qa also. Such a storing of heat during compression and restoring during expansion is considered to act like the regenerator of a hot-air engine, and to make the efficiency of the actual cycle approach the efficiency of the ideal cycle more nearly than would be the case without compression. It does not, however, appear that engines of that type have exceeded, if they have equalled, the performance of slow-speed engines with small clearance and little compression.

Application. -- In order to show the details of the method of applying Hirn's analysis the complete calculation for a test made on a small Corliss engine in the laboratory of the Massachusetts Institute of Technology will be given. Its usefulness is mainly as a guide to any one who may wish to apply the method

for the first time.

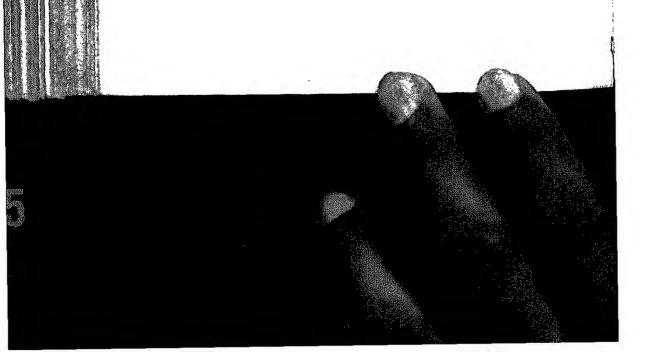


Diameter of the cylinder	· · · · · · · 8 Inches.
Stroke of the piston	a feet.
Piston displacement: crank end	o.6791 cu. ft.
head end	
Clearance, per cent of piston di	splacement:
crank end	3.75
hendend	
Boller-pressure by gauge	
Barometer	
Condition of steam, two per ce Events of the stroke:	nt of moisture.
Cut-off: crank end	
Release at end of stroke.	
Compression: crank end	o.o13 of stroke.
head end	
Duration of the test, one hour.	
Total number of revolutions	3692
Weight of steam used	548 pounds.
Weight of condensing water used	
Temperatures:	
Condensed steam	
Condensing water: cold	
warm	
MODE PUBLISHED THE TOTAL	TATIOTCATIO D_DTAGBAMS A

# \* ABSOLUTE PRESSURES, FROM INDICATOR-DIAGRAMS, AND CORRESPONDING PROPERTIES OF SATURATED STEAM.

department of the state of the second state of	CHARK KRD.					llwa	Кир.	
managa ay ay ay ay ay ay ay ay ay ay ay ay ay	1	٧	r	Washington Walter Company	*	4	P	н
Release Compression.	83.6 29.2 14.8 21.8	284.6 217.8 181.1	813.0 864.8 803.2 877.4	5.190 13.924 26.464 18.344	83.3 31.0 14.8 29.8	284.4 222.9 181.1 219.0	813.2 860.8 893.2 863.9	5.207 12.804 26.464 13.664

<sup>\*</sup> These values are taken from the first edition of the Tables of Properties of Saturated Steam.



# MEAN PRESSURES, AND HEAT-EQUIVALENTS OF EXTERNAL WORKS.

	CRANI	K END,	HEAD END.		
	Mean Pressures.	Equivalents of Work.	Mean Pressures.	Equivalents of Work.	
Admission Expansion	87.7 44.5 14.8 18.3	3.369 3.877 1.836 0.0299	89.3 47.1 14.8 21.8	3.711 4.159 1.847 0.1104	

#### VOLUMES, CUBIC FEET.

	CRANK END.	HEAD END.
At cut-off, $V_0 + V_1$	0.8333	0.2626
At release, Vo + V,		0.7396
At compression, $V_0 + V_1$	0.0343	0.0655 0.03806
At admission, Vo	0.02550	0.03806

At the boiler-pressure, 92.1 pounds absolute, we have

$$r = 888.4, \qquad q = 291.7.$$

The steam used per stroke is

$$M = \frac{548}{2 \times 3692} = 0.0742$$
 pound.

The steam caught in the clearance space at compression, on the assumption that the steam is then dry and saturated, is obtained by multiplying the mean volume at that point by the weight of one cubic foot of steam at the pressure at compression, which is 0.03781 of a pound.

:. 
$$M_0 = \frac{0.0343 + 0.0655}{2} \times 0.03781 = 0.0019$$
 of a pound;

$$M + M_0 = 0.0742 + 0.0019 = 0.0761$$
 pound.

The condensing water used per stroke is

$$G = \frac{14568}{2 \times 3692} = 1.973.$$

(/ = 11 (.17 + 4) = 0.0/.11(0.06 × 666.3 + 291.8) = 00.243;

$$x_0 = \frac{V_0}{M_0 u_0} = \frac{\sigma}{u_0}$$

$$\frac{\frac{1}{2} (0.02550 + 0.03806)}{0.0019 \times \frac{1}{2} (18.344 + 13.664)} = \frac{1}{62.4 \times \frac{1}{2} (18.344 + 13.664)}$$
= 1.043.

This indicates that the steam is superheated at admission. Such may be the case, or the appearance may be due to an error in the assumption of dry steam at compression, or to errors of observation. It is convenient to assume  $x_0 = 1$ .

$$x_1 = \frac{V_0 + V_1}{(M + M_0) u_1} - \frac{\sigma}{u_1};$$

$$\frac{\frac{1}{3}}{0.0761 \times \frac{1}{2}} \frac{(0.2333 + 0.2626)}{0.0761 \times \frac{1}{2}} \frac{1}{(5.190 + 5.207)} \frac{1}{62.4 \times \frac{1}{2}(5.190 + 5.207)}$$
= 0.6236.

$$x_2 = \frac{V_0 + V_2}{(M + M_0) u_1} = \frac{\sigma}{u_2};$$

$$I_0 = M_0 (q_0 + x_0 \rho_0);$$

... 
$$I_0 \approx \frac{1}{4} \times 0.0019 [201.5 + 219.0 + 1.00 (877.4 + 863.9)]$$
  
= 2.054.

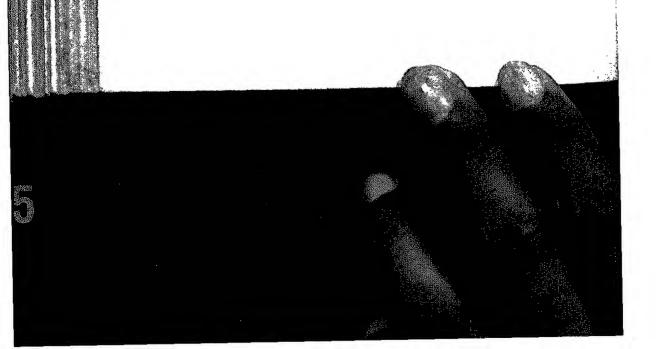
$$I_1 = (M + M_0) (q_1 + x_1 \rho_1);$$

:. 
$$I_1 = \frac{1}{2} \times 0.0761 [284.6 + 284.4 + 0.6236 (813.0 + 813.2)]$$
  
= 60.238.

$$I_1 = (M + M_0) (q_1 + x_2 \rho_1);$$

.. 
$$I_2 \longrightarrow \frac{1}{2} \times 0.0761$$
 [217.8 -1-222.0 -1-0.7088 (864.8 + 861.8)]  $\longrightarrow 63.311$ .

$$I_a = M_o(q_a + x_a \rho_a);$$



 $Q_a = Q + I_0 - I_1 - AW_a;$ 

 $\therefore Q_a = 86.243 + 2.054 - 60.238 - \frac{1}{2} (3.369 + 3.711) = 24.519.$ 

 $Q_b = I_1 - I_2 - AW_b;$ 

 $Q_b = 60.238 - 63.311 - \frac{1}{2}(3.877 + 4.159) = -7.091.$ 

 $Q_c = I_2 - I_3 - Mq_4 - G(q_k - q_i) + AW_c;$ 

 $Q_c = 63.311 - 2.041 - 0.0742 \times 109.3$  $-1.973(56.35-21.01)+\frac{1}{2}(1.836+1.847)$ 

= -14.721.

 $Q_d = I_1 - I_0 + AW_d;$ 

 $Q_d = 2.041 - 2.054 + \frac{1}{2}(0.0299 + 0.1104) = 0.157.$ 

 $Q_a = Q_a + Q_b + Q_c + Q_d = 2.764.$ 

Also, equation (171) for this case gives

 $Q_e = Q - Mq_4 - G(q_k - q_i) - AW$ 

= 86.243 - 8.110 - 69.723 - (3.540 + 4.018 - 1.841 - 0.070)

= 86.243 - 8.110 - 60.723 - 5.647 = 2.764.

It is to be remembered that the heat lost by radiation and conduction per stroke, when estimated in this manner, is affected by the accumulated errors of observation and computation, which may be a large part of the total value of  $Q_e$ .

Dropping superfluous significant figures, we have in B.T.U.

Q = 86.2

 $Q_a = 24.5,$   $Q_b = -7.1,$   $Q_d = .06,$   $Q_b = 2.8.$ 

Q = 86.2,  $Q_0 = -14.7,$ 

Noting that 5.647 are the B.T.U. changed into work per stroke and 3692 the total revolutions the horse-power of the engine is

$$\frac{778 \times 5.647 \times 3692 \times 2}{60 \times 33000} = 16.35 \text{ H.P.}.$$

and the steam per horse-power per hour is

$$\frac{548}{16.35}$$
 = 33.5 pounds.

For data and results of this test and others see Table IV.

APPLICATION OF HIRVS ANALYSIS TO A SMALL CORLESS ENGINE AT THE MASSACHUSETTS INSTITUTE OF TECHNOLOGY. TABLE IV.

1
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20272
NGRN;
c/S
DIAMETER.

	Administra.	H. F.	82,448		13t) 13t) 13t)	cated pawer, learn per hos learn per hos larer per hos	s l	6.53 8.08 8.08 8.73 8.73 39.0 11.13 35.3 16.35 33.5
	Adding to	7	* # 8 # 5			lation and rot. .aled	اہے۔ ایدن	20.1.2.2.2.2.2.2.2.2.2.2.2.2.2.2.2.2.2.2
DG.	Compression.	m m	2 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1	3	į	wheel by the duting inpression.	Syn	00000 12088
are po	2	C. E.	4444	24.0	'ਬ .	led by ills cluting hanse.	19/V	24.7.4
Alsoine presents, pounds	j l	ui mi	8 15 M M		Interchanges B.T.E.	ed by the during pausion,	14 G	11.65 1.65 1.05 1.05 1.05 1.05 1.05 1.05 1.05 1.0
Absolt	Reference	ς. Έ	5 CM 5			thed by the during mission.	cosclA nw don	20.01 22.26 31.28 23.30 24.53
	*i_	H.E.	4.7 1.8 4.000			th alter lo alter annyla tak	and O	3.12.32.38 5.28.52.4
	S. E.	ς. Έ.	1:27:11	83.6		Com-	描	90000 81801
ije: a jik	inasaid-təl Muud Jahus J	1011 &	20 1.48 1. 1. 0 2.48 1.				E. C.E	73 0.052
olin atan	uorg "1939m Fotkupa eili	atAff Frid	wi.ex		equivalents of work.	Exhanc.	C. E. H. J	1.81.1 1.82.1 1.83.1 1.83.1 1.84.8 1.
ند ا	-Arrienelm -mraw, ante		7.881	26.3	d-equivale B.T	Promision.	я 1	444444
Tonpenmen. depos Februados	idenalng. Ist cold.	RW G	*****		Hos	*****	1 H	0.070 2.486 3.285 1.033 3.285
Total	beaneh. .ma	10() 4 914 4	65 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5	2 2		Admission.	C.F. H	0 1 1 6 0 1
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1919	i of conilei saiar, pion	laly VV V-aul	25.00	1,58	o beginni		<u>     </u>   <u>     </u>	8 8 8 8 8 8 8 8 8 8 8 8 8 8 8 8 8 8 8
gs.4140 + 90	magra let ri Abrinces	IglaW been	375	£Z	rems of the Strake —	Reisse	Hi Li	8888
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	stunim, no	lianuct	888	₩8	N N	Caron	и 0	0 2 0 4

Effect of Varying Cut-off. — An inspection of the interchanges of heat shows that the values of  $Q_a$ , the heat absorbed by the walls during admission, increase regularly as the cut-off is lengthened, and that the heat returned during expansion decreases at the same time, so that there is a considerable increase in the value of the heat  $Q_a$  which is rejected during exhaust. Nevertheless there is a large gain in economy from restricting the cut-off so that it shall not come earlier than one-third stroke. Unfortunately tests on this engine with longer cut-off than one-third stroke have not been made, and consequently the poorer economy for long cut-off cannot be shown for this engine as for the engine of the *Michigan*.

Hallauer's Tests. — In Table V are given the results of a number of tests made by Hallauer on two engines, one built by Hirn having four flat gridiron valves, and the other a Corliss engine having a steam-jacket. Two tests were made on the former with saturated steam and six with superheated steam. Three tests were made on the latter with saturated steam and with steam supplied to the jackets. These tests have a historic interest, for though not the first to which Hirn's analysis was applied, they are the most widely known, and brought about the acceptance of his method. They have also a great intrinsic value, as they exhibit the action of two different methods of ameliorating the effect of the action of the cylinder walls, namely, by the use of superheated steam and of the steam-jacket. In all these tests there was little compression, and  $Q_d$ , the interchange of heat during compression, is ignored.

Superheated Steam. — Steam from a boiler is usually slightly moist, x, the quality, being commonly 0.98 or 0.99. Some boilers, such as vertical boilers with tubes through the steam space, give steam which is somewhat superheated, that is, the steam has a temperature higher than that of saturated steam at the boiler-pressure. Strongly superheated steam is commonly obtained by passing moist steam from a boiler through a coil of pipe, or a system of piping, which is exposed to hot gases beyond the boiler.

TABLE V.

TESTS ON A HIRN AND A CORLISS ENGINE

By HALLAUTH, Bulletin de la Soc. Ind. de Musicour, val XIVII, 18-7.

M.T. It, rejected per atroles,	ઢ	147	7.888321	3 3 3
đ	8		Processing the Control of the Contro	1.0.4 1.0.4
Extenges of hear in per cent of ural hear furnished per stroke.	ঙ	1.0.1	9 . п то .	1.65
4 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1	Ġ	25.6	2. 0. 1. 1. 1. 1. 1. 1. 1. 1. 1. 1. 1. 1. 1.	12.08 8.08 0.08
mgra of 1 head form	3	10.12	w . v	17.5
4	đ	28.3	4 · O · · ·	26.4 21.1 15.4
LTAD, per 11. P. per minute.	ľ	33.85	8 8 8 8 8 E	
lishm per 11, 11, ser hour, pounds.	1	22.53	20.02	17.8
lloree-power,	Br. e-Milong	134.6	134.0 142.4 142.4 124.5 89.6	103.6 129.1 155.9
ilack-tytesaure, ibsolute, pounda ibsolute, per square loch.	anessty-dad! almog (slufosda .tlad stups req		************	и и й н 40
foller-pressure, about, telufosda per square inch,		20.7	1. 1. 8. 8. 1. 8. 1. 0. 6. 4. 6. 1.	**************************************
.anolannqu3(	เลยอร์ลศาจุกไร้		A 4.04 4.00	500
Revolutions per inlaute,	Hevalutions per infinite,		8 8 8 8 8 8 8 6 6 6 8 8 8 8 8	50.4 51.1 49.3
onuparques!' questa belaniteque,	onnanguasT unasia bajaodioqua		8 14 4 4 4 4 4 4 4 4 4 4 4 4 4 4 4 4 4 4	
Condition.		т тоб. Фанцуудуу туруу	Buparhedica	Jacketed

\* Non-condensing. † The true value is probably zero. The throttle-value was partly closed for 6, 7, and 8.

Superheated steam may yield a considerable amount of heat before it begins to condense; consequently where superheated steam is used in an engine a portion of the heat absorbed by the walls during admission is supplied by the superheat of the steam and less condensation of steam occurs. This is very evident in Dixwell's tests given by Table XXV, on page 271, where the water in the cylinder at cut-off is reduced from 52.2 per cent to 27.4 per cent, when the cut-off is two-tenths of the stroke, by the use of superheated steam; with longer cut-off the effect is even greater. This reduction of condensation is accompanied by a very marked gain in economy.

The way in which superheated steam diminishes the action of the cylinder walls and improves the economy of the engine is made clear by Hallauer's tests in Table V. A comparison of tests 1 and 3, having six expansions, shows that the heat Q<sub>a</sub> absorbed during admission is reduced from 28.3 to 22.4 per cent of the total heat supplied, and that the exhaust waste is correspondingly reduced from 21.6 to 12.5 per cent. A similar comparison of tests 2 and 5, having nearly four expansions, shows even more reduction of the action of the cylinder walls. The effect on the restoration of heat  $Q_b$  during expansion appears to be contradictory: in one case there is more and in the other case less. It does not appear profitable to speculate on the meaning of this discrepancy, as it may be in part due to errors and is certainly affected by the unequal degree of superheating in tests 3 and 5. It may be noted that the actual value of  $Q_{\epsilon}$  in calories is nearly the same for tests 1 and 2, there being a small apparent increase with the increase of cut-off, which is, however, less than the probable error of the tests. The exhaust waste  $Q_c$ is much more irregular for tests 3 to 7 for superheated steam. The increase from 81 to 87 B.T.U. from test 6 to test 7 may properly be attributed to a less degree of superheating; the increase from 66 to 81 B.T.U. for tests 5 and 6 is due to longer cut-off and less superheating; finally, the steady reduction from 75 to 66 B.T.U. for the three tests 3, 4, and 5 is probably due to the rise of temperature of the superheated steam, which more than compensates for the effect of lengthening the cut-off, Finally in test 8 the exhaust waste is practically reduced to zero by the use of strongly superheated steam in a non-condensing engine; this shows clearly that the exhaust waste  $Q_{\epsilon}$  by itself is no criterion of the value of a certain method of using steam.

Steam-Jackets. - If the walls of the cylinder of a steamengine are made double, and if the space between the walls is filled with steam, the cylinder is said to be steam-jacketed. Both barrel and heads may be jacketed, or the barrel only may have a jacket; less frequently the heads only are jacketed. The principal effect of a steam-jacket is to supply heat during the vaporization of any water which may be condensed on the cylinder walls. The consequence is that more heat is returned to the steam during expansion and the walls are hotter at the end of exhaust than would be the case for an unjacketed engine. This is evident from a comparison of tests 1 and 11 in Table V. In test I only a small part of the heat absorbed during admission is returned during expansion, and by far the larger part is wasted during exhaust. In test 11 the heat returned during expansion is equal to two-thirds that absorbed during admission, though a part of this heat of course comes from the jacket. About half as much is wasted during exhaust as is absorbed during admission. The condensation of steam is thus reduced indirectly; that is, the chilling of the cylinder during expansion, and especially during exhaust, is in part prevented by the jacket, and consequently there is less initial condensation and less exhaust waste, and in general a gain in economy. The heat supplied during expansion, though it does some work, is first subjected to a loss of temperature in passing from the steam in the jacket to the cooler water on the walls of the cylinder, and such a nonreversible process is necessarily accompanied by a loss of efficlency. On the other hand, the heat supplied by a jacket during exhaust passes with the steam directly into the exhaust-pipe. It appears, then, that the direct effect of a steam-jacket is to waste heat; the indirect effect (drying and warming the cylinder)



educes the initial condensation and the exhaust waste and often

gives a notable gain in economy.

Application to Multiple-expansion Engines. - The application of Hirn's analysis to the high-pressure cylinder of a compound or nultiple-expansion engine may be made by using equations (150), (160), and (162) for calculating  $Q_a$ ,  $Q_b$ , and  $Q_d$ , while equation (174) may be used to find  $Q_o$ .

A similar set of equations may be written for the next cylinder, whether it be the low-pressure cylinder of a compound engine or the intermediate cylinder of a triple engine, provided we can determine the value of Q', the heat supplied to that cylinder. But of the heat supplied to the high-pressure cylinder a part is changed into work, a part is radiated, and a part is rejected in the exhaust waste. The heat rejected is represented by

$$Q + Q_I - AW - Q_e . . . . . . (175)$$

where Q is the heat supplied by the steam entering the cylinder, Q is the heat supplied by the jacket, AW is the heat-equivalent of the work done in the cylinder, and Q, is the heat radiated. Suppose the steam from the high-pressure cylinder passes to an intermediate receiver, which by means of a tubular reheater or by other means supplies the heat Q<sub>r</sub>, while there is an external radiation Qre. The heat supplied to the next cylinder is consequently -

 $Q' = Q + Q_i - AW - Q_o + Q_r - Q_{ro}$  . (176)

In a like manner we may find the heat Q" supplied to the next cylinder; for example, to the low-pressure cylinder of a triple engine.

It is clear that such an application of Hirn's analysis can be made only when the several steam-jackets on the high- and the low-pressure cylinders, and the reheater of the receiver, etc., can be drained separately, so that the heat supplied to each may be determined individually.

Table VI gives applications of Hirn's analysis to four tests on the experimental triple-expansion engine in the laboratory of the Massachusetts Institute of Technology.

It will be noted that the steam in the cylinders becomes drier in its course through the engine, under the influence of thorough steam-jacketing with steam at boiler-pressure, and is practically dry at release in the low-pressure cylinder. All of the tests show superheating in the low-pressure cylinder, which is of course possible, for the steam in the jackets is at full boiler-pressure while the steam in the cylinder is below atmospheric pressure. The superheating was small in all cases—not more than would be accounted for by the errors of the tests. The exhaust waste  $Q_e$ " from the low-pressure cylinder in the triple-expansion tests is very small in all cases—less than two per cent of the heat supplied to the cylinders. The apparent absurdity of a positive value for  $Q_e$ " in two of the tests (indicating an absorption of heat by the cylinder walls during exhaust) may properly be attributed to the unavoidable errors of the test.

In the fourth test, when the engine was developing 120.3 horse-power, there were 1305 pounds of steam supplied to the cylinders in an hour, and 3.15 pounds to the steam-jackets; so that the steam per horse-power per hour passing through the cylinders was

1305 + 120.3 - 10.86 pounds,

while the condensation in the jackets was

345 + 120.3 - 2.87 pounds.

So that, as shown on page 145, the B.T.U. per horse-power per minute supplied to the cylinders by the entering steam was 191.1, while the jackets supplied 40.6 B.T.U., making in all 231.7 B.T.U. per horse-power per minute for the heat-consumption of the engine. In the same connection it was shown that the thermal efficiency of the engine for this test was 0.183, while the efficiency for incomplete expansion in a non-conducting cylinder corresponding to the conditions of the test was 0.222; so that the engine was running with 0.824 of the possible efficiency. In light of this satisfactory conclusion some facts with regard to the test are interesting.

# TABLE VI.

APPLICATION OF HIRN'S ANALYSIS TO THE EXPERIMENTAL ENGINE IN THE LABORATORY OF THE MASSACHUSETTS INSTITUTE OF TECHNOLOGY.

TRIPLE-EXPANSION; CYLINDER DIAMETERS, 9, 16, AND 24 INCHES; STROKE, 30 INCHES.

Trans. Am. Soc. Mech. Engrs., vol. xil, p. 740.

	t.	11.	111.	IV.
Duration of test, minutes Total number of revolutions Revolutions per minute Steam-consumption during test, liba.:	60 5200 88.3	60 5228 87.1	60 5173 86.2	60 5148 85.8
Passing through cylinders Condensation in h.p. Jacket in first receiver-jacket in inter. jacket jn second receiver-jacket	1193 57 61 85	1157 50 64 92 50	1234 20 60 97 52	1305 30 72 105
in t.p. jacket	53 80	76	90	87
Total	1238	1489 I	1571	1650
Condensing water for test, lbs Priming, by calorimeter	0.013	0.012 0.012	0.011	0.012
Condensed steam	95.4	93.1 42.1	102.4	105.3 42.8
Condensing-water, hot	96.1 14.8	96.6 14.8	106.3	109.6
Boiler pressure, llis. per sq. in. also-	155-3	155.5	156.9	14.7
Vacuum in condenser, inches of mer- cury	25.0	25. I	24.1	23.9
High-pressure cylinder — Cut-off, crank and	0.102	0.194	0.245	
head end	0.215			0.183
Release, both ends	1,00	1.00	1,00	1.00
Compression, crank end	0.05	0.05	0.01	0.04
head end	0.05	0.05	0.05	0.05
Cut-off, both ends	0.20	0.20		0.00
Release, both ends	1.00	1.00	1.00	1.00
Compression, crank end	0.03	0.03	0.03	0.03
head end	0.04	0.04	0.04	0.04
Low-pressure cylinder		,		
Cut-off, crank and	0.38	0.38	0.38	0.38
head end	0.39	0.39	0.39	0.39
Release, both ends	1,00	1.00	1.00	1.00
		<del></del>	<del></del>	<del>'</del>

TABLE VI -- Continued.

	ı.	n.	m.	۱۷.
	Ι.		**********	
desolute pressures in the cylinder,	ì	1	1	
panings per sq. in.;	i	1	1	
High pressure cylinder	, i	1	i	
Cut off, crank end	145.0	145.0	138.8	138,3
head cul	143.4	143.1	140.3	140.6
Release, rank end	41.3	41.5	44.7	48.4
head call	41.5	40.5	45.7	49.8
Compression, crank end	13.7	45-3	48.5	53.2
head end	48.7		54.5	62.0
Admission, crank end	64.5	47.0 68.8	72.2	81.2
hend end	75.3	74.8	86.7	97.8
Intermediate cylinder	7.1.3	, I		971.0
Cut off, crank end	37.4	37.6	38.6	40.0
	35.0	35.3	39.6	42.6
head cod	13.6	14.2	14.7	16.0
Release, crank end	13.4	13.8	14.9	16.0
head cud	10.3	17.3	18.2	10.0
	17.0	18.8	20.3	22.4
head end	10.1	20.8	22.2	23.1
Admission, crank end	J1.1	8,44	24,2	26.7
head end	""		-41	
Law-pressure cylinder	(3.3	12.0	12.4	13.2
Cut off, crank and	(2.0	12.4	13.1	14.0
head end	5.6		5.1	5.7
Release, trank end		5.3 5.8	5.0	6.4
hend end	5.4	3	1 3.7	",
Compression and admission		3.8	4.1	4.2
trank ritt	3.7	1.5	4.6	4.7
head end	4-3	1 7.3	1 7	1 7.7
Heat equivalents of external work,			1	ŀ
n.r.u., from a reason indicator		}	}	İ
dlagram to line of absolute vacuum	1	1	1	1
High pressure cylinder		1		
During admission,		5.78	7.00	8.
All's crank and	5.71		8.42	9.
head end	0.60	6.37	1	, r
During expansion,		10.76	10.40	10.
All's, crank ond	10.05			11.
head end	. 10.81	1 11.00	1	1
During exhaust,		7.80	8.44	9.0
All's crank end	7.73	1 6.2		
head end	. n.on	8.15	1,0.1	'``
During compression,		0.00	0.40	0.
Alf a crank end	0.48			
hendend	. 0.62	0.64	1 9.73	' i
Intermediate cylinder	1	1	1	1
During admission,	1		7.98	8.
All'A crank end	· 7.5			, s.
head end	7-43	1 7.55	1 9.4	′  "
During extransion,				10.
All's crank and	9.50			
	, g.a.	1 9.3		

TABLE VI - Continued.

	ĭ.	II.	III.	īv.
Intermediate cylinder —				
During exhaust,	J		. ]	
AW, crank end	9.27	9.47	9.64	10.54
head end	9.27	9.47	10.18	10.84
During compression,	3,7,	9147	10,10	22704
AWa', crank end	0.39	0.43	0.57	0.46
head end	0.60	0.70	0.78	0.84
Low-pressure cylinder —		,-		•
During admission.	- 1	1		
AWa", crank end	7.75	7.95	8.33	8.97
head end	7.99	7·95 8.19	8.66	9.39
During expansion,		· l		
AW, crank end	6.83	7.10	6.86	7.45
head end	6.87	7.12	7 - 34	7.87
During exhaust,				
AW, crank end	5.08	5.08	4.62	5.09
head end	5.08	5.16	4.81	5.00
During compression,			- 1	
AWa", crank end	0.00	0.00	0.00	0.00
head end	0.00	0.00	0.00	0.00
Quality of the steam in the cylinder				
At admission and at compression	- 1		,	
the steam was assumed to be dry		, i		
and saturated:				
High-pressure cylinder —	0_		0.848	0.875
At cut-off $x_1$ . At release $x_2$ .	0.785 0.899	0.784	0.920	
At release	0.099	0.903	0.920	0.931
At cut-off $\dots$ $x'$ .	0.899	0.912	0.906	0.908
At cut-off $x_1'$ .  At release $x_2'$ .	0.994	* * *	* * *	* * *
Low-pressure cylinder	0.994			
At cut-off	0.078	* * *	0.970 * * *	0.974
At release $\dots x_2''$ .	* * *	* * *	* * *	* * *
Interchanges of heat between the				
steam and the walls of the cylin-			- 1	
ders, in u. T. v. Quantities			i }	
affected by the positive sign are				
absorbed by the cylinder walls;				
quantities affected by the negative	- 1		ĺ	
sign are yielded by the walls:				
High-pressure cylinder —	ì			
Brought in by steam . Q	132.93	130.77	141.11	149.84
During admission Q	23.51	23.43	17.49	14.93
During expansion $Q_b$	-18.69	-19.28	-15.33	-14.03.
	- 8.36	- 7.22	- 3.50	- 2.38
During compression Q <sub>d</sub>	0.45	0.51	0.49	0.52
Supplied by jacket Q,	4.56	4.08	2.39	2.50
Lost by radiation Q	1.50	. 1.52	1.54	1.54
First intermediate				
First intermediate receiver —		P 00	- 6-	F 04
First intermediate receiver — Supplied by jacket Q <sub>r</sub> Lost by radiation Q <sub>r</sub>	4.92	5.20	5.67 0.59	5.95 0.59

<sup>\*</sup> Superheated.

TABLE VI - Continued,

power and the second section of the second section of the second section of the second section of the second section of the second section sec		o the contract of the generalization of		
	I. [	11.	m.	1٧.
•••	ĺ			
Intermediate cylinder	}		,	
Brought in by steam . Q'	131.80	129.61	137.87	
During admission Q.	13.04	11.24	11.33	116.64
During expansion (4'	18,65	18.84	20.30	11.75
During exhaust O.	0. 33	1.57	2.88	-21.88
During compression Q.	0.44	0.51	0.62	3.41
Supplied by Jacket Q'	6.83	7.50	7.97	0.59
Land by radiation Q'	2.45	រ.្មីន 🏻	3.50	8.64
Second intermediate receiver			-,34	. 2.51
Supplied by Jacket Q'	g.20 J	4.04	4.27	4.45
Last by radiation On'	1.30	1.32	1.23	4.22
Law pressure cylinder	Į.			1.24
Brought in by steam . O"	430.14	130.50	138.61	119.44
During nelmission (4"	5.85	3.05		147.33 5.20
During expansion Ch' .	9.50	7.00	· 8.65	→ 10.13
Disting exhibits	P - 53 (	4.43	* 1.44	11.0
During compression Q." .	O, GO	0,00	0.00	0.00
Sombled by in ket O'' 1	7. OH (	6.30	7.41	7.14
Lant by radiation Q."	4 - 34	4.40	4.45	4-47
Total loss by fadilation				7.11
lly preliminary tests . X(4 )	10.67	10.20	10.31	10.35
By equation (171).	Ra. r.i	to, to	8.75	8.07
Pawer and economy:	- 1			-1
Heat equivalents of works per	1			
blenke	6.2			
H.P. cylinder All'	H. 44	н, да	9.17	9.51
Internacylluder AB'	7.11	6.95	7.77	8.42
L. P. cylinder AW"	g.61)	10.00	10.87	11.70
			~ · ~ · · · · · · · · · · · · · · · · ·	
Tatala	25. JO	45.35	37.81	29.73
			ì	
Total heat furnished by fackets	27.58	27.02	27.71	28.45
Distribution of work				
High pressure cylinder	t . Corr	1.00	1.00	1.00
Intermediate cylinder	0.84	a,83	0.85	0.88
Low pressure cylinder	1.14	1.71	1.19	1.24
Horse-paiwer	104.0	104.3	113.1	120.3
Steam per H.P. per luge	14.05	19.31	13.90	13.73
If TAU, per H.P. per infinite (1995)	147	441	230	333
·			· · · · · · · · · · · · · · · · · · ·	The state of the s

It will be noted that for test IV 1.10.84 n.T.U. per stroke are brought in by the steam supplied to the high-pressure cylinder and that 28.45 n.T.U. per stroke are supplied by the steam-jackets; and that, further, 20.73 n.T.U. are changed into work while 10.35 are radiated. Thus it appears that the jackets furnished almost as much heat as was required to do all the work developed. Of the heat furnished by the jackets something more than a third

was radiated; the other two-thirds may fairly be considered to have been changed into work, since the exhaust waste of the low-pressure cylinder was practically zero.

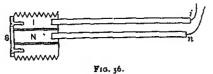
Quality of Steam at Compression. - In all the work of this chapter the steam in the cylinder at compression has been considered to be dry and saturated, and it has been asserted that little if any error can arise from this assumption. It is clear that some justification for such an assumption is needed, for a relatively large weight of water in the cylinder would occupy a small volume and might well be found adhering to the cylinder walls in the form of a film or in drops; such a weight of water would entirely change our calculations of the interchanges of heat. The only valid objection to Hirn's analysis is directed against the assumption of dry steam at compression. Indeed, when the analysis was first presented some critics asserted that the assumption of a proper amount of water in the cylinder is all that is required to reduce the calculated interchanges of heat to zero. It is not difficult to refute such an assertion from almost any set of analyses, but unfortunately such a refutation cannot be made to show conclusively that there is little or no water in the cylinder at compression; in every case it will show only that there must be a considerable interchange of heat.

For the several tests on the Hirn engine given in Table V, Hallauer determined the amount of moisture in the steam in the exhaust-pipe, and found it to vary from 3 to 10 per cent. Professor Carpenter \* says that the steam exhausted from the high-pressure cylinder of a compound engine showed 12 to 14 per cent of moisture. Numerous tests made in the laboratory of the Massachusetts Institute of Technology show there is never a large percentage of water in exhaust-steam. Finally, such a conclusion is evident from ordinary observation. Starting from this fact and assuming that the steam in the cylinder at compression is at least as dry as the steam in the exhaust-pipe, we are easily led to the conclusion that our assumption of dry steam is proper. Professor Carpenter reports also that a calorimeter

<sup>\*</sup> Trans. Am. Soc. Mech. Engrs., vol. xii, p. 811.

test of steam drawn from the cylinder during compression showed little or no moisture. Nevertheless, there would still remain some doubt whether the assumption of dry steam at compression is really justified, were we not so fortunate as to have direct experimental knowledge of the fluctuations of temperature in the cylinder walls.

Dr. Hall's Investigations. — For the purpose of studying the temperatures of the cylinder walls Dr. E. H. Hall used a thermo-electric couple, represented by Fig. 56. I is a cast-



iron plug about three-quarters of an inch in diameter, which could be screwed into the hole provided for attaching an indicator-cock to the

cylinder of a steam-engine. The inner end of the plug carried a thin cast-iron disk, which was assumed to act as a part of the cylinder wall when the plug was in place. To study the temperature of the outside surface of the disk a nicket rod N was soldered to it, making a thermo-electric couple. Wires from I and N led to another couple made by soldering together cast-iron and nickel, and this second couple was placed in a bath of parassine which could be maintained at any desired temperature. In the electric circuit formed by the wires joining the two thermo-electric couples there was placed a galvanometer and a circuit-breaker. The circuit-breaker was closed by a cam on the crank-shaft, which could be set to act at any point of the revolution. If the temperature of the outside of the disk S differed from the temperature of the parasine bath at the instant when contact was made by the cam, a current passed through the wires and was indicated by the galvanometer. By properly regulating the temperature of the bath, the current could be reduced and made to cease, and then a thermometer in the bath gave the temperature at the surface of the disk for the instant when the cam closed the electric circuit. Two points in the steam-cycle were chosen for investigation, one immediately after cut-off and the other immediately after compression, since they gave the means of investigating the heat absorbed during compression and admission of steam, and the heat given up during expansion and exhaust.

Three different disks were used: the first one half a millimetre thick, the second one millimetre thick, and a third two millimetres thick. From the fluctuations of temperature at these distances from the inside surface of the wall some idea could be obtained concerning the variations of temperature at the inner surface of the cylinder, and also how far the heating and cooling of the walls extended.

The account given here is intended only to show the general idea of the method, and does not adequately indicate the labor difficulties of the investigation which involved many secondary investigations, such as the determination of the conductivity of nickel. Having shown conclusively that there is an energetic action of the walls of the cylinder, Dr. Hall was unable to continue his investigations.

Callendar and Nicolson's Investigations.—A very refined and complete investigation of the temperature of the cylinder walls and also of the steam in the cylinder was made by Callendar and Nicolson\* in 1895 at the McGill University, by the thermo-electric method.

The wall temperatures were determined by a thermo-electric couple of which the cylinder itself was one element and a wrought-iron wire was the other element. To make such a couple, the cylinder wall was drilled nearly through, and the wire was soldered to the bottom of the hole. Eight such couples were established in the cylinder-head, the thickness of the unbroken wall varying from 0.01 of an inch to 0.64 of an inch. Four pairs of couples were established along the cylinder-barrel, one near the head, and the others at 4 inches, 6 inches, and 12 inches from the head. One of each pair of wall couples was bored to within 0.04 of an inch, and the other to 0.5 of an inch of the inside surface of the cylinder. Other couples were established along the side of the cylinder to study the flow of heat from the

<sup>\*</sup> Proceedings of the Inst. Civ. Engrs., vol. cxxxii.

head toward the crank end. The temperature of the steam near the cylinder head was measured by a platinum thermometer capable of indicating correctly rapid fluctuations of temperature.

The engine used for the investigations was a high-speed engine, with a balanced slide valve controlled by a fly-wheel governor. During the investigations the cut-off was set at a fixed point (about one lifth stroke), and the speed was controlled externally. By the addition of a sufficient amount of lap to prevent the valve from taking steam at the crank end the engine was made single acting. The normal speed of the engine was sporevolutions per minute, but during the investigations the speed was from 40 to 60 revolutions per minute. The diameter of the cylinder was 10.5 inches and the stroke of the piston was 12 inches. The clearance was ten per cent of the piston displacement.

From the indicator diagrams an analysis, nearly equivalent to Hirn's analysis, showed the heat yielded to or taken from the walls by the steam; on the other hand the thermal measurements gave an indication of the heat gained by or yielded by the walls. The results are given in the following table; and considering the difficulty of the investigation and the large allowance for leakage, the concordance must be admitted to be very satisfactory.

TABLE VII.

INFRUENCE OF THE WALLS OF THE CYLINDER,
CALLSTIAN ASTONIOUS, Proc. Int. Civ. Engr., 1897.

	;	l.	11	111.	ıv.	v.	Vi.	VH.
finite study to order process 4 and 4 St. 4 78 9 to 107 7-7-118	the eductions for endouse them gauge proceeds them gauge proceeds them advant for the eduction to have get the eduction that get the eduction that the them the eduction the them taught at the endouse educate the tight of the test end to end one test and decare at quantum area as test and test educate of the one test para at their educate educate the test and to expend to as the table of each of the table of expendation the table of expendation the table of expendation the table of expendation the table of expendation the table of expendation the table of expendation the table of expendation the table of expendation the table of expendation the table of expendation the table of expendation the table of expendation the table of table table of table table of table table of table table of table ta	表生 教	新聞 書きま 外別 声 い を考ます い のを記さい は 知さいを コ コをき マ コをき マ コをき マ コをき マ コをき マ コをき マ コをき マ コをき マ コをき マ コをき マ コをき マ コをき マ コ で で で で で で で で で で で で で で で で で で	The design of the control of the con	ya 4  Dg 1  Dg 1  To 1004  To	71 4 01 0 2 1036 2 1036 2 0037 2 0.400 0 0068 1 0307 0 0304 0 0416 0 0416 0 0611 0 0611	35 81.7 94.2 9.1000 0.0376 0.0424 0.0100 0.0310 0.0454 0.0030 0.0030 0.0050 0.0050 0.0010	25 07-0 90-8 0-049 0-049 0-049 0-049 0-049 0-001 0-001 0-001 0-001

The platinum thermometer near the cylinder-head showed superheating throughout compression, thus confirming our idea that steam can be treated as dry and saturated at the beginning of compression. This same thermometer fell rapidly during admission and showed saturation practically up to cut-off, as of course it should; after cut-off it began again to show a temperature higher than that due to the indicated pressure, which shows that the cylinder-head probably evaporated all the moisture from its surface soon after cut-off. If this conclusion is correct, there would appear to be little advantage from steam jacketing a cylinder-head, a conclusion which is borne out by tests on the experimental engine at the Massachusetts Institute of Technology.

The following table gives the areas, temperatures, and the heat absorbed during a given test by the various surfaces exposed to steam at the end of the stroke, i.e., the clearance surface.

TABLE VIII.

CYCLICAL HEAT-ABSORPTION FOR CLEARANCE SURFACES.

Portions of surface considered.	Area of surface, aquare feet.	Mean temperature,	lical almorbed 11.7° 11. per minute.		
Cover face, 10.5 Inches diameter	0.60	305	Bo		
Cover side, 3.0 inches	0.70	305	70		
Piston face, 10.5 inches diameter	ດ.ດັດ	305	110		
Piston side, 0.5 inch	0.11	205	40		
Barrel side, 3.0 inches	0.71	207	1/3		
Counterbore, 0.5 Inch	0.12	101	I A		
Ports and valves	0.00	305	101		
	mercy in a right.	41	is a successive of the paper of		
Sums and means	3 - 7 - 1	101	5,10		

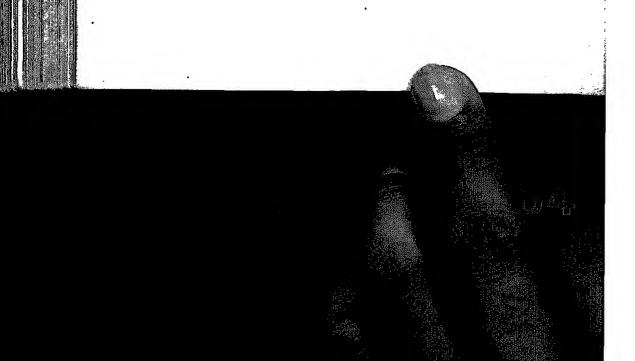
The heat absorbed by the side of the cylinder wall uncovered by the piston up to 0.25 of the stroke was estimated to be 55 B.T.U. per minute, which added to the above sum gives 585 B.T.U.; from which it appears that 90 per cent of the condensation is chargeable to the clearance surfaces, which were exceptionally large for this type of engine. Further inspection shows that the condensation on the piston and the barrel is much more

energetic than on the cover or head. For example, the face of the piston absorbs 110 B.T.U., while the face of the cover absorbs only 68 B.T.U., and the sides of the cover and of the barrel, each 3 inches long, absorb 79 and 123 B.T.U. respectively. This relatively small action of the surface of the head indicates in another form that less gain is to be anticipated from the application of a steam-jacket to the head than to the barrel of a steam-engine.

The exposed surfaces at the side of the cylinder-head and the corresponding side of the barrel are due to the use of a deeply cored head which protrudes three inches into the counterbore of the cylinder, and which has the steam-tight joint at the flange of the head. It would appear from this that a notable reduction of condensation could be obtained by the simple expedient of making a thin cylinder-head.

Leakage of Valves. —Preliminary tests when the engine was at rest showed that the valve and piston were tight. The valve was further tested by running it by an electric motor when the piston was blocked, the stroke of the valve being regulated so that it did not quite open the port, whereupon it appeared that there was a perceptible but not an important leak past the valve into the cylinder. There was also found to be a small leakage past the piston from the head to the crank end.

But the most unexpected result was the large amount of leakage past the valve from the steam-chest into the exhaust. This was determined by blocking up the ports with lead and running the valve in the normal manner by an electric motor. This leakage appeared to be proportional to the difference of pressure causing the leak, and to be independent of the number of reciprocations of the valve per minute. From the tests thus made on the leakage to the exhaust, the leakage correction in Table VII was estimated. Although the investigators concluded that their experimental rate of leakage was quite definite, it would appear that much of the discrepancy between the indicated and calculated condensation and vaporization can be attributed to this correction, which was two or three times as large as the



weight of steam passing through the cylinder. Under the most favorable condition (for the seventh test) the leakage was 0.0494 of a pound per stroke, and since there were 97 strokes per minute, it amounted to

$$0.0494 \times 97 \times 60 = 287.5$$

pounds per hour, or 32.6 pounds per horse-power per hour, so that the steam supplied per horse-power per hour amounted to 56.4 pounds. If it be assumed that the horse-power is proportional to the number of revolutions, then the engine running double-acting will develop about 44 horse-power, and the leakage then would be reduced to 6.5 pounds per horse-power per hour. Such a leakage would have the effect of increasing the steam-consumption from 23.5 to 30 pounds of steam per horse-power per hour.

To substantiate the conclusions just given concerning the leakage to the exhaust, the investigators made similar tests on the leakage of the valves of a quadruple-expansion engine, which had plain unbalanced slide-valves. The valves chosen were the largest and smallest; both were in good condition, the largest being absolutely tight when at rest. Allowing for the size and form of the valve and for the pressure, substantially identical results were obtained.

The following provisional equation is proposed for calculating the leakage to the exhaust for slide-valves:

leakage = 
$$\frac{kep}{l}$$
,

where l is the lap and e is the perimeter of the valve, both in inches, and p is the pressure in pounds in the steam-chest in excess of the exhaust-pressure. The value of the constant in the above equation is 0.021 for the high-speed engine used by Callendar and Nicolson, and is 0.019 for one test each of the valves for the quadruple engine, while another test on the large valve gave 0.021.

This matter of the leakage to the exhaust is worthy of further investigation. Should it be found to apply in general to slidevalve and piston-valve engines it would go far towards explaining the superior economy of engines with separate admission and exhaust-valves, and especially of engines with automatic dropcut off valves which are practically at rest when closed. It may be remarked that the excessive leakage for the engine tested appears to be due to the size and form of valves. The valve was large so as to give a good port-opening when the cut-off was shortened by the fly-wheel governor, and was faced off on both sides so that it could slide between the valve-seat and a The cover-plate was recessed opposite massive cover-plate. the steam-ports, and the valve was constructed so as to admit steam at both faces; from one the steam passed directly into the cylinder, and from the other it passed into the cover-plate and thence into the steam-port. This type of valve has long been used on the Porter-Allen and the Straight-line engines; the former, however, has separate steam- and exhaust-valves. Such a valve has a very long perimeter which accounts for the very large effect of the leakage. Callendar and Nicolson consider that the leakage is probably in the form of water which is formed by condensation of steam on the surface of the valve-sent uncovered by the valve, and say further, that it is modified by the condition of lubrication of the valve-seat, as oil hinders the leakage.

#### CHAPTER XII.

## ECONOMY OF STEAM-ENGINES.

In this chapter an attempt is made to give an idea of the economy to be expected from various types of steam-engines and the effects of the various means that are employed when the best performance is desired.

Table X gives the economy of various types of engines, and represents the present state of the art of steam-engine construction. It must be considered that in general the various engines for which results are given in the table were carefully worked up to their best performance when these tests were made. In ordinary service these engines under favorable conditions may consume five or ten per cent more steam or heat; under unfavorable conditions the consumption may be half again or twice as much.

All the examples in the table are taken from reliable tests; a few of these tests are stated at length in the chapter on the influence of the cylinder walls; others are taken from various series of tests which will be quoted in connection with the discussion of the effects of such conditions as steam-jacketing and compounding; the remaining tests will be given here, together with some description of the engines on which the tests were made. These tables of details are to be consulted in case fuller information concerning particular tests is desired.

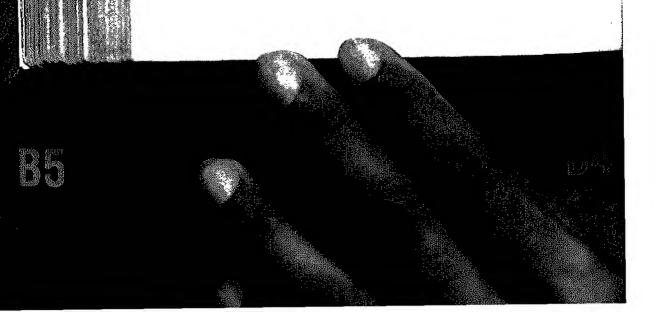
The first engine named in the table is at the Chestnut Hill pumping-station for the city of Boston. Its performance is the best known to the writer for engines using saturated steam. Some engines using superheated steam have a notably less steam-consumption; but the heat-consumption, which is a better criterion of engine performance for such tests, is little if any better. The first compound engine for which results are given, used 9.6

TABLE X, EXAMPLES OF STEAM-ENGINE ECONOMY.

Type of Magine.	Revolutions per minute.	Steam-pressure. Pounds per square inch.	Наж-рочет.	Steam per borse power per bour. Pounds.	B.T.U. per horse-power per min.	Coal per nonser power per hour. Pounds.
Triple-expansion engines: Leavitt pumping engine at Chestout Hill Sulzer mill-engine at Augsburg Experimental engine at the Massachusetts Institute of Yechnology Marine engine Iona	50 01	1.10 1.47 165	576 1823 125 615	11.3 13.7 13.4	231	1.15 1.19
Marine engine Meteor	74 01 128	1.15 15.1 135 135	1004 1136 135 137	9.6	100	2.01
Leavitt pumping engine at Louisville Marine engine Rush Marine engine Furi Vann Simple engines, condensing: Curies engine at Creusat	18,6 73 56 60	137 60 57 84	643 466 371 176	12.2 18.4 21.2	222	2.45 2.66
Corliss engine without Jacket	59 76 51 63 61 76	61 96 65 104 78	150 145 260 237 200 120	10.4 23 21.5 24.2		
Harris-Corliss engine at the Massachusetts Institute of Technology  Direct-acting steam-pumps: Fire-pump at the Massachusetts Institute of Technology	(12 *(10	77	10	33.5	548	<b>o</b>
at reduced power  Steam and feed pump on the Mhineapolis at reduced power		50	8,8	013		

pounds of steam and 199 n.T.U. per minute, the gain being hardly more than the variation that might be attributed to difference in apparatus, etc. The Chestnut Hill engine, which was de-

\* Strokes per minute.



signed by Mr. E. D. Leavitt, has three vertical cylinders with their pistons connected to cranks at 120°. Each cylinder has four gridiron valves, each valve being actuated by its own cam on a common cam-shaft; the cut-off for the high-pressure cylinder is controlled by a governor. Steam-jackets are applied to the heads and barrels of each cylinder, and tubular reheaters are placed between the cylinders. Steam at boiler-pressure is supplied to all the jackets and to the tubular reheaters.

#### TABLE XI.

TRIPLE-EXPANSION LEAVI'TT PUMPING-ENGINE AT THE CHESTNUT HILL STATION, BOSTON, MASSACHUSETTS.

CYLINDER DIAMETERS 13.7, 24.375, AND 39 INCRES; STROKE 6 FEET.

By Professor E. F. MILLER, Technology Quarterly, vol. ix, p. 72.

	•
Duration, hours	4
Total expansion	I
	0.6
	5 · 7
Barometer, pounds per square inch	4.9
Vacuum in condenser, inches of mercury	7.25
Pressure in high and intermediate jacket and reheaters, pounds per	
square inch	5 - 7
Pressure in low-pressure jacket, pounds per square inch	9.6
Horse-power	5 - 7
Steam per horse-power per hour, pounds	1.2
Thermal units per horse-power per minute	4.3
Thermal efficiency of engine, per cent	8.0
	8.0
	4
Coal per horse-power per hour, pounds	1.146
Duty per 1,000,000 B.T.U	55,000
	9 . 5

The Sulzer engine at Augsburg has four cylinders in all, a high-pressure, an intermediate, and two low-pressure cylinders. The high-pressure cylinder and one low-pressure cylinder are in line, with their pistons on one continuous rod, and the intermediate



cylinder is arranged in a similar way with the other low-pressure cylinder. The engine has two cranks at right angles, between which is the fly-wheel, grouved for rope-driving. Each cylinder has four double-acting poppet-valves, actuated by eccentrics, links, and levers from a valve-shaft. The admission-valves are controlled by the governors. Four tests were made on this engine, as recorded in Table XII.

## TABLE XII.

TRIPLE EXPANSION HORIZONTAL MILL-ENGINE.

CYLINDER DIAMETERS 20.0, 44-5, AND TWO OF \$1.6 INCHES; STROKE 78.7

Bulli by Sutzer of Winterthur, Zeitschrift des Vereins Deutscher Ingenieum, vol. 31, p. 534.

	· .		*******	
	1	П	111	īv
	}			4
Duration, industry	ვირ	311	272	327
Revolutions per minute	50.23	ኛስ. #ዘ	56.18	
Steam-pressure, pounds per square inch .	145.4	147.9	1,18.4	149.0
Vacuum, inches of mercury	37.34	27.20		27.10
Horse-power	1872	1835	1850	1823
Steam per horse-power per hour, pounds Mean for four tests	11-53	ii.40		11.33
Coal per horse-power per hour, pounds	1-37	1.36	1.20	1.19
Steam per pound of coal	ส. 78	8.40	8.07	9.61

The test on the experimental engine at the Massachusetts Institute of Technology is quoted here because its efficiency and economy are chosen for discussion in Chapter VIII. Taking its performance as a basis, it appears on page 148 that with 150 pounds boiler-pressure and 1.5 pounds absolute back-pressure such an engine may be expected to give a horse-power for 11.5 pounds of steam, from which it appears that under the same conditions its performance compares favorably with the Sulzer engine or even the Leavitt engine.



#### TABLE XIII.

#### MARINE-ENGINE TRIALS.

By Professor Alexander B. W. Kennedy, Proc. Inst. Mech. Engrs., 1889-1892; summary by Professor H. T. Beare, 1894, p. 33.

The engines of the S. S. Iona have an unusually large expansion and give a correspondingly good economy. The engines of the Meteor and of the Brookline give the usual economy to be expected from medium-sized marine engines. Table XIII gives details of tests on the engines of the first two ships mentioned, together with tests on compound marine engines. Table XIV gives tests on the engine of the Brookline. It appears probable that the relatively poor economy of marine engines compared with stationary engines is due to the smaller degree of expansion, which is accepted to avoid using large and heavy engines.

# TABL

#### TESTS ON THE ENGINE

CYLINDER DIAMETERS 23, 35, AN By F. T. MILLER and R. G. B.

Duration, hours										
Revolutions per	mir	ıuı	te							
Steam-pressure, mosphere										
Vacuum, inches	of 1	ne	rc	ur	y			٠		
Horse-power .										
Steam per horse	-pov	we	r	pe:	r	hot	ır,	ря	ou	nds

Coal per horse-power per hour, pounds B.T.U. per horse-power per minute

The horizontal mill-engine w engines in Table X, is a tand are given in Table XXVI on I superheated steam is the best

with saturated steam is a trifle

TABL

COMPOUND LEAVITT PUMP KENT

engine.

CYLINDER DIAMETERS 27.2 AND

By F. W. DEAN, Trans. Am. S

#### AUTOMATIC CUT-OFF ENGINES

TABLE XVII.
ENGINES OF THE U. S. REVENUE STEAMERS REGALLATIN.

													Rush.
The state of the s				11 1.19	67 C N	elabo "-"a	rwe zew	7 344. [1	en Sparrage	G-nan	5100573	REPORTED.	чин техносогия полите сто проведения
Diameters of cylinders	, i	ne	hes	ı,					,		,		24 and 38
Stroke, inches	, ,	, ,	,	3			,	,			,		27
Duration, hours		,			٠		,	٠		4			55
Revolutions per minute Steam-pressure by gau	0			:	b		,	ı		,		4	71
Steam-pressure by gau	ge	. [1	citif	14 14	,		*	à	•				Og. r
Vacuum, inches of mei	ret	184	,				4				,		26.5
Total expansions					,						٠		6.2
Horse-power			,	,	٠	1	٠.					,	266.5
Steam per horse-power	P	4°F	her	ur,	11	1.14	134	4	ı		,	,	18.4

The details of the tests on the U. S. Revenue Ste and Gallatin are given in Table XVII, as made ab a board of naval engineers to determine the advanta pounding and using steam-jackets. Three other e tested at the same time, but they were of older types interesting.

A remarkably complete and important series of test in 1884 by M. F. Delafond. These tests are recorde XXX and XXXI, from which there are quoted in T results with and without condensation and with a steam in the jackets.

The details of the tests on to cinnati, together with tests on to Table XVIII.

TABLE
DUPLEX DIRECT-ACTING FIRE
INSTITUTE OF

TWO STEAM-CYLINDERS 16 INCH Technology (Quart

Single strokes per minute.	Length of stroke. West.	Length of stroke. East.	Steam- pressure by gauge.	H or pow- Stea cylind
99	11.40	10,10	58.5	6.
114	11.70	11.07	55.6	12.
119	11.40	11.07	51.4	12.
135	11.60	11.10	53.8	18.
156	10.00	10.26	47.2	21.
193	10.00	10.31	45.6	32.
175	11.77	11.70	45.6	39.

TABL

TESTS OF AUXILIARY STEAM

MINNI
By P. A. Engineer W. W. WHITE

Engrs.,

Paulos or numer testad

# METHODS OF IMPROVING ECONOMY

The two tests on the direct-acting fire-pump Massachusetts Institute of Technology are taken fr XIX, and the tests on the feed- and fire-pump on the M are given in Table XX. Both sets of tests show the exconsumption of steam by such pumps when running a powers. The latter table is most interesting on accolight that it throws on the way that coal is consumed vessel when cruising at slow speeds or lying in harbor.

Methods of Improving Economy. — The least expe of engine to build is the simple non-condensing engine valve gear; this type is now used only where economy importance, or where simplicity is thought to be in Starting with this as the most wasteful type of engine ments in economy may be sought by one or more of the devices:

- 1. Increasing steam-pressure.
- 2. Condensing.
- 3. Increasing size.
- 4. Expansion.
- 5. Compounding.
- 6. Steam-jackets.

7. Superheating.

by the ideas that have be of thermodynamics, and it the steam-engine; the four in this category as a means range effective. It has be the cylinder of metal whe energetic action on the steattempts to approach the non-condensing engines, at to be gained by increasing devices enumerated (increasing jackets, and superheating

been applied to diminish and allow us to take advan

appears at first sight that the first category, as it or range between the steam-put the steam in the cylinand it is better to considerly cylinder condensation.

It is interesting to cons steam-jackets were used by he was limited in pressure

# EFFECT OF RAISING STEAM-PRESSURE

that the theory has sometimes been misapplied, has erroneous opinion that the steam-engine has been d without or in spite of thermodynamics. And further, hall the advantages then available has had a tendency to their importance, and makes it the more desirable to several methods categorically as given above.

It is now commonly considered that the steam-en

been brought to full development, and that there is litt substantial improvement to be expected; in fact, this was reached a decade or two ago, when the triple engisteam at 150 to 175 pounds by the gauge, was perfect most recent change is the use of superheated steam pressures, now that effective and durable superheat been devised. Experiment and experience have settl well the limitations for the various methods of improving and allow of a fair and conservative presentation to whe will probably be few exceptions. We will, therefore, general conclusions as briefly as may be, and give the

In order to bring out the advantage to be obtained by device, such as compounding, we will compare only performance of the simple engine with the best perfort the compound engine, each being given all the advant

which they may be based.

If t' is taken to be 100° F

300°, and 400°, the values of t But the influence of the cy improvement unless we resort studying Delafond's tests Figs. 57 and 58 on pages 25 sumption is plotted as ordina cut-off, each curve being lett was maintained while a serie resents tests without steam is steam in the jackets. Thos with condensation, and those condensing. Inspection of tion in steam-consumption, 35 pounds by the gauge to 6 without a steam-jacket, but to 80 and 100 pounds gives sumption. The same figure the limit for non-condensing on Fig. 58 are not quite so figures give the following as

simple engines of good desig

#### DELAFOND'S TESTS

used in the jacket could be determined. The engine with and without steam in the jacket, both condensing condensing, and at various pressures from 35 to 16 above the pressure of the atmosphere. The effect and the friction of the engine were also obtained by friction-brake on the engine-shaft.

The piping for the engine was so arranged that steam drawn either from a general main steam-pipe or fron boiler used only during the test. Before making engine, which had been running for a sufficient tim to a condition of thermal equilibrium, was supplied from the general supply. At the instant for beginning the general supply was shut off and steam was taken special boiler during and until the end of the test, an pipe from that boiler was closed. The advantage of t was that at the beginning and end of the test the w boiler was quiescent and its level could be accurately d At the end of a test the water-level was brought to noted at the beginning. The water required for f special boiler during the test and for adjusting the at the end was measured in a calibrated tank. As pressure in the general-supply main and in the spe was the same, there was little danger of leakage th

58 represents tests with ste densation, at 50 pounds be curves are the per cents of steam-consumptions in pour

TA

HORIZONTAL COR

CYLINDER DIAMETER 21.65 INC BARREL (

BARREL ( By F. Delafon

		DI I. L	/ ELAFON
Number of test.	Duration, minutes.	Revolu- tions per minute.	Cut-off in per cent o stroke.
1 2 3 4 5 6 7 8	60 105 75 36 73 55 80 39	60.0 58.6 59.4 57.7 58.8 61.5 59.9 58.1	4 6 9 12.5 5.5 6.7 6.7
9 10 11 12 13 14 15 16	120 100 90 55-5 50 94 102 40	59.8 59.3 59.8 58.0 59.1 59.6 59.6 59.4	7.5 8.3 10.5 14 18 5 5.5 11.5

18

19

91 90 75 58.3 59.5 59.0

5.9 9 15.5

# DELAFOND'S TESTS

results for individual tests are represented by dots which or near which the curves are drawn. As there a few tests in any series, a fair curve representing the be drawn through all the points in most cases. The

TABLE XXII.

HORIZONTAL CORLISS ENGINE AT CREUSOT CYLINDER DIAMETER 21.65 INCHES; STROKE 43.31 INCHES; JACKET ONLY; NON-CONDENSING.

By F. DELAFOND, Annales des Mines, 1884.

Number of test.	Duration, minutes.	Revolu- tions per minute.	Cut-off in per cent of stroke.	Steam- pressure, pounds per square inch.	Steam used in jacket, per cent.	Indicate horse- power.
r	78	61.7	1.3	96.3	The had been a second and a second a second and a second and a second and a second and a second	147.5
2	55	61.4	17	100.2		181.5
3	25 80	63.6	20	102.0		217
4		60.8	111	98.1	2.5	143
5	60	62.0	13	103.8	3.4	177.5
6	36	63.0	16	103.0	3.1	194
7	30 66	62.7	20	103.5	2.0	237
8		62.0	15.5	73.7		131
9	60	60.9	18	77.0		236
10	60	60.0	24.5	76.7		178
II	30	60.6	32	77.5		300
12	70	61.1	16.5	77.0	1.7	
13	50	61.6	23.5	75.8	1.2	137
14	30	60.5	30	78.0	1.3	204
15	71	61.4	24.5	50.8		Rot
× 45		ALK D	1			

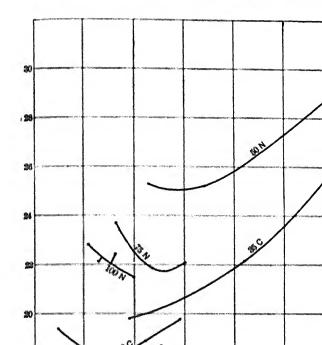
radically from the curve at so early a cut-off is a probable error of determ



# CONDENSATION

on Fig. 58. It does not appear worth while to try to curve to represent these tests.

Condensation. — The complement of raising the steam



of either pair of results v 25 per cent, which would of brake tests for this engical efficiency when runn it was only 0.82 when the brake horse-power per hadicated steam by the mairs of results became for

non-condensing 26.9, and with steam in the jacket from condensation was

$$\frac{26.9 - 22.1}{26.9} = 0$$

The gain from condens and the conditions of ser to twenty per cent. Cle vacuum than with a poor feature which should be of pressure; when the condit effective pressure is large advantage of maintaining

when the mean effective be best illustrated with

#### INCREASE OF SIZE

pressure for a pumping-engine or mill-engine may be 18 pounds per square inch, and a difference of o vacuum (or half a pound of back-pressure) will be to nearly three per cent in the power; on the other has engine is likely to have a reduced mean effective forty pounds per square inch, and compared with it a of one inch of vacuum is equivalent to a little more the cent. In any case the gain in economy due to a sma ment in vacuum is approximately equal to the reducabsolute pressure in the condenser, divided by the mean effective pressure.

A very important matter is brought out in this di the gain from condensation, namely, that the real ga mined by comparing the engine consumption for brake horse-powers. The only reason for using th power (as is most commonly done) is that the bral often difficult to determine and sometimes impowas pointed out on page 144, a true basis of compaheat-consumption of the engines compared in B.T.U. power per hour. But that quantity was not determitests by Delafond, and since the comparisons are for of tests, one pair with and the other without jackets objection to it in the cases discussed.

In this case the larger engine capacity of the smaller one, the absolute size of the engine is little if any advantage in

limits of practice.

But the advantage from as will be apparent from t in Table X are for engines of standards. These engines and of the use of steam-jack tages from jacketing or s

and such devices are pos

engines.

Expansion. — There are that can be advantageouslis imposed by the action of imposed by the friction of most advantageous point owhich can be clearly determents; compound and tri

the temperature-range th

employed. The terminal a stationary, triple, or com

#### COMPOUNDING

The total expansion for a compound or triple engiobtained in two ways: we may use a large ratio of

cylinder to the small cylinder, or we may use a short the high-pressure cylinder. The two methods may be by the two Leavitt engines mentioned in Table X; the large to the small cylinder of the compound Louisville, is a trifle less than four, and the cut-off for pressure cylinder is a little less than one-fifth strok other hand, the triple engine at Chestnut Hill has a than eight for the extreme ratio of the cylinders, an cut-off for the high-pressure cylinder at a little more fifths. So large an extreme ratio as eight would not venient for a compound engine, but ratios of five or been used, though not with the best results.

Marine engines usually have comparatively little to sion both for compound and for triple engines, and con are unable to work with an economy equal to that for engines; the type of valve-gear which the designers feel c to use is also little adapted to give the best results. some question whether there is not room for improboth these directions.

Compounding. — The most efficacious method v

and two low-pressure cylinders was a ships. Many triple engines have to which with the high-pressure and make four in all. Again, some trip pressure cylinders and two low-pressure

Two questions arise: (1) Under viseveral types of engines be used? an pected by using compound or triple e Neither question can be answered

intermediate cylinder, making five ir

From tests already discussed and are given in Table X, it appears that best results were attained with the fol engines about 175 pounds by the ga 145 pounds, and for simple engines for engines with condensation. Ne obtained for a compound engine vand on the other hand the simple en with equal advantage. The informa

engine is sufficient to serve as a reli least room for discretion concerning pound and triple engines. There wi of serious disappointment if the follow

### COMPOUNDING

pounds with a steam-jacket; with an allowable variation pounds. For a non-condensing compound engine we as the preferred pressure about 175 pounds, but our ter include this case, and the figure is open to question. little, if any, occasion for using triple-expansion non-c engines.

About ten years ago an attempt was made to introd ruple-expansion engines, using steam at about 250 p marine purposes in conjunction with water-tube boile can readily be built for high-pressures; but more recen has been to adhere to triple engines even where the has chosen a high-pressure for sake of developing a la per ton of machinery, or for any other purpose.

For convenience in trying to determine the gain f pounding, the following supplementary table has been of

Data and Results.	Simple Corliss at Creusot.	Compound Mill-Engine
Regional property of the state	Choracter and an annual section of the section of t	Secretal and American Secretary and American
Revolutions per minute	60	127

Steam-pressure above atmosphere, pounds . .

Steam per horse-power per hour, pounds . . .

BTII ner hame namer ner mir

Total expansion

Compound and triple engines have be to marine work, where for various reason well be used. Taking the engines of the in the following supplementary table to r

we can determine the gain from compou

Data and Results.							
Revolutions per minute Steam pressure by gauge Total expansion		5					
Steam per horse-power per hour, pounds.		2					

Gain from compounding,

$$\frac{22 - 18.4}{22} = 0.16.$$

Gain from using triple engine instead o

$$\frac{22-15}{22}=0.32.$$

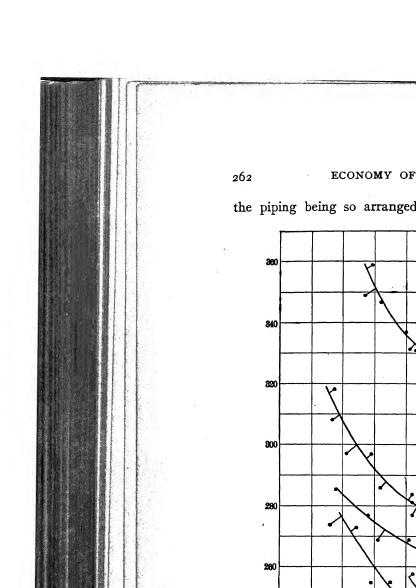
Cain from using triple engine instead

#### EXPERIMENTAL ENGINE

Properly the comparison for finding the gain from coing should be based on thermal units per horse-power per but the data for such a comparison are not given for engines, and as all the engines have steam-jackets, the coof steam-consumptions is not much in error.

Steam-Jackets. — As has already been pointed ou

discussion of the influence of the cylinder walls, the action of a steam-jacket is to dry out the cylinder during without unduly reducing the temperature of the cylind and thus check the condensation during admission. T iacket does indeed supply some heat during expan that effect is of secondary importance, and the heat with a thermodynamic disadvantage. The principal thus to supply heat which is thrown out in the exhaust all lost in case of a simple engine; in case of a compou the heat supplied by a jacket during exhaust from pressure cylinder is intercepted by the low-pressure and is not entirely lost. It would clearly be much mo tageous to make the cylinders of non-conducting m that were possible. A clear grasp of the true actisteam-jacket has a natural tendency to prejudice against that device, and this prejudice has in many of strengthened by the confusion that has come from indi-



#### EXPERIMENTAL ENGINE

steam-jackets on the barrel and the heads, and supplied to any or all of these jackets at will. To densed in the jackets of any one of the cylinders is of pressure in a closed receptacle and measured. receivers were also provided with steam-jackets; provided with tubular reheaters so divided that of thirds, or all the surface of the reheaters can be steam condensed in the reheaters is also collected in a closed receptacle.

The valve-gear is of the Corliss type with vacu which give a very sharp cut-off. The high-press mediate cylinders have only one eccentric and w consequently cannot have a longer cut-off than hal the control of the drop cut-off mechanism. The cylinder has two eccentrics and two wrist-plates, and valves can be set to give a cut-off beyond half governor is arranged to control the valves for an Each cylinder has also a hand-gear cylinders. its valves. For experimental purposes the gove control only the high-pressure valve-gear, when running compound or triple-expansion. The used for adjusting the cut-off for the other cylinder usually the cut-off for such cylinder or cylinders is

Clearance in per cent

High-pressure cylinder Intermediate '' Low-pressure ''

Results of tests on the order to form a triple XXIII, and are represedut-off of the high-preseconsumptions of thermal

ordinates.

The most important this engine is of the advisteam in the jackets. I purpose: (1) with steam receivers, (2) with steam

the cylinders only, and (.

The most economical steam in all the jackets the receiver-jackets, as

heads and barrels, (3) w

There is a small but dis the receiver-jackets also

## EXPERIMENTAL ENGINE

TABLE XXIII.

# TRIPLE-EXPANSION EXPERIMENTAL ENGINE AT CHUSETTS INSTITUTE OF TECHNOLOGY

Trans. Am. Soc. Mech. Engs., 1861 (1864) Technology Que

	نه	ė	i	The state of the s		Site	ram t	isrel in jack or cout.	ets.
Condition.	Revolutions per minute.	Per cents of cut-off, high pressure cylinder	Builti-present by gauge.	Vaccourth of confidencer, styches of mercury.	Patrician Company	High greater		Intermediate pre- nere cylinder. Second receiver.	Low-pressur crists- der.
o see our true is it	80 03 90 00 91 93 91 55 93 37 84 87 91 15 80 70 87 55	30 1 45 0 27 1 27 8 24 0 21 0 17 4 12 0 8 3	146 9 147 0 146 9 146 7 146 8 147 8 147 8 147 8	## # # # # # # # # # # # # # # # # # #	414 H 103 A 414 U 303 B 103 P 103 P 103 B	1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1	- 1 - 1 - 1 - 1 - 1 - 1	H 6 H H H H H H H H H H H H H H H H H H	6, 1 2 5 4 5 7 4 5 8 8 8 8 8 8 8 8 8 8 8 8 8 8 8 8 8 8
to 11 Dittes.	H4 23 H2 50 A2 13	# # # # # # # # # # # # # # # # # # #	145 4 144 5 145 1	30 4 30 4	10 0 14 9 10 1	4 4		u e	0 0 1
Markets on Cold day and Cold day and Cold days and Cold da	01 30 01 49 01 83 01 81 02 17 02 57	16 1 14 H 40 3 27 5 25 0 21 0	141 7 141 0 141 4 147 1 141 7	## 7 ## # ## # ## 5	\$10 a \$10 a \$10 a \$10 a \$10 a \$10 a	2 50 2 50 2 50 2 5 3 5 4	****	0 4 4 4 7 7 6 4 U 4 4 7 7 6 4 U 4 7 7 7 4 4 9	4 0 1 6 4 1 7 1 1 7 7 1
10 20 21 22 23 24 24 25 26 27 28 29 29 29 29 29 29 29 29 29 29 29 29 29	84 05 84 03 83 45 82 40 81 40 81 05 80 28 80 32	0 1 13 0 13 6 20 7 27 4 20 7 14 0 33 6	# # # # # # # # # # # # # # # # # # #	46 46 77 44 5 45 45 45 45 45 45 45 45 45 45 45 4	\$0 0 0 40 M	****	Section of the state of the section	7 7 4 6 6 7 7 1 6 6 6 7 7 1 6 6 6 6 6 6 6 6 6	8 7 8 6 8 6 8 6 8 6 8 6 8 6 8 6 8 6 8 6
37 38 29	85 60 85 62 85 60	H 4 H 5	1 4 9 16 1 4 9 1 1 4 9 1	25; 2 25; 2 25; 1	30 7 30 9	The state of the s	Share and the same of the same		

Table XXIV gives tests in the jackets and with stea the results of these tests wil

TRIPLE-EXPANSION EXPER CHUSETTS INSTITUTE REHEATERS.

	Condition.	Revolutions per minute.	Percent of Cal-of-	Boier-present	A ACTUALTY OF COME.
3 4	Without steam in reheaters.	H: H H: H H: G H: J	27 27 20 10	146 7 147 5 147 0 148 3	31 81 8
5 6 7	Steam in first reheater.	Ng q Ng q Nz 4	10 10	140 ±	3 4
8 10 11 12	Steam in both reheaters.	Hq 61 H4 5 H4 4 H1 9 H2 10	# 1 1 2 2 2 3 3 M	147 1 140 9 147 1 147 7 140 6	41

the most favorable conditions should be chosen when has steam in the jackets, and in like manner the without steam in the jackets should be selected; a of two such selected tests has more weight than a comparison of individual tests, however great the such tests may be. An investigation of Delafond Tables XXI and XXII and represented by Figs. gives such a comparison. The tests selected are the Table X and give two pairs, with condensation a Thus the best result with steam in the jacket and we sation is 16.9 pounds, and without steam in the jacket the gain is

Without condensation the best results are 21.5 withe jackets and 24.2 without steam in the jackets; the

These results are probably too small, as the steam jackets should be collected and returned to the boil a moderate reduction of temperature below the ten the steam in the boiler. The drip from the jackets through a trap, and as reported is probably too small the most questionable result from the tests.

Data for a similar comparison for compound eng at hand, but the tests described on page 265 seem to b for the triple engine.

From the diagram Fig. on the best would with

These heat-consumptions of steam per horse-power per consumption the gain from appear to be only 9 per centent. This large difference steam used in the jackets, of the total steam-consumvidual jacket is, however, n

The effect of jacketing surprisingly small, as fron B.T.U. per horse-power pe best result without steam only

in the jackets of the high-pu the jackets of each of the o

$$\frac{274 - 262}{274}$$

The correspondence betwee Callendar and Nicolson of has already been pointed

From the tests just disc servative to say that about

#### INTERMEDIATE REHEATERS

are the Leavitt pumping-engines, for which results are Table X. The fact that these engines give the best recorded for engines using saturated steam lead to the that such reheaters may be used to advantage. The evidence, however, is not so favorable, for, as has been out on page 264, there was found a small but distinct disfrom using steam in double walls or jackets on the in receivers of the experimental engine at the Massachusett of Technology. It appears that this engine gives economy when steam is supplied to the jackets on the and not to the jackets on the reheaters, and, further, steam is used in the receiver-jackets the steam in pressure cylinder shows signs of superheating, which considered to indicate that the use of the steam-jacket too far.

After the tests referred to were finished the enginnished with reheaters made of corrugated-copper arranged that one-third, two-thirds, or all of the reheat can be used, when desired. Table XXIV, page 266 results of tests made on the engine with and without the reheaters; in these tests the entire reheating-surface when steam was supplied to a reheater.

For some reason the heat-consumption when no used in the reheaters is somewhat greater than that Table XXIV for the engine without steam in a jackets; the difference, however, is not more than that and a half per cent and cannot be considered of much in It is clear from the table that there is advantage from reheater, and still more from using two. If the heat-conforthe engine without steam in the jackets and with in the reheaters (taken from Table XXIV) is assu

which is scarcely more the jackets. These tests they are too few and refer Superheating. — The m

the interference of the congine economy is by to 1863-64 a number of natheaters by Chief Engineers showed a marked advantable heated steam for stational and in Europe. But the dry steam on one side and

deteriorated, and after and the use of superheated si pound and triple engines.

More recently improvint oduced in Great Briendurance, and superheated in the superhe

the application of super. Two series of tests will long a simple engine, and so There appears to be no

successfully for sufficient

TABLE XXV.

# DIXWELL'S TESTS ON SUPERHEATED STE

CYLINDER DIAMETER 8 INCHES; STROKE 2 FEET.

Proceedings of the Society of Arts, Mass. Inst. Tech., 188

	Sati	Saturated Steam.			
	I	II	III	IV	
Duration, minutes Cut-off Revolutions per minute Boiler-pressure above atmosphere, pounds per square inch Back-pressure, absolute, pounds per sq. in Temperatures Fahrenheit: Near engine In cylinder by pyrometer Per cent of water in cylinder: At cut-off At cut-off At cut-off Steam per horse-power per hour, pounds, B.T.U. per horse-power per minute.	50.4 15.4 302 278-297 52.2 32.4 7.65	83 0.443 60.4 50.2 15.7 303 279-296 35.9 29.3 12.7 42.2 696	63 0.689 58.0 50.3 15.8 303 282-300 27.9 23.9 23.9 45.3 747	180 0.218 61.0 50.4 15.2 478 313 27.4 18.3 6.83 35.2 631	
B.I.O. per norse-power per minute	/90	090	/4/	031	

A metallic thermometer or pyrometer was place in the head of the cylinder. When saturated steathis pyrometer showed a large fluctuation, but when steam was used its needle or indicator was at rest part of the apparent change of temperature with satis attributed to the vibration of the needle and the mechanism, it is very clear that the use of super reduces the change of temperature of the cylinder emarkable manner. The effect of superheating of the cylinder walls is also indicated by the per in the cylinder at cut-off and release.

The apparent gain by comparing the amounts of per horse-power per hour in favor of superheated

we must compare instead the giving a real gain of

<u>696 – 546</u> 696

This same Harris-Corlis consumption of 548 B.T.U supplied with saturated stea why the earlier attempts a so easily set aside when it w pressure.

Though we have no test condensation on engines of it is probable that a very ruse of superheated steam we heat were as much as fiftee consumption to a larger

The best results obtained steam in compound engined in Table XXVI, for a

huilt in Chant Fire tosts

and would be likely to give steam per horse-power per

#### SCHRÖTER TESTS

which places it a little beyond the performance of engine mentioned. But since the uncertainty of the tion of power by the indicator is probably two per coreasonably conclude that the effect of using superh in a compound engine is to place it on a level wengine, and the question is to be decided in pracrelative expense and trouble of supplying and using a instead of a third cylinder and higher steam-pressur

It is somewhat remarkable that steam was sup jackets during the superheating tests, but not at ing that for those tests the jackets had a small made evident by noting the percentages of steam of them.

# TABLE XXVI.

# COMPOUND HORIZONTAL MILL-ENGINE CYLINDER DIAMETERS 12.8 AND 22 INCHES; STROKE 33.5 By Professor M. Schröter, Milleilungen über Forschun Heft 19, 1004.

	Saturated					Suj	
		11	111	iv	v		
	•	8.4	111	14		VI	VII
Mathematical processors in the construction of the constructio	WARRANG CATA		One Particular		NA.	STORY TO 1	
Horse-power	200	403	211	100	***	39.1	agi
Duration, minutes	Go	f) i	87 6	55	60	48	(no
Revolutions per minute	146	1 26	1 20 8	127	r all	136	136
Cut-off, high pressure cylinder	19 aN	0.11	19.34	0.16	9.10	0.41	9.11
Total expansions	7.0	9.7	13.8	20	39	7 1	0 1
Initial pressure, absolute pounds per	1	40.4	4.4.3		'And		9.
sq.in.	144	140	147	141	143	144	140
Back pressure, absolute pounds per	2 441	4 4840	4 444		.44		* 10.00
sq. in.	8 . 3	2 2	1 1.1	1.1			
Superheating, degrees F.						1 1	1,0
	1 1 1		100	2 4 4	1 1 4	246	857
Steam per horse-power per hour, pounds	1 . 3					4	
	13.0	13.8	10.3	11.4	1.3	19.0	10.4
Per cent condensed in jackets	10.6	集装 . 跨	17 0	11.7	14 4	3. 1	3. 5

one-third stroke when the about one-sixth stroke whatests on simple engines such the small Corliss engine

Technology, confirm these

The term total expansion can properly have only a contaken to be the product of cylinder by the reciprocal of for the high-pressure cylinds sion is about 20 for all the tax, except those on marin poor economy. It may the advisable to use much me and that less expansion shallows of service (for example expansion.

The stationary compour have about 20 expansions, that for highest economy quired. In practice some advisable,

Variation of Load. -- I

#### VARIATION OF LOAD

in the next chapter; and the second is evident from of curves of steam-consumption as given by Fig. 5 and Figs. 57 and 58, pages 252-253.

The allowable range of power for a simple engi than for a compound or a triple engine. Compa simple and a triple engine may be made by aid of 50. The Corliss engine at Creusot when supplied at 60 pounds pressure, with condensation and w the jacket, developed 150 horse-power and used of steam per horse-power per hour. If the increa to 10 per cent of the best economy, that is, to 10 horse-power per hour, the horse-power may be redu 02, giving a reduction of nearly 40 per cent from power. The triple engine at the Massachusetts Technology with steam at 150 pounds pressure and in all the cylinder-jackets developed 140 horse-pov 233 B.T.U. per horse-power per minute. Again, increased consumption to 10 per cent or to 254 B.T. may be reduced to about 104 horse-power, giving a 26 per cent from the normal power. The effect power for these engines cannot be well shown fr made on them, but there is reason to believe the engine would preserve its advantage if a compari made. Though the tests which we have on comp do not allow us to make a similar investigation of changing load, there is no doubt that it is intermed respect between the simple and the triple engine.

When the power developed by a compound engi by shortening the cut-off of the high-pressure cylind of the low-pressure cylinder must be shortened at t indicator-diagram due to expansion of the power is reduced by shortening the cylinder. Such a loop is always accome conomy; if the loop is large the enging than a simple engine, for the highnearly all the power and may have

piston, which is then worse than usele

cylinder is fixed, is likely to have a

There is seldom much difficulty in rany desired reduced power by shortenithe steam-pressure, or by a combinate But a compound engine sometimes govery low power (even when attention the low-pressure cylinder), which used discussed; i.e., the power is developed a cylinder. Triple engines are even a way. A compound or triple engine

liable to be cut or abraded.

Automatic and Throttle Engines. —
may be regulated by (1) controlling t

power is subject not only to loss of action, but the inside surface of the

may be regulated by (1) controlling the by adjusting the cut-off. Usually the

speed the forces acting on the governor are in equithe balls revolve in a certain horizontal plane. If the engine is reduced the engine speeds up and the outward and upward until a new position of eqfound with the balls revolving in a higher horizon. Through a proper system of links and levers the upward of the balls is made to partially close a throttle valve which supplies steam to the engine and thus adjusts the engine to the load.

by gravity. When the engine is running steadily

Shaft governors have large revolving weights whose forces are balanced by strong springs. They a enough to control the distribution or the cut off vengine, which, however, must be balanced so that i easily.

Automatic engines, like the Corliss engines, have

two for admission and two for exhaust of steam. The release, and compression are fixed, but the cut off by the governor. Usually an admission valve is attactuating mechanism by a latch or similar device, we opened by the governor, and then the valve is close by a spring, or by some other independent device, of the governor is to control the position of a swhich the latch strikes and by which it is opened to

valve.

Corliss and other automatic engines have long had reputation for economy, which is commonly attributed method of regulation. It is true that the valve goingines are adapted to give an early cut off, which is

elements of the design of an economical simple engi-

off is

from the steam to the exhaust side of similar construction.

Every steam-engine should have

of its normal power; and again it that a single-cylinder engine sho through the greater part of its stro tions, together with the fact that it a plain slide-valve engine to give an use of a long cut-off for engines con The tests on the Corliss engine a XXII, pp. 250 and 251) show clea a long cut-off for simple engines. out that a non-condensing engine about one-third stroke. With cutpounds steam-pressure the engine

and used 24.2 pounds of steam pe running without steam in the jack If the steam-pressure is reduced to lengthened to 58 per cent of the s is increased to 30.2 pounds per hor

power being then 173. The gain

Considering also that automatic engine built and carefully attended to, while often cheaply built and neglected, the one and the bad reputation of the counted for.

It is, however, far from certain that an have a decided advantage over a thrott latter is skilfully designed, well built and to run at the proper cut-off. Considerin steam-consumption per horse-power per is unduly shortened, it is not unreasonal not better results from a simple throttlir automatic engine when both are run for at reduced power.

The disadvantage of running a compo

with too little expansion can be seen by consumptions of marine and stationary hand, the great disadvantage of too mule evident from the tests on the engine in Massachusetts Institute of Technology 265). Considering that the allowable veconomical cut-off is more limited for a engine, it appears that there is less reason governor instead of a throttling governor triple engines than there is with simple the most economical engines (simple, co

Effect of Speed of Revolution. — Thou steam on the walls of the cylinder of a rapid, it is not instantaneous. It would an improvement in economy might be att

automatic engines.

surfaces exposed to steam in fact, all engines which for to run at very high rotative economy, in part from the refact that piston-valves are contour to the kind of leakage descripage 234, even when they amonly the engine has a flyvalve to be very free with the Willans invented a single-act at high rotative speed, and suppassages without excessive of

rod to carry the steam from tandem. Tests on this engin in this book) showed that a 200 revolutions per minute from 24.7 to 23.1 pounds further increase of speed to 21.4 pounds; the engine condensing. This engine use power per hour, when development of the condensity of the condens

lottenburg give some insight into the possibilities of The engine is of moderate size, developing about 15 as a steam-engine, and about 200 horse-power as a lusing steam at about 100 pounds by the gauge superheating. The engine is a three-cylinder triengine, but can be run also as a compound engiprobably is not proportioned to give the best econo latter condition.

The general arrangement of the engine is as follosteam cylinders are arranged horizontally side by additional cylinder using the volatile fluid (sulphus on the opposite side of the crank shaft, to which it is

its own crank and connecting rod. Steam is suppleabler and superheater to the steam engine, and into a tubular condenser which acts as the sulvaporizes; the condensed steam is pumped back in and the vacuum is maintained by an air pump as us of 20 to 25 inches of mercury was maintained in the The vaporous sulphur dioxide at a pressure of 120 to by the gauge was led to the proper cylinder, from exhausted at about 35 pounds by the gauge; this condensed in a tubular condenser by circulating temperature of about 50° F, at the inlet and aboth exit.

The drips from the steam jackets of the steam copied to the steam condenser instead of being reboiler, but that cannot be of much importance condensation in the jackets was probably less than of the total steam supplied to the engine. The pe

the engine is given in Table XXVIII in terms

TAI

## BINARY ENGINE, ST

By Professor E. Josse, Royal

	1
Revolutions per minute	139.6
Steam-Engine:	
Pressure at inlet, h.p. cylinder	
by gauge pounds	136.5
Vacuum, inches of mercury	23.0
Superheating, degrees Fahrenheit	175
Horse-power, indicated	132.1
Steam per h.p. per hour, pounds .	12.5
Thermal units per h.p. per minute	244
Sulphur-Dioxide Engine:	
Pressure by gauge pounds:	
In vaporizer	132
In condenser	31
Temperature Fahr. at inlet to cyl-	
inder	132.0
Temperature Fahr. at outlet from	
condenser	66.2
of circulating water inlet	49.6
outlet	59.9
Horse-power, indicated	45.3
per cent of steam-engine power	34.4
Combined Engine:	34.4
Horse-power, indicated	177.4
Steam per h.p. per hour, pounds .	9.7
Thermal units per h.p. per minute	183
Mechanical efficiency	85.5
mechanical enciency	23.3

## BINARY ENGINE

about 35 pounds in the sulphur-dioxide cylinder a ture of about 65° F., the efficiency would be

$$\frac{T - T''}{T} = \frac{575 - 65}{575 + 460} = 0.55:$$

$$\frac{0.55 - 0.50}{0.55} = 0.09.$$

and

The results of the tests given in Table XXVIII difficult to use as a basis for the discussion of the the binary system on account of certain discrepancie tests No. 3 and No. 7 have substantially the sams team-pressure, superheating and vacuum, and no vapor-pressures in the sulphur-dioxide cylinder advantage appears to lie slightly in favor of No. 7 the latter test is charged with 189 thermal units p

per minute, and the former with 176, giving to is advantage of about 7 per cent. A comparison horse-power per hour gives nearly the same reparison of tests No. 2 and No. 4 gives even a discrepancy, though the conditions vary more,

the total power of the latter is much greater.

If we take 200 thermal units per horse-power p

Finally it appears probable binary engine could be obtated compound engine, using surgood results might be expect 175 pounds gauge pressure valready been called to the fibut little with highly superfunnecessary and illogical.

## CHAPTER XIII.

#### FRICTION OF ENGINES.

ed on the indicated horse-power, because that nite quantity that may be readily determined hand, it is usually difficult and sometimes ke a satisfactory determination of the power activate the engine. A common way of determining the need by friction in the engine itself is to disconnect, or other gear for transmitting power from the place a friction-brake on the main shaft; the power hand determined by aid of indicators, and the power activated by the brake, the difference being the need by friction. Such a determination for a olves much trouble and expense, and may be used the engine-friction may depend largely on assmitting power from the engine, especially were are used for that purpose.

HE efficiency and economy of steam-engines

cent of the indicated horse-power condition of the engine. The pump (when connected to the the friction of the engine. It is cent of the indicated power of air-pump. Independent air-pumbest speed consume much less States naval vessels used only of the main engines. But as inconditional conditions are conditionally as a single condition.

direct-acting steam-pumps, muci-

tion of such pumps.

Mechanical Efficiency. — The an engine to the power generated efficiency; or it may be taken a indicated power. The mechan from 0.85 to 0.95, corresponding above.

The following table gives the number of engines, determined

TABLE

## INITIAL FRICTION AND LOAD FRICTION

pumping-engines, by measuring the work done is water.

Initial Friction and Load Friction. — A part of the an engine, such as the friction of the piston-rings stuffing-boxes of piston-rods and valve-rods, may to remain constant for all powers. The friction a head guides and crank-pins is due mainly to the thof the steam-pressure, and will be nearly proportional effective pressure. Friction at other places, such a bearings, will be due in part to weight and in part pressure. On the whole, it appears probable that may be divided into two parts, of which one is indithe load on the engine, and the other is proportional

load friction. Progressive brake-tests at increasing firm this conclusion.

Table XXX gives the results of tests made by Waier and Ludwig \* to determine the friction of a horizon.

The first may be called the initial friction, and the

compound engine, with cranks at right angles and wheel, grooved for rope-driving, between the conjuston-rod of each piston extended through the conjuston was carried by a cross-head on guides, and the aworked from the high-pressure piston-rod. The conjustion plain slide-valves, two for admission and two the exhaust-valves had a fixed motion, but the admission were moved by a cam so that the cut-off was determined.

The main dimensions of the engine were:

governor.

Stroke .							
Diameter:	small	piston					
	large	piston		_	_		

10 11

12 13 14

15 16

17

10

Таі

# FRICTION OF C

WALTHER-MEUNIER and LUDWIG, vol.

· · · · · · · · · · · · · · · · · · ·	1
	Horac-Powers
Condition.	
	Indicated.
A CARRON CONTRA	1
	288. ς
	276.0
Compound	209.0
condensing	343.7
with	7.686
air pump.	211.5
	180.4
	148 1
	130.1
	Compound condensing with

High pressure cylinder

only. Condensing with

air pump.

80.3

68.8

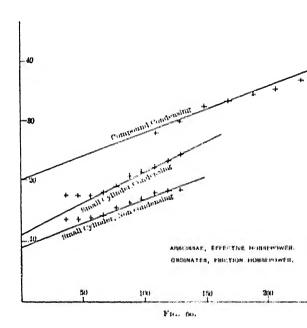
55. 3

### INITIAL FRICTION AND LOAD FRICTION

brake (numbers 9, 18, 19, 28, and 29) were irregular tain.

The first nine tests were made with the engine wo pound. Tests 10 to 10 were made with the high-preder only in action and with condensation, the low practing-rod being disconnected. Tests 20 to 20 were the high-pressure cylinder in action, without condensa

The results of these tests are plotted on Fig. 60



effective horse powers for abcisse and the friction he for ordinates. Omitting tests with small powers (for brake ran unsteadily), it appears that each series of t

normal net or brake horse to deliver, and may be rep

where a is a constant to be 60. If P is the net horse time, then the load friction

where b is a second consta The total friction of the er

so that the indicated powe

I.H.P. 
$$P + aP$$

The mechanical efficiency

The compound condensented by Fig. 60 develops power to the brake, so the friction. The diagram shape horse-power and contact the condense power and condense power and condense power and condense power and condense power and condense power and condense power and condense power and condense power and condense power and condense power and condense power power and condense power p

## INITIAL FRICTION AND LOAD FRICTION

but at half load (125 horse-power) the indicated hors

I.H.P. =  $0.07 \times 250 + 1.07 \times 125 = 151$ , and the efficiency is

$$125. \div 151 = 0.83.$$

### TABLE XXXI.

## FRICTION OF CORLISS ENGINE AT CREUSO

By F. Delafond, Annales des Mines, 1884.

Condensing with air-pump, tests 1-33.

Non-co	ndensing wit	hout air-pun	np, tests 34-	-46.	
	Cut-off Frac-	Pressure at	Revolutions	Horse-Pow	ver — Cheva
	tion of Stroke	Cut-off, Kilos per Sq. Cm.	per Minute.	Indicated.	Effective
ı	0.030	0.64	64.0	27.8	16.3
				60.0	37.6
3					45.2
4	0.065		64.0	117.0	88.7
5	0.065	6.20	61.0	138.5	106.3
ð	0.065	7.10	64.0	163.2	129.2
7	0.065	7.60	64.0	185.0	144.6
	0.100	0.16		21.0	10.6
9		1.55	60.0	61.9	42.3
	0.100	2.82	57.3		61.0
			58.3		106.7
					124.8
					28.4 28.7
					28.7 59.8
16					59.8 78.2
					145.0
īś					27.0
19				110.8	83.3
20	0.273	0.40	62.3	50.2	33.8
21	0.264	1.57	63.3	89.1	61.8
22	0.240	1.64	62.0	87.2	63.т
23	0.245	3.25	56.0	145.0	116.0
24	0.260	4.76	58.0	209.4	178.0
25	0.335	0.25	59.0	47.2	32.5
	0.339				90.0
27	0.338	2.97			133.0
			59.3		67.2
					67.9
					128.4
	I				191.0
32	0.50	2.70	61.5	215.5 TE 8	191.0
	1 2 3 4 4 5 6 7 8 9 10 11 12 13 14 15 16 17 18 19 20 21 22 23 42 25 26 27 28 29 30 31 32	Cut-off Fraction of Stroke  1	Cut-off Fraction of Stroke  I 0.039 0.64 2 0.044 2.40 3 0.045 4.90 5 0.065 7.60 8 0.100 0.166 9 0.106 1.55 10 0.100 2.82 11 0.090 4.80 12 0.142 0.76 14 0.137 0.71 15 0.132 2.50 16 0.147 4.05 17 0.155 4.65 18 0.167 0.22 19 0.197 2.55 18 0.167 0.22 19 0.197 2.55 20 0.273 0.245 1.57 21 0.264 1.57 22 0.245 1.57 24 0.260 4.76 25 0.338 2.97 28 1 20 1 1 0.47 21 1 0.47 22 1 0.338 27 0.338 28 1 1 2.70	Cut-off Fraction of Stroke    Cut-off Fraction of Stroke	Cut-off Fraction of Stroke    Cut-off, Kilos per Sq. Cm.   Revolutions per Minute.

0.70

6.00

7.00

0.50 0.120

0.106

33

35

61.5

60.0

53.0

216.5 215.5

132.5

125.0

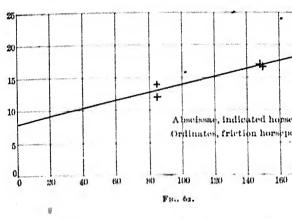
107.5

103.0

Table XXXI gives the retests made on a Corliss engboth with and without a pressures and cut off. The on Fig. 61, and those withe In both figures the abscissae

the ordinates are the frictio are represented by dots; the most economical cut off (on

friction than the other tests. The tests on this clearly that both initial and load friction are afficut-off and the steam pressure, and that friction be made at the cut-off which the engine is expecte service.



The initial friction was eight horse power be without condensation. But Fig. 61 shows that with condensation gave the best economy when 160 horse power; the friction was then 30 horse-pthe net horse-power was 130, which will be taken f horse-power  $P_n$ . Consequently

$$a = 8 + 130 = 0.06;$$
  
 $b = (30 - 8) + 130 = 0.17.$   
 $\therefore 1.\text{H.P.} = 0.002P_B + 1.17P.$ 

In like manner Fig. 62 shows the best ecor condensation, for about 200 indicated horse-pow the friction is 20 horse-power, leaving 180 for the

in friction, when developi sation it had 20; conseque

(36 -

of the indicated power.

to the high vacuum maint

Thurston's Experiments.

tests on non-condensing of with his advice, Professo for engines of that type load, and that it can, in ing the engine without a

T FRICTION OF 1

230

STRAIGHT-LINE ENGINE, 8

No. of Diagram.	Boiler- Pressure.	Revolutio			
I 2	50 65	232 229			
3	63	230			

lubrication and other minor causes rather than cof load.

Distribution of Friction. As a consequence of in the preceding section, Professor Thurston dec friction of an engine may be found by driving external source of power, with the engine in sul same condition as when running as usual, but without cylinder, and by measuring the power required the distribution of friction among the several mengine may be found by disconnecting the several mengine members.

The summary of a number of tests of this sort, fessor R. C. Carpenter and Mr. G. B. Preston Table XXXIII. Preliminary tests under norr showed that the friction of the several engines of the same at all loads and speeds.

The most remarkable feature in this table is the main bearings, which in all cases is large, both absolutely. The coefficient of friction for the r calculated by the formula

is given in Table XXXIV. p is the pressure on a pounds for the engines light, and plus the meather piston for the engines loaded; c is the circumbearings in feet; n is the number of revolution and H.P. is the horse power required to overcon

# TAE DISTRIBU

Parts of Engine.	troight line 6
Main Bearings	
Main Bearings	4
Piston and Rod	3
Crank Pin	

Valve and Rod . Eccentric Strap .

Total

Link and Eccentric . . Air-Pump . . . . .

TAI

100.

5.

### DISTRIBUTION OF FRICTION

The second and obvious conclusion from Tah that the valve should be balanced, and that ninefriction of an unbalanced slide valve is unnecessary

The friction of the piston and piston-rod is always but it varies much with the type of the engine, an ences in handling. It is quite possible to change power of an engine by screwing up the piston-ro too tightly. The packing of both piston and rod tighter than is necessary to prevent perceptible le more likely to be too tight than too loose.

# CHA

INTERNAL CO

RECENT advances in the been found in the developm and of steam turbines; the k. When first introduced the or bustion or gas engines was use to small sizes, for which ance offset the cost of fuel, horse-power was a large th time Mr. Dowson had succeedite coal and from coke in h

of 400 horse power were but as they had four cylinders that twice that of single cylinder fuel used in the producer with present time, gas engine

#### STIRLING'S ENGINE

perature, and the heat rejected must be given up at temperature. The hot-air engine is the only attem the example of Carnot's engine by supplying heat t drawing heat from a constant mass of working substant attempt to obtain the diagram of Carnot's cycle an engine would involve the difficulty that the act which the isothermal and adiabatic lines for air crevery long and attenuated diagram that could be obtain an excessively large working cylinder, with so m that the effective power delivered by the engine would ficant. This is illustrated by Problem 20, page 75. this difficulty Stirling invented the economizer or which replaced the adiabatic lines by vertical lines volume, and thus obtained a practical machine.

engine is still employed, but only for very small pump which are used for domestic purposes, as they are free

page 39) it was pointed out that to obtain the maciency all the heat must be added at the highest prac-

Stirling's Engine. — This engine was invented in was used with good economy for a few years, and the because the heaters, which took the place of the boiler engine, burned out rapidly; the small engines now little trouble on this account. It is described and its performance given in detail by Rankine in his "Steam-Engine." An ideal sketch is given by Fig. 63. E is a displacer piston filled with non-conducting material, and working freely in an inner cylinder. Between this cylinder and an outer one from A to C is placed a regenerator made of plates of metal.

ger and require little attention.

inner is pierced with holes t displaced by the plunger, pipe through which cold wat has free communication w

cylinder, and consequently , be packed in the usual man In the actual engine the

there are two displacer cylin cylinder.

If we neglect the action

cylinder H and the commideal cycle. Suppose the wof the forward stroke, and its cylinder, so that we may part of that cylinder or in the perature  $T_2$ , the condition by the point D of Fig. 64.

P A W D D

quickly stroke; s little tha The air

of the d rator, fro

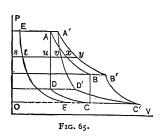
#### STIRLING'S ENGINE

stant temperature, as represented by the isothermal completing the cycle.

To construct the diagram drawn by an indica

assume that in the clearance of the cylinder H, cating pipe, and refrigerator there is a volume of a back and forth and changes pressure, but remains a ture  $T_2$ . If we choose, we may also make allowardar volume which remains in the waste spaces at of the displacer cylinder, at a constant temperature

In Fig. 65, let ABCD represent the cycle of oper out any allowance for clearance or waste spaces; volume will be that displaced by the displacer pix maximum volume is larger by the volume displaceding pixon. Let the point E represent the maximum the same as that at A; and the united volumes of at one end of the working cylinder, of the communications.



of the clearance at the top and bottom of the disp and the volume in the refrigerator and regenerate of this combined volume will have a constant to that the volume at different pressures will be repr hyperbola *EF*. To find the actual diagram A' any horizontal line, as sy, cutting the true diagram as Stirling's hot-air engine. To avoid do cant in the working cylinder Stirling four nect only t displacer cyl



Fig. 66.

mineral oil c

cylinder, an cylinders for It has been

the displace hot end also of the displacer cylinder of connected with the working cylinders, of Thus each working cylinder is connected

one displacer cylinder and with the displacer cylinder.

The distortion of the diagram Fig. 66 large clearance and waste space, and I the displacer pistons are moved by a cran

with the working crank.

A test on the engine mentioned by I

Johnson\*showed a consumption of 1.66 o

coal per horse-power per hour; but the fi

large, so that the consumption per brake pounds. This engine, like the original S isothermal expansion, and DA and BC take the constant volume lines on Fig. 64. To shalines are properly drawn, we may consider the eq

$$d\phi = \epsilon_v \frac{dt}{T} + (\epsilon_p - \epsilon_v) \frac{dv}{v}$$

which was deduced on page 67. For the lin BC the volumes are constant, so that the equal

$$d\phi = \epsilon_v \frac{dt}{T};$$

or transposing,

$$\frac{dt}{d\phi} = \frac{T}{\epsilon_{\mathbf{r}}};$$

but this last expression represents the tangent of the the axis  $O\Phi$  and the tangent to the curve. This is (but with a diminishing ratio) with the temperatis constant for a gas, the angle depends only on the  $T_i$ , so that the curve BC is identical in form with and is merely set off further to the right; in consolike WX and ZY between a pair of constant ten are identical except in their positions with regard to. Suppose now that the material of the regene temperature  $T_i$  at the lower end and  $T_i$  at the unthat the temperature varies regularly from bottom pose further that the air when giving heat to the (or receiving heat from it) differs from it by only able amount. Then the diagram of Fig. 67 will

ideal action correctly, and it is easy to show that

Moreover, the small amount ZY at the temperature T heat yielded during the open

so that there is no loss of et mentioned are represented by It can be shown that one c

at random, provided that the tical and set off further to importance enough to warra

In practice a regenerator temperature than the air frehigher temperature than that of air is rapid. The loss of of the original Stirling engine temper cent. It may be pre-

state that regenerators are r

at the present day.

Gas-Engines. The chief to transmit heat to and from the engines this difficulty is remain (so that heat is developed and by rejecting the hot gas

The fuel may be illuminating

Gas-Engine with Separate Compressor. -

engine itself; the second type of engines, engine is an example, is the only successful time; the other type has some advantages when development.

a compressor, a reservoir, and a working cyas a gas-engine a mixture of gas and air is dr compressor, compressed to several atmosphe a receiver. On the way from the receiver to the mixture is ignited and burned so that t volume are much increased. After expans cylinder the spent gases are exhausted at atmosphere.

The ideal diagram is represented by Fig. the supply of the combustible mixture to the

compressor, DA is the adiabatic compression, and AF represents the forcing into the receiver. FB represents the supply of burning gas to the working cylinder, BC represents the expansion, and CE the exhaust. In practice this type of engine always has a release, represented by GH, b

has reduced the pressure of the working subs

This type of engine has been used as an oilthe fuel in the form of a film of oil to the a compressed. In such case the compressor and there is not an explosive mixture in Brayton engine when run in this way could bu or, after it was started, could burn refined

defect appears to have been incomplete con

atmosphere.

temperatures correspondin

heat added from A to B i 
$$v_p$$

and the heat withdrawn fr

so that the efficiency of the

$$e^{-\epsilon_{p}+T_{r}} = \frac{r_{p}+T_{r}}{\epsilon_{p}+T_{r}}$$

But since the expansion

$$\frac{T_{i}}{T_{i}} = \begin{pmatrix} f \\ f \end{pmatrix}$$

but  $p_e = p_d$  and  $p_b = p_m$ 

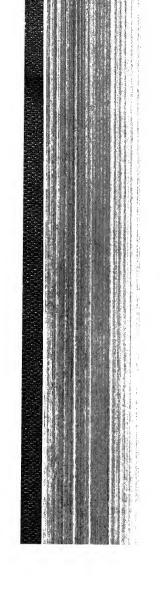
$$\frac{T_x}{T_x} = \frac{T_x}{T_x}$$
 and  $\frac{T}{T_x}$ 

so that the equation for eff

8

has the advantage of replacby a simple ideal operation efficiency. How far the icthe probable advantages of degree of approximation,

This discussion of ideal ef



above the atmosphere the efficiency is

$$e^{-1} = \begin{pmatrix} \frac{1.405 - 1}{1.405} \\ \frac{1.405}{1.405} \end{pmatrix} = 0.43.$$

When the cycle is incomplete the expression for the is not so simple, for it is necessary to assume cooling volume from G to H (Fig. 68), and cooling at constant from H to D; so that the heat rejected is

$$c_v (T_g - T_h) + c_p (T_h - T_d),$$

and the efficiency becomes

$$e = 1 - \frac{\frac{1}{\kappa} (T_g - T_h) + (T_h - T_d)}{T_h - T_d}.$$

For example, let it be assumed that the pressure pounds above the atmosphere, that the temperature a F-, and that the volume at G is three times the volume

First, the temperature at A is

$$T_a = T_d \begin{pmatrix} p_a \\ p_d \end{pmatrix}^{\frac{\kappa}{\kappa}} = (60 + 460) \left( \frac{1.4.7 + 90}{1.4.7} \right)^{\frac{0.405}{1.405}}$$

provided that the temperature of the atmosphere is 6

The temperature at 
$$G$$
 is
$$T_g = T_b \left(\frac{v_b}{v_l}\right)^{\kappa - 1} = 2900 \left(\frac{1}{2}\right)^{0.405} = 1897$$

and the pressure at G is

$$p_{\sigma} = p_{\delta} \left(\frac{v_{\delta}}{v_{\sigma}}\right)^{\kappa} = (14.7 + 90) \left(\frac{1}{3}\right)^{1.405} = 22.4 \text{ pc}$$

so that the temperature at II is

in the working cylinder.
end of the cylinder only,
the cycle, so that there is o
working at full power. S
four-cycle engines. Some
of the cylinder accomplish
as two-cycle engines; they
tion when single-acting.
have been made double-ac
stroke of the piston from
mixture of gas and air, wh
at the completion of this re
the pressure rises very ra

Gas-Engines with Computed gas-engines of the present

The most perfect ideal

strokes.

working stroke, which is expel the spent gases. In are of equal length, for the length, as required for the terbalanced by the mecha and withdrawing heat at constant pressure fr with the adiabatic expansion and compression

The heat added under this assumption is 
$$c_n(T_a - T_d)$$
,

and the heat rejected is

$$c_p (T_b - T_c),$$

so that the efficiency is

$$e = \frac{c_v (T_a - T_d) - c_p (T_b - T_c)}{c_v (T_a - T_d)} = 1 - \kappa$$

If the temperature at A and the pressure then it is necessary to make preliminary temperatures at D and at B before using equ

adiabatic compression from C to D gives at D

$$T_d = T_c \left( \frac{p_d}{p_c} \right)^{\frac{\kappa - 1}{\kappa}}$$

in like manner adiabatic expansion from A

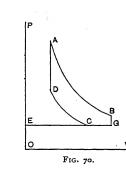
$$T_b = T_a \left(\frac{p_b}{p_a}\right)^{\frac{k-1}{k}}$$

provided that the temperature

$$p_a = 104.7 \frac{2500}{91}$$

 $T_b = (2500 + 460)$ 

$$e = 1 - 1.405 \frac{110}{200}$$



to cau

G, and

stant

 $c_v (T_b - C_b)$ 

If the atmosp shows as in a consider heat as by with

1.1 00 :

represented by GC. The he

and the efficiency is

## GAS-ENGINES WITH COMPRESSION IN THE CY

For example, let it be assumed that the expande when the pressure becomes 20 pounds above the the other conditions being as in the previous examp

$$T_b = (2500 + 460) \left(\frac{14.7 + 20}{338}\right)^{\frac{0.405}{1.405}} = 153$$

$$T_g = 1536 \frac{14.7}{34.7} = 650;$$

and

$$e = 1 - \frac{1536 - 650 + 1.405 (650 - 520)}{2960 - 917}$$

Though not essential to the solution of the exinteresting to know that the volume at C is

$$\left(\frac{90 + 14.7}{14.7}\right)^{\frac{1}{\kappa}} = 4 +$$

times the volume at D, and that the volume at B is

$$\left(\frac{338}{34\cdot7}\right)^{\frac{\tau}{\kappa}} = 5 +$$

times the volume at A.

When, as in common practice, the four strokes of the piston are of equal length, the diagram takes the form shown by Fig. 71; the effective cycle may be

The heat applied is

and the heat rejected is

so that the efficiency is

$$e = \frac{c_{\rm r} \left(T_a - T_d\right) - c_{\rm r}}{c_{\rm r} \left(T_a - T_d\right)}$$

Since the expansion and the equations

$$T_b v_b^{\kappa-1} = T_a v_a^{\kappa-1}$$

but the volumes at A and I at B and C; consequently by

consequently

$$\frac{T_b - T_c}{T_a - T_d}$$

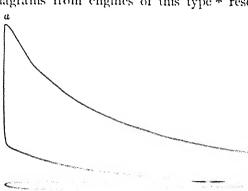
and the expression for effici

## GAS-ENGINES WITH COMPRESSION IN THE C

pounds absolute, or 88.4 pounds by the gauge, efficiency is therefore not much less than the efficie other examples; it is notable that the efficiency same as that calculated on page 307 for an engine compression to 90 pounds by the gauge. For the however, the pressure after explosion, which de-

temperature, may exceed 300 pounds per square.

The diagrams from engines of this type \* rese



Fu. 74.

which was taken from an Otto engine in the lal Massachusetts Institute of Technology. During stroke, the pressure in the cylinder is less than the

of 20 to the inch, and with a piston; the upper part of appear in the figure. The pounds, and the reduction of



three and four pound, be the influence of the negat indicated horse power will

The compression line do or in reality from an adiable be expected to receive heat the first part of the compreducing the latter part. To the adiabatic line for a

for large engines; but in are very different, for the a

## CHARACTERISTICS OF GASES

and adjuncts must be adapted to the conditions, gas is made from coke, anthracite, or from non-caking coal, and consists mainly of hydrogen and carbon more with the nitrogen of the air, together with five or of carbon dioxide and a small percentage of hydrocacially when bituminous coal is used. Illuminating commonly made by the water-gas process, which yie very unlike producer-gas, but that gas is enriched carbons of varying composition; formerly illuminated distilled from gas-coal, which was a rich bituminous a large percentage of hydrocarbons when distilled.

and, if the gas is to be used for generating power,

The general characteristics of illuminating gas are by the following analysis of Manchester coal-gas of the first edition of Clerk's *Gas Engine*, and used investigate the effect of combustion on the volume of

ANALYSIS OF MANCHESTER COAL GAS. (Bunsen a

Vols. O required

	Vol.	for Combustion.	
Hydrogen, H		22.70 60.8	45.58,
Carbon monoxide, CO	to to		6.61

316 INTERNA COMPOSI

details are given on pagoriginal paper, which ar Rich non-caking bitur larger proportion of hyd

In a paper on the use of gives the composition of Scotland, and Germany, following table were de-

COMPOSITIO

### CHARACTERISTICS OF GASES

The amounts of oxygen required for the combustion volume of any gas can be computed from the for resenting the chemical changes accompanying of together with the fact that a compound gas occupies twif measured on the same volumetric scale as the gases. Thus two volumes of hydrogen with one oxygen unite to form superheated steam as represent formula

$$_{2}H + () = H_{_{2}}(),$$

and the three volumes after combustion and reduct original temperature are reduced to two volumes; in to have the statement hold, the original temperature verous to be very high, to avoid condensation of the steam. But in the application to gas-engines this leads to no ience, because the gases after combustion remain at a perature till they are exhausted, and the laws of gassumed to hold approximately. A compound gas like can be computed as follows:

$$CH_4 + 4O = CO_2 + 2H_2O_1$$

Since the compound gas methane occupies two vorequires four volumes of oxygen, it is clear that each of that gas will demand two cubic feet of oxygen; the to

but in practice the producer volume of air, so that the coin 230 to 250 volumes, and contraction.

Clearly this matter has page 300, as to the reliance which assume heating of a For illuminating gas that a and for producer gas the destroy the value of the met

Temperature after Explose concerning the theoretical the determination of the to

determination is difficult beture and the very short into mum temperature can be o

A comparatively simple explosion can be made from pression can be assumed to perfect gases can be applied line measured on an ordina

pressure, is 61 pounds, or perature of the gases in the

## AFTER BURNING

are and remain the same as those of gases at orditures, can be taken as a first approximation only.

In connection with tests on a gas engine (see pa

illuminating-gas, Professor Meyer makes a careful of the temperature which might be developed in of a gas-engine if the charge were completely bur conducting cylinder. The results only will be The composition of the gas will be found on particle that it was probably coal-gas, by use of which Fig. 72 was obtained. The end of compression was 60 pounds by the gas explosion was 220 pounds, so that the conditions different from those of Fig. 72, except that the 4 compression line is not on the ordinate for measurement pressure, and therefore the parallel calculations.

On the assumption of constant specific heats P finds that complete combustion should give 4250 conducting cylinder, but using Mallard and equation for specific heats at high temperatures be Those experimenters report that dissociation of ca

begins at about 3200° F., and of steam at about

made.

time. The actual e for gas, and for lar represented by the

but a part of this a carbon monoxide and may reduce the expe

Water-Jackets, engines have the he water-jackets; large with water, and dot stuffing-boxes cooled, cooling surface is 1

chamber; the latte former is in part fo Primarily, water j

and to make lubrica cooling devices has I many inventors hav it is only a question

water-jacket, or whe

# ECONOMY AND EFFICIENCY

and oil-engines have been rated in pounds of fu power per hour. The variation in the fuel used for makes the secondary methods less satisfactory than a on steam-consumption, so that it should be employ the calorific capacity of the fuel cannot be d estimated.

Since the heat equivalent of a horse power is .

units per minute, the actual thermal efficiency of combustion engine can be determined by dividin by the thermal units consumed by the engine per per minute. For example, the engine tested by Proused about 170 thermal units per horse-power and its thermal efficiency was 0.25, using the incover. The ratio of the cartridge space to the

was  $\frac{1}{3.8.4}$ , so that equation (187) gives in this cas

nominal theoretical efficiency; consequently the efficiencies is nearly 6.66.

By a somewhat intricate method Professor Me the efficiency for two tests on the engine for whigiven on page 350, on the assumption that compleoccurred in a non-conducting cylinder. The ratio heat, be taken as the basis of conthe ratio of actual to theoretical eff

 $0.253 \div 0.398 = 0.64$ , or If, however, we take his second value we have

because, if the nominal theoretical basis of comparison, there apper improvement in the economy of

second set of computations is take prospect of improvement. In co

the fact that these tests were on a

only ten brake horse-power.

In the discussion of efficiency we

heat-consumption per indicated because the fluid efficiency (or the working substance) should for the confusion with the friction and engine. For the same reason, an

steam-engine can be determined

# ECONOMY AND EFFICIENCY

the indicator piston from rising too high which effects of an idle cycle and other features. A po expansion curve is shown, with oscillations due to suddenly leaving the stop. The exhaust of the specific content of the spe



Ftt. 74.

shown by the curve ab, after which the engine dra of air (without gas) and compresses it on the uppe c to d; on the return stroke the indicator follow curve from d to c, so that the loop represents work engine; finally the air is exhausted, while the indicator the line cc. To explain the difference between the

ab and ce with spent gas and with air only, it may be

time considerable import out spent gas, but it attra engines.

In indicating a gas-eng

the negative work of exha allowance for the negati Fig. 74 should be made for has only a few working cy of the negative work may another reason why comp power. As can be seen

continuous explosions, an reduced if explosions are
Two-cycle engines co
which supplies the mixtur
ten pounds above the atm

mechanical efficiency may depending mainly on the

pression must be determine measurement of the indic Valve-Gear. — The support of the pression of the indic valve-Gear.

combustion engine are least two valves (or the

### STARTING DEVICES

remaining closed during the compression, exp strokes; but very commonly the admission and for gas (when the latter are separate) trolled, and for very high speeds this action

From what has been said, it will be evid problem of the design of the valve-gear for

tion engine resembles that for a four-valve cially that type of steam-engine valve-gear lift-valves. The solution which is most evimonly chosen is some form of cam-gear; us held shut by springs, and are opened by ca either directly or through linkages. This of iently placed parallel to the axis of the cylin the main shaft through bevel-gears; the fe the gear in the ratio of one to two, so that t one revolution for two revolutions of the properly time the four principal operations spring closing a valve must be properly d give the required pressure to hold the valve the proper acceleration so that the valves the control of the cam when closing. The

tion to the cams for the normal action of the

which facilitate starting the engine.

formed, whereupon the for very small sizes, to into action, and white piston has completed which the charge is proposed to manner the ignit

the operations of cha

and there is great dar.
When electric or of hand-power, this met

past the dead-point, oward. The disengag

large size.

A very common de air from a tank at a inch. This air is su the engine when necedisconnected tempora

and is worked like a way, whereupon the action is restored. T

valves controlled by l

for controlling the power of an internal-combustic by regulating the proportion of air and fuel, (2) the amount of air and fuel without changing the (3) by omitting the supply of fuel during a part of delaying ignition.

(1) Regulation by controlling the supply of fue method for engines working on the Joule or Bray compression in a separate cylinder, for which a treussion is given on page 305. For this cycle the sion, but the gaseous or liquid fuel can be burned sion in any proportion.

The Brayton engine had a double control fo load. In the first place a ball-governor shorten for the working cylinder when the speed increase of reduction in the load; this had the effect of rassure in the air reservoir into which the air-pump d that pump delivered nearly the same weight of under all conditions. In the second place, there we ment for shortening the stroke of the little oil-pupressure increased; so that indirectly the amoun proportioned to the load. A similar effect was p the engine was designed to use gas.

For the Diesel motor, to be described later, the can be adjusted to the power demanded for all service.

But for gas-engines it has not been found practical the engine by regulating the mixture of gas a within narrow ranges. This comes from the fact or very poor mixtures of gas and air will not explain at the Massachusetts Institute of Technology.

that even though the extension of the work.

The tests on page 350

varying from 1:8 to 1 brake horse-power.

This discussion of the

varying the mixture of for many purposes that: a gas-engine. Neverthe it was tried early.

(2) The common was vary the supply of the There are two ways of charge may be throttled lower pressure; in the sclosed before the end of supply. The effect of the reduction of pressure sponding increase in the

like that shown by Fig. of closing the inlet-valv

the brake economy of the engine. Now, a sin cycle engine has only one working stroke in four nish between times the work of expulsion, filling sion, and even with a very heavy fly wheel will a larity in speed of revolution that is very objection purposes. This difficulty is very much increase is governed by omitting explosions on the hit or

small power the negative work of idle cycles ver

(4) Delaying ignition is one of the favorite we the power of automobile engines on account of it is little used for other engines, and is very was there is not time for proper combustion.

Ignition. The ignition of the charge may one of three methods: (1) by an electric spark, (2 or (3) by compression in a hot chamber.

(1) The electric spark may be produced in o

— by the make and break method, or by the jum For the first method a movable piece is worked der walls, which closes a primary circuit some t tion is desired; the slight closing spark has no proper time the moving mechanism breaks th good spark is made between the terminals, w with platinum. A coil in the circuit intensifie opening spark. The spark obtained by this r

to be better than the jump spark, but there is venience of a moving mechanism in a cylinder high pressure, and the motion must be com-

piece which enters the cylinder through a stuffin.

The jump spark between two platinum termilated spark-plug, screwed through the cylinder.

The circuit may be supgenerated by a small dynsupplied from any converplied, the engine is usuall

The electric method of history of the gas engine, a now tends to become univ

(2) The hot tube required kept red hot by a Bunser tube comes out horizont, is turned upward for continue the explosive mixtuitube by a valve which the tube has an inlet value with air drawn in all

has been widely used in

method has met with litt it is passing away.

(3) Ignition by comprused exclusively in oil en

taking advantage of a country undesirable. The mixtu

#### GAS PRODUCERS

same way. Premature explosion in a small e started may be an inconvenience, but in a larglead to an accident.

Gas-Producers. A gas producer is essent

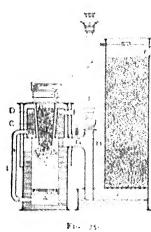
which burns coal or other fuel with a restricted that the combustion is incomplete and the production are capable of further combustion. In its gas-producer will deliver a mixture of carbornitrogen together with small percentages of carbornitrogen together with small percentages of carbornitrogen. If a proper proportion of steam the air, its decomposition in contact with the it will yield free hydrogen, and the gas will give a when exploded, and develop more power in the

intricate devices may be used to rectify the aby-products, which are likely to be so imports the methods employed. The most important the present time appears to be ammonium so used as a fertilizer, and for this reason a coal is has a relatively large proportion of nitrogen station a coal containing three per cent of a crude ammonium sulphate that could be sold of the coal. This branch of chemical engineer

When gas is produced on a large scale in a

the present time the fuels. caking bituminous coal. tion, at St. Louis in 1904, a caking bituminous coal and plant, and it is likely that used in practice.

Fig. 75 gives the section which A is the grate carrying



through the mine /

cite; those that burn bituminous coal must have of dealing with tarry matter. Sometimes this is by passing the gas through a sawdust cleaner centrifugal extractor is added. Some makers r by care in cooling before the gas comes in conta Others pass the distillate through the fire, and into light gas or burn it; with this in view, some p with a down-draught. It is probable that diff fuel will need different treatments.

Blast-furnace Gas. — From the composition of gas on page 316, it is evident that it differs from only in that it contains very little hydrogen, and like the gas that would be made in a producer we steam. During the operation of the furnace the is liable to vary and the gas may become too we this difficulty, it is desirable to mingle the gas more furnaces. Since the gas available from the equivalent to 2000 horse-power, it is evident that to develop power from that source must be of scale.

The gas from a blast-furnace is charged with a of dust, some of which is metallic oxide, and reand the remainder is principally silica and lime fine and light. To remove this fine dust the passed through a scrubber, which has the addition of cooling the gas.

Other Kinds of Gas. — Any inflammable gas the nished with sufficient regularity can be used power. The gas from coke-ovens is a rich producer-gas in its general composition. Natural of 90 to 95 per cent of methane (CH<sub>4</sub>) with a small phydrogen and pitrogen and traces of other of the producer of phydrogen and pitrogen and traces of other of the producer.

Gasoline. The lighter line, are readily vaporized the most ready means of stof several hundred horse have been built for small of gasoline has been limited craft and to automobiles;

for business, other things tion of the engines. The tively small power used fo

The most vital feature is or carburetor, and this especially for automobile speed.

There are three types of

gasoline engines; at these those that depend on as depending on aspiration depended on direct vapor mass of the third, or throface of wire gauze; some a a regulation of feed that a supplied, leaving only a

in any case there was a cl resulted in the producti

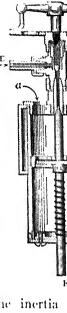
thuid.

The more recent carba supply being drawn past line is supplied, and from more or less in proporti

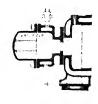
### KEROSENE OIL

A third form of carburetor is illustrated by the gasoline is supplied by a pipe E to a valve t to give good average action. Below is a fine of the end of a vertical rod which is held up by a light spring; at the middle of the spindle is a diskvalve which fit sloosely in a sleeve. At aa are air inlet valves, and at A is the entrance to the cylinder. During the suction or filling stroke the spindle is drawn down, opening the valve at the top of the spindle and allowing the air to draw gasoline by aspiration. Some of the hot products of combustion from the exhaust are circulated around the aspirating chamber to prevent undue reduction of temperature. This type of carburctor works well enough at moderate speeds, but at very high speeds the inertiaand disk-valve cannot be overcome rapidly enor

which is consequently throttled, so that there is r of warrant relative materials are a min to the contract of



of this engine is shown in of the cylinder head and a



Fis. 77.

from a vaporized bolted to end is cylinder which is conseque

the engi

the engine is running. The into this hot end of the vary with the hot spent gases; the stroke the charge of air pressed enters the various the vaporizer head has been running, depending on the the hard adherent deposit head is put on for a context.

governed by controlling the bypass valve on the oil supto the tank. The hit or material vaporizer would become too

# THE FOUR CYCLE ENGINE

appears to be no reason why there should be troul of some form of carburetor like those used for gas

The Four-cycle Engine. - Fig. 78 gives a vertice Westinghouse four cycle gas engine built in various horse-power with one cylinder, and up to 300 with the Massive engines of this type are horizontal

acting pistons, having two cylinders tandem or four twin-tandem. It is somewhat curious while massive steam-engines tend to wards the upright con struction, large gas engines appear to be all horizontal; it may be for the convenience of the tandem arrange ment. In Fig. 78 the frame of the engine is arranged to form an inclosed crank case, which is somewhat unusual for gas engines. The piston is in the form of a plunger, so that no cross-head is needed;

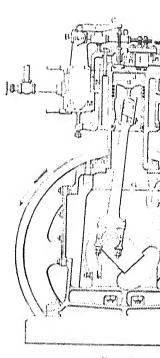


Fig. 78.

a common arrangement for all except massive. The cylinder barrel and head are water jacket

to give any desired miareas for gas and air areas remain unchange piston valve to give the demanded by the load of the exhaust valve E are indicated, the cams inrevolution of the engir Large sizes have the of burning the valve, and t

that can be moved by I

# Two-cycle Engines.

there is a handle for shi reduces compression who low tension make and be thrown into action; they operates the valve J.

which exhaust the spent performed with a present lower than that of the advantage provided the other way. The first s was that by Dugald Cl regularity of rotative velocity. The engine could twice as much power for its size as a four-cycle er certain tests by Mr. Clerk, showed a slightly bet than the older type of engine. But the operation the remnants of the spent charge by the fresh charge of this type is rather delicate, there being a chance the spent charge will remain, or that some of the will be wasted; it is likely that the charges mingle engine experiences both defects. Eventually the was withdrawn from the market, but the principles two types of engines: (1) small gasoline engines for other small craft, and (2) large engines built for b furnace gas.

Gasoline engines of small power and moderate r

have been made on the two cycle principle by or crank- and connecting rod in a casing, so that the pit as the compressing pump. On the up stroke a cand gasoline is drawn into the crank case, and it is pressed on the down stroke. There are two sets through the cylinder walls near the end of the down are opened by the piston; these are on opposite cylinder; one set, which is opened slightly earlier the forms the exhaust ports and the other the inlet ports communication with the crank case, and therefore and gasoline to replace the spent charge. A barrithe cylinder-head which prevents the fresh charge directly across from the inlet to the exhaust, but never action is probably much inferior to that of Clerk's chad the charge supplied at the cylinder-head. These

engines have been introduced Two German engineering for especially for burning blastas 1500 horse-power in a sing

Company) is a double-actin as long as the stroke of the of the cylinder is a ring of the end of each stroke, an one end of the cylinder and engine-cylinder, and arrang driven by one crank (which one for compressing air, as

The Körting engine (bu

of the two pumps are deburned.

The air-pump compresses phere and delivers air to the cams at the time when the state of the cams are two pumps are designed.

pump in communication is stroke of that pump, which the first place the compressi

controls a bypass-valve v

## THE DIESEL MOTOR

plungers in a long open-ended cylinder; these connected to cranks at 180° so that they approa from the middle of the cylinder simultaneously. has a cross-head at each end of the cylinder to ta thrust of the connecting-rod, so that the engine great length on a horizontal foundation. Towar end of the cylinder there is a ring of exhaust-ports the inner (or crank-end) piston, and toward the ou cylinder there is another row uncovered by the or part of these outer ports supply air, and a part gas and gas-ports may be controlled by annular valve by hand when the engine uses blast-furnace gas. conditions the engine is regulated by a governor, v the pumps that supply air and gas. These pum driven from the outer cross-head, have bypassconnect the two ends and begin to deliver o bypass valves are shut by the governor, so that adjusted in amount to the load. When the engir gas that has a wide explosive range, the governor annular valves at the gas-ports and varies the mixt

The Diesel Motor. A new form of internengine was described by Rudolf Diesel in 1893

away with many of the difficulties of gas- and oil-engines, and which at the same time gives a much higher efficiency. The essential feature of his engine consists in the adiabatic compression of atmospheric air to a sufficient temperature to ignite the fuel

ger. Atmospheric air is drawn pressed from b to c to a p square inch and a temperature is injected in a finely divided excess it burns completely at by the injection mechanism. is petroleum or some other of

interrupted, and the remainder is an adiabatic expansion. The at e and a rejection of the proof.

The cycle has a resemblance

The cycle has a resemblance differs in that the air only is of the combustion is accompanied his theoretic discussion of his of combustion shall be so regulated not rise during the injection of therefore be very nearly an isot the fuel is added during the or

cd, the weight of the material is physical properties change, so isothermal. The fact that there

# THE DIESEL MOTOR

rise of temperature, or that there is any great adva a regulation if the temperature is not allowed to ris The diagram from an engine of this type is show

which appears to show an introduction of fuel

or one-seventh of the working stroke. It is prol compression and the expansion (after the cessati supply) are not really adiabatic, though as there i dry gas in the cylinder during those operations may not be large. The sides and heads of the c the engines thus far constructed are water-jac the use of such a water-jacket and the consequent was one of the difficulties in the use of interengines that Diesel sought to avoid by controlli combustion. The statement on page 30 that efficiency is attained by adding heat only at the perature has no application in this case. The i are that heat cannot at first be added at a temp than that due to compression (about 1000° F.), h tion proceeds heat can be added at higher ter with greater efficiency. The fuel may be regui avoid temperatures at which dissociation has an after burning can be avoided.

The oil used as fuel is injected in form of a sp

engines, by the necessity to form a discussion of the theoretical efficiency the efficiency increases as the time of in In practice the engine shows a sliglight loads, due probably to the loss

water-jacket, which are nearly consta

In the exposition of the theory of that all kinds of fuel, solid, liquid, a in his motor. As yet oil only has beleum or other heavy oil has probabof such oils. It is evident that gas of engine; the gas can be compress

of engine; the gas can be compress somewhat higher than that in the rair is which is used for injecting oil. sary to cool the gas after compressio supplied with air.

There appears to be no insurmous ing powdered solid fuel to this engash from such fuel in the cylinder to give trouble. Diesel claims that (for example, a hundred pounds of

the ash will be swept out of the cy

### THE DIESEL MOTOR

A theoretical discussion of the efficiency of the simple engine as represented by Fig. 79 may be considering that heat is added at constant temp to d and that heat is rejected at constant volume.

bearing in mind that bc and dc represent adiabat From equation (75), page 63, the expression supplied from c to d is, for one pound of working

$$Q_1 \sim A p_c v_c \log_e \frac{v_d}{v_c} - ART_c \log_e \frac{v_d}{v_e}$$

The heat rejected at constant volume is

$$Q_2 \sim \epsilon_v \left( T_e \sim T_b' \right) - \frac{\epsilon_p}{\kappa} \left( T_e \sim T_b \right)$$

Since the expansion de is adiabatic,

$$T_e = T_d \left(\frac{v_d}{v_l}\right)^{\kappa - 1} = T_c \left(\frac{v_d}{v_l}\right)^{\kappa - -1};$$

but since the compression be is also adiabatic,

$$T_c = T_b \left(\frac{v_b}{v}\right)^{a-1},$$

and consequently

$$T_e = T_h \left( \frac{q_h}{q_h} \right)^{\kappa + \gamma - 1} \left( \frac{q_d}{q_h} \right)^{\kappa + \gamma - 1} = T_h \left( \frac{q_d}{q_h} \right)^{\kappa}$$

temperature  $T_5$ . The latter atmosphere, but  $T_2$  by reducing the clearant pressure at the end a may be increased by reinjected, that is, by reduby a series of calculation This is a very important will have in practice little loads.

It is reported that a cent is associated with temperature of 1999 of the atmosphere at 14.7 pression to \$100 pounds absolute requires a clear

so that the clearation is

# ENGINES FOR SPECIAL PURPOSES

The equation for efficiency gives in this case

$$e = 1 - \frac{778 \times 0.2375 \times 530 \left\{ \frac{0.1716}{0.0796} \right\}^{0.405} - 1}{1.405 \times 53.22 \times 1480 \log_e \frac{0.1716}{0.0796}}$$

Engines for Special Purposes. - Small engines

to give any required degree of regularity for elect purposes, by giving a sufficient weight to the large power the same object can be attained by us of cylinders, by making the engine double acting, struction of two-cycle engines, or by the combinati

more of these devices.

well as impracticable.

The four-cycle engine has not as yet been ma and even if the complexity of valve-gear for rur directions could be accepted, it appears likely t starting device would be required for every reversa launches and automobiles is done by aid of a mech ing gear, except that for some small boats a rever

Two cycle engines would not require much co

is used. Such gear for large ships appears to be

group could be connected worked without compression convenient place could whole system. Such at the same certainty of ma

The application of a considered to be accouthat can use all grades qualities.

Automobiles are corengines, and have a rdevices, including clubble when the carriage is stated for running slowly and call of this entails weigh line vehicles can be hand not the facility of contro-The speed and power.

Economy of Gas-Eng the economs of gas en

and by delaying the is the methods of control,

well adjusted.

# ECONOMY OF GAS-ENGINES

- (5) Time of ignition.
- (1) The influence of compression is indicated the equation (187), page 312, which shows that the efficiency expected to increase progressively with increasing To exhibit this feature and to compare it with the res in practice, the following table has been computed for

and 7 of Table XXXV, page 350. The composition of ating-gas used was similar to that on page 315; detailed report of these tests shows little variation in

Number of tests	. 2	5
Ratio of compression	. 4.98	4.59
Theoretical efficiency	. 0.479	0.461
Thermal efficiency .	. 0.270	0.264
Ratio	. 0.564	0.573

Such a comparison is commonly considered to sactual efficiency follows the theoretical efficiency being based on the indicated horse-power, and be by dividing 42.42 (the equivalent of one horse-power units per minute) by the thermal units per indicated

per minute. But if the brake horse-power is taken of comparison, as has already been shown to be appears to be practically no advantage in the higher

kinds of gas the richest basing the comparison of The first trio of tests show

GAS-ENGINE WITH 11.1

PROFESSOR MEYER, Mittell

	до гусуулган ана наган танаас тар зарандагайда тадабайдага того, того	Congressed	The state of the s	Beate borne power
	VID-UP		1	
1	- 4	4 19%	101	363 3
2	75	4 13%	2534	24 1
3	Bummaing-Ca	4 13%	384	₹n 3 }
4	123	4.50	3 8 796 3	12 7
5	2	4 59	2000	25 3
0	E	4 60	2532	E 2
7	\$100g	3.84	2537	10 4
9.65		8 WR 1	- 44	7 1940 144 1

### ECONOMY OF GAS-ENGINES

eight to one will give the minimum per brake horse-power. remainder of the table is less conclusive, but it appears that a ratio of eight volumes of illuminating-gas to one vof air is proper, and that for power-gas the ratio should be what larger than unity.

(3) A committee of the Institution of Civil Engineers \* three gas-engines of varying size, but all having the same of compression, and tested under the same conditions. results that bear on the question of size are as follows:

Brake horse-power . . . . . 5.2 20.9 52.

Thermal units per horse-power per aminute

It is to be remarked that the results just quoted are rema low, but that the composition of the committee and the p tions taken, place them beyond cavil. It is somewhat diffiaccount for the difference between the results just quoted those given in Table XXXV, though part of it is due to the mechanical efficiency of the former. This was estimated about 0.87, while that of the engine tested by Professor was about 0.72; allowance for this difference may be estimated.

to reduce the results of the first test in Table XXXV thermal units per brake horse-power per minute. This trates an inconvenience of using the brake horse-power

Professor Meyer ma the influence of the time results following:

Lead of ignition, Thermal units per indicated horse power per

minute

This appears to show the same result for th undesirable.

The question as to engines has been considerable for various con. The best result that is committee of the Institu-

thermal units per horse.

1

brake horse power.
volume:

Hydrocarbons Methane CH<sub>4</sub> Hydrogen Carbon monoxide

#### A PRODUCER-GAS PLANT

development of power by the combination of a Taylor ducer with necessary adjuncts, and a three-cylinder Wesgas-engine; a detailed report of the tests is given by Parker, Holmes, and Campbell,\* the committee in characteristics.

The gas-producer had a diameter of 7 feet inside lining, and at the bottom was a revolving ash table diameter; the blast was furnished by a steam-blower from a battery of boilers used for other purposes; t made to determine the probable amount of steam tak blower, but the variation of steam-pressure acting at t during tests made this determination somewhat unsa The cost of the steam in coal of the kind used for any

be estimated closely from boiler-tests made with the sa The gas from the producer passed through a coke and then through a centrifugal tar-extractor using amount of water. From the extractor the gas passe

a purifier filled with iron shavings to extract sulphur way to the engine the gas was measured in a meter.

The engine-cylinders were 19 inches in diameter are inches stroke. At 200 revolutions the engine was rat

brake horse-power. The engine was belted to a diregenerator, and the energy was absorbed by a water-rho

The results of a test on a bituminous coal from Wes

TEST

Duration, hours Total coal fired in prod Coal equivalent of stear Coal equivalent of power Total equivalent coal . Thermal value of total, Total gas (at 62° F. and Thermal value of total

Efficiency of producer

Electrical horse-power Mechanical efficiency, e Brake horse-power . . Gas per horse-power pe

Thermal units per horse Thermal efficiency of b Coal per brake horse-po

It is interesting to co plant with the tests from which the results

Combined thermal effici

TEST AT CE

Coal required by plant, Thermal value of Georg

Heat abstracted from or Efficiency of boiler Indicated harse-nower

Duration hours,

# ECONOMY OF A DIESEL MOTOR

correspond to one pound per brake horse-power per of a pound per indicated horse-power; the maker power-plants are now ready to guarantee a coone pound of anthracite per brake horse-power

Economy of Oil-Engine. — An engine of the typ page 335 was tested by Messrs, A. E. Russell and of the Massachusetts Institute of Technology, had a diameter of 11.22 inches and a stroke of 15 220 revolutions per minute developed ten brake the mechanical efficiency was about 0.72, so that power was about 14; the clearance or charging sp

With kerosene the best economy was 1.5 pour horse-power per hour; this kerosene weighed per gallon, flashed at 10.4° F., and had a calo 17,222 thermal units per pound.

0.44 of the piston displacement.

The engine was also tested with a crude d comes from petroleum after the kerosene, weighin per gallon, with a flash point at 148° F., and hav power of 19,410 thermal units per pound; of this

used 1.3 pounds per brake horse power per hour.

The thermal units per horse power per minute horses and 1.50 for the distillate: the thermal officers and 1.50 for the distillate:

power, the oil-consul (34.4 horse-power) th

Distribution of Ho

The following tabl

Dimension of Engine.

> $6.75 \times 13.7$ 9.5 X 18.0 26 × 36 {

### WASTE-HEAT ENGINES

that is desired or can be obtained. This must fuel and its mixture with air, and on the degree There does not at the present time appear to that will serve as the basis of a working theory the mean effective pressure even when thes determined.

first question to be determined is the mean ef

It is desirable, in order that the engine shall be compact, that the mean effective pressure shall be engineers commonly make use of 90 to 100 pound pressure; but German engineers who have had very large engines for which presignition is dange content with 60 pounds or less.

Waste-heat Engines. - On page 180 attention

the fact that the exhaust-steam from a steam-eused for vaporizing some fluid like sulphur dithereby the temperature range could be extentests quoted failed to show the advantage that mis when this method is used with steam-engines, from a gas-engine is very hot, probably 1000° I there appears to be no reason why the heat she

as it could readily be used to form steam in a bo

Durnoses.

COMPRESSED air is energy, and for propressure, produced by of iron and steel; and than that of the ablowers) are used to for producing forced

ceptible of but little be reserved for anoth A treatment of the involves the discussi through pipes, and o storage of energy diff

the compressed air,

be given mainly to the production and use

### FLUID PISTON-COMPRESSORS

which receive air at atmospheric pressure, con deliver it against a higher pressure. They are sin pact, but are wasteful of power on account of friction and are used only for moderate pressures.

Fan-blowers consist of a number of radial placed to a horizontal axis and enclosed in a case axis and the vanes attached to it are rotated at a list drawn in through openings near the axis and centrifugal force into the case, from which it delivery-main or duct. Only low pressures, suital tion and forced draught, can be produced in the little has been done in the development of the determination of the practical efficiency of fan-boventilating-fans have their axes parallel to the diair-current, and the vanes have a more or less have that they may force the air by direct pressure effect the converse of a windmill, producing insidirven by the current of air. They are useful rath

Fluid Piston-Compressors. — It will be shown of clearance is to diminish the capacity of the consequently the clearance should be made as small with this in view the valves of compressors are

air than for producing a pressure.

and cover the value fall to the level of quently two vertica horizontal piston, thuid pictons act sha

from partons act sha as in a packet, and irregularities to bre the compressor mass

forming the fluid ; air by continuous at Air pumps used as

may be made with water coming with supplied is insumed

of water from the

Displacement Consufficient head is asarranged exlinders on air, compressing compresses are ser-

befor to more water:

## MOISTURE IN THE CYLINDER

ing water into the cylinder, but experience has work of compression is not much affected by only effective way of reducing the work of couse a compound compressor, and to cool the from the first to the second cylinder. Three-state used for very high pressure... It is, howeair which has been compressed to a high pressure...

density is more readily cooled during compression Moisture in the Cylinder. — If water is not in

cylinder of an air-compressor the moisture in the on the hygroscopic condition of the atmosphere the air were saturated with moisture the absolut tive weight of water in the cylinder would I Thus at 60° F, the pressure of saturated stean fourth of a pound per square inch, and the weig foot is about 0.0008 of a pound, while the weig foot of air is about 0.08 of a pound. It is proponly effect of moisture in the atmosphere is to

When water is sprayed into the cylinder of

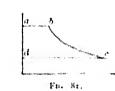
jacket.

the exponent of the equation (77), page 64. sion probably holds when the cylinder is coole

of operations represente the air is compressed,

CAME

dina dina dina



of the compressor whethat the compression of nential curve having the

then the work of comp

$$\int pdv = p_i v_i^{\alpha} \int_{v_i=1}^{v_i} dv$$

The work of expulsion

 $p_{x^{T}x}$ 

### EFFECT OF CLEARANCE

in which the subscripts refer to the normal proper freezing-point and at atmospheric pressure.

If, instead of the specific volume  $v_1$ , we use the vair drawn into the compressor we may readily transfer (189) to give the horse-power directly, obtaining

H. P. = 
$$\frac{144 p_1 V_1 n}{33000(n-1)} \left\{ \left( \frac{p_2}{p_1} \right)^{\frac{n-1}{n}} - 1 \right\}$$

where  $p_1$  is the pressure of the atmosphere in pound inch, and n is the exponent of the equation repression curve, which may vary from 1.4 for pressors to 1.2 for fluid piston-compressors.

Effect of Clearance. — The indicator-diagram compressor with clearance may be represented. The end of the stroke expelling air is at a, and the air remaining in the cylinder expands from a to d, till the pressure becomes equal to the pressure of the atmosphere before the next supply of air is drawn in. The expansion curve ad may commonly be represented by an exponential equation having the next as the compression curve cb, in which case the clearance acts as a supplier which stores and read

364

the pressure  $p_x$ , and, a law expressed by the c

its volume will be

part of the piston displaining the of the diagram v

di di

and this is the factor by without clearance musdisplacement.

Temperature at the I the compressor cylinder brought in with it, it ma

vapor follows the law of

# VOLUME OF THE COMPRESSOR CYLINI

will be discussed under the head of the flow of air it should not be large, unless the air is carried a. The loss of temperature causes a contraction of v ways: first, the volume of the air at a given press as the absolute temperature; second, the moistu (whether brought in by the air or supplied in the excess of that which will saturate the air at the lowes in the conduit, is condensed. Provision must

draining off the condensed water. The method the contraction of volume due to the condensatio

pressor to the place where it is to be used. The lo

will be exhibited later in the calculation of a specia.

Interchange of Heat.—The interchanges of the air in the cylinder of an air-compressor and the cylinder are the converse of those taking place betwand the walls of the cylinder of a steam-engine, less in amount. The walls of the cylinder are ne

the incoming air, nor so warm as the air expelled the air receives heat during admission and the compression, and yields heat during the latter pression and during expulsion. The presence of

Volume of the Compressor Cylinder. — Let

the air increases this effect.

360

If the compressor will be

if the clearance is  $\frac{1}{m}$ 

by the factor (1911) gi

expressed in cubic for The pressure in the

172

in, is always less than the air is expelled it it is delivered. From the compressor will from its dimensions, as as calculated, wheth

creased by an amoun

# COMPOUND COMPRESSOR

The work of compressing one pound of air fr  $p_1$  to the pressure p' is

$$W_1 = p_1 v_1 \frac{n}{n-1} \left\{ \left( \frac{p'}{p_1} \right)^{\frac{n-1}{n}} - 1 \right\}.$$

The work of compressing one pound from the

is 
$$W_2 = p'v'\frac{n}{n-1} \left\{ \left(\frac{p_2}{p'}\right)^{\frac{n-1}{n}} - 1 \right\} = p_1v_1\frac{n}{n-1} \left\{ \left(\frac{p_2}{p'}\right)^{\frac{n-1}{n}} - 1 \right\} = p_2v_1\frac{n}{n-1} \left\{ \left(\frac{p_2}{p'}\right)^{\frac{n-1}{n}} - 1 \right\} = p_$$

because the air after compression in the first cy to the temperature  $t_1$  before it is supplied to the and consequently  $p'v' = p_1v_1$ . The total work of

$$W = W_{1} + W_{2} = p_{1}v_{1}\frac{n}{n-1} \left\{ \left(\frac{p'}{p_{1}}\right)^{\frac{n-1}{n}} + \left(\frac{p_{2}}{p'}\right)^{\frac{n-2}{n}} \right\}$$

and this becomes a minimum when

$$\left(\frac{p'}{p_1}\right)^{\frac{n-1}{n}} + \left(\frac{p_2}{p'}\right)^{\frac{n-1}{n}}$$

becomes a minimum. Differentiating with reequating the first differential coefficient to zero,

$$p' = \sqrt{p, p}$$
 . . .

Three-stage Compress required, as where air is to use a compressor with which the air is passed it way from one cylinder to sures are  $p_1$  and  $p_2$  amintermediate receivers in for most economical confidence.

ing way:
The work of comprecylinders will be

$$W_{x} = p_{x}r_{x_{x_{x}}}$$

$$W_{\tau} = p' v'$$

$$W_{\bullet} = p^{n_1 \cdot n_2}$$

But since the air is so from one cylinder to the

the test wear and a setting

# FRICTION AND IMPERFECTIONS

and  $\frac{\partial R}{\partial p''} = \frac{n-1}{n} \frac{p'' - \frac{1}{n}}{p' - \frac{n-1}{n}} = \frac{n-1}{n} \frac{\frac{n-1}{n}}{p'' - \frac{n}{n}}$ 

Equations (206) and (207) lead to  $p'^2 = p_1 p'' + \dots$ 

Since the temperature is the same at the ad-

$$\frac{p'^2}{p''^2} - \frac{p_1 p''}{p' p_2} \cdot \dots \cdot$$

from which by elimination we have

$$p' = \sqrt[3]{p_1^2 p_2} \quad . \quad . \quad .$$

and

$$p^{\prime\prime} = \sqrt[3]{p_1 p_2^2} \dots \dots$$

of the three cylinders, the volumes of the cylinversely proportional to the absolute pressures. As with the compound compressors, this metha three-stage compressor leads to an equal dist between the cylinders. For, if the values of

equations (210) and (211) are introduced into e (204), taking account also of the equation (100)

$$W_1 = W_2 = W_3 = p_1 v_1 \frac{n}{n+1} \left\{ \left( \frac{p_2}{p_1} \right) \right\}$$

and consequently the total work of compression

370

engines; compressors dr to a like extent by frict

The following table effect of imperfect valvas deduced from tests had a diameter of 18 in-

RATIO OF ACTUAL

Piston speed, feet per minute.

240 280

This table does not nor is the clearance for

# EFFICIENCY OF COMPRESSION

would be

$$W = p_2 v_2 + p_1 v_1 \log_e \frac{v_1}{v_2} - p_1 v_1;$$

but  $p_1v_1 = p_2v_2$  for an isothermal change, and const

$$W = p_1 v_1 \log_e \frac{p_2}{p_1} \dots \dots \dots$$

Some investigators have taken the work of isot pression, represented by equation (214), as a basis o for compressors, and have considered its ratio to the of compression as the efficiency of compression. together into one factor the effect of heating during and the effect of imperfect valve-action.

Professor Riedler \* obtained indicator-diagram cylinders of a number of air-compressors and drew the diagrams which would represent the work of compression, without clearance or valve losses. A of the areas of the isothermal and the actual diagram.

arbitrary efficiency of compression just described. Table gives his results:

There are three not, this table: a there working at the same efficiency tapidly as to or two stage compresson.

Test of a Blowing lead of a blowing engine converters at Crearest engine, with the crare each extinder extended a double acting comp

Diametet, Steatil

Stroke

Diameter of fix a

Industril here p

Ith was s

editained.

pressure, and a separator to gather the air from compression. The water is brought to the compstock, as it would be to a water wheel, and below away in a tailrace; the power available is determined weight of water flowing and the head in the pertailrace, in the usual manner. Below the dam vated to a depth proper to give the required 2.3 feet depth per pound pressure), and then a vated to provide space for the separator. I

plate-iron pipe or cylinder, down which the way passing the separator the water ascends in the

away at the tailrace.

temperature. The essential features are an asp ing the water with air, a column of water to g

The head of the pipe is surrounded by a valuum into which the penstock leads, so that to the head all round the periphery. The hea of two inverted conical iron castings, so formed into which the water flows at first contracts at the changes of velocity being gradual, no at energy ensues. At the throat of the inlet, who highest, there is a partial vacuum, and air is a numerous small pipes so that the water is chart of air. The upper conical casting can be set by the supply of water and air.

As the mingled column of water and air-but

the pipe, the air is compressed at appreciably of the water. At the lower end, the pipe expavelocity, and delivers the air and water into the air gathers in the top of the bell, from v

o.70; making allowance efficiency of the comparison to the configuration to the ordinal

Air-Pumps. The

usually contains air in with the steam to the a like manner the injectorings in air in solution air into the exhaust paper must therefore be provide vacuum. The air promise surface condense injection water from a

densation of the steam and it would be suffice pump, which, with a pump.

The weight of injects

into the combenies the :

by the method on page but it is sudamars to:

#### DRY-AIR PUMP

Seaton\* states that the efficiency of a vert air-pump varies from 0.4 to 0.6, and that of horizontal air-pump from 0.3 to 0.5, depending and condition; that is, the volume of air and discharged will bear such ratios to the dispump.

He also gives the following table of ratios o pump cylinders to the volume of the engine cyldischarging steam into the condenser:

RATIO OF ENGINE AND AIR-PUMP C

Description of Pump.				Description of Engine.			
Single-acting  ""  ""  Double-acting  ""  ""  ""  ""  ""  ""  ""  ""  ""	« « «				Surface- Jet- Surface-	"	expansion  " " compound expansion  " compound

Dry-air Pump. — In the recent development of ing, especially for steam-turbines, great emptobtaining a high vacuum. For this purpose the pump which withdraws air and water from the been replaced by a feed-pump which takes we condenser, and a dry-air pump which removes is necessarily saturated with moisture at the condenser, and allowance must be made for

To illustrate the r use will be made of a Pumping Station also.

The variable on the and the baremeter of that the absolute prodensity water entered at Sc". & P.; had there the temperature on calculation. Making comlensing water on

> 11 ¥. 2

twiffer the entrypter now ture lieute intel eine einen

$$100 \times \frac{450.5 + 85.2}{459.5 + 51.9} \times \frac{14.85}{0.878} = 2980 \text{ c}$$

Assuming the air-pump to be single-acting nected directly to the engine which made abo per minute, the effective displacement of the

should be

To allow for the effect of the air-pump clears of valve-action, and for variation in the tempering water, this quantity may be increased by 50

The engine had 31 feet for the diameter as

stroke of the low pressure piston, so that its of nearly 50 cubic feet; the air pump had a diamonal a stroke of one foot, so that its displacement feet; the ratio of displacements was about sixtee ancy shows that the conventional method of des

provides liberal capacity.

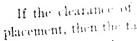
the dimensions of an air compressor to deliver air per minute at 100 pounds per square inch l also the horse power required to drive it.

Calculation for an Air Compressor. Let it le

If it is assumed that the air is forced into at the temperature of the atmosphere, and, for is no loss of pressure between the compressor pipe, equation (193) for finding the volume compressor will be reduced to

$$V_i = V_s \frac{p_s}{p_i}$$
 300 ×  $\frac{114.7}{14.7}$  = 2341 cu

If now we allow five per cent for imperfect



$$1 = \frac{1}{m} \left( \frac{p_1}{p_1} \right)^n$$

if the exponent of the the air in the cleara which the dimensions

24/24

At 80 revolutions will be 2623.5

Assuming a stroke of

1144

Allowing to square is gives a mean area : corresponds very ne piston.

The power expens culated by equation of the compressor, s The calculation has been carried on for a simple but there will be a decided advantage in using a corpressor for such work. Such a compressor should pressure in the intermediate reservoir

$$p' = \sqrt{p_1 p_2} = \sqrt{114.7 \times 14.7} = 41.06$$
 po

The factor for allowing for clearance of the cylinder will now be

$$1 - \frac{1}{m} \left( \frac{p'}{p_1} \right)^{\frac{1}{n}} + \frac{1}{m} = 1 - \frac{2}{100} \left( \frac{41.06}{14.7} \right)^{\frac{1}{14}} + \frac{2}{100} =$$

The loss from imperfect action of the valves an of the air as it enters the compressor will be less for than for a simple compressor, but we will here ret 2464 cubic feet, previously found for the apparent the compressor. The volume from which the dime

compressor will be found will now be

the low-pressure cylinder 31% inches.

$$2464 \div 0.9784 = 2518$$
 cubic feet,

which with 80 revolutions per minute will give 15 for the piston displacement, and 755.5 square in effective piston area, if the stroke is made 3 fee Adding 16 inches for the piston-rod, which will be pass entirely through the cylinder, will give for the

Since the pressure p' is a mean proportional be  $p_2$ , the clearance factor for the high-pressure cylinder, and, a are inversely proportional to the pressures  $p_1$  and pressure piston displacement will be

$$(15.74 \times 14.7) \div 41.06 = 5.64$$
 cubic fe

a simple compressor, la pistons will be less than pressor. Again, the ros small piston may be ro which depend on the c receive much attention a

The power required to from equation \$1000, re the apparent capacity of apparent capacity alreated for the power expended

and, as before, allowing and compressor, we has steam-engine

ě.

The temperature at the will be for you'F, atmost

which last term is obtained by dividing the a by its perimeter. For a cylindrical pipe we ha

$$m = \frac{1}{4}\pi d^2 \div \pi d = \frac{1}{4}d \quad . \quad .$$

The expression (215) represents the head of lie overcome the resistance of friction in the pipe w of flow is u feet per second. Such an expression be applied to flow of air through a pipe when the ciable loss of pressure, for the accompanying inconcessitates an increase of velocity, whereas the extremely as a constant. If, however, we continue through an infinitesimal length of pipe, for when may be treated as constant, we may write for the due to friction

$$\zeta \frac{u^2}{2g} \frac{dl}{m} \dots$$

This loss of head is the vertical distance through must fall to produce the work expended in over and the total work thus expended may be found the loss of head by the weight of air flowing the loss of head with one pound of air, so sion for the loss of head also represents the work.

The air flowing through a long pipe soon apperature of the pipe and thereafter remains at a ature, so that our discussion for the resistance of made under the assumption of constant term much simplifies our work, because the intrinsic remains constant. Again, the work done by t ing a given length dl will be equal to the work when it leaves that section, because the produc

382

But the velocity of air i kinetic energy can be n

The air expands by length dl of pipe, and work must be supplied no other expenditure of head is equal to the

But from the characte

we have

which substituted in equ

If the area of the paper flow through it per sec-

## FRICTION OF AIR IN PIPES

But from equation (221) the velocity at the entrar where the pressure is  $p_1$  will be

$$u_1 = \frac{WRT}{A p_1}$$
 and  $W = \frac{A p_1 u_1}{RT}$ ,

so that equation (223) may be reduced to

$$\zeta \frac{A^{2} p_{1}^{2} u_{1}^{2} L}{g A^{2} m R^{2} T^{2}} = \frac{p_{1}^{2} - p_{2}^{2}}{R T};$$

$$\therefore \zeta \frac{u_{1}^{2} L}{g R T m} = \frac{p_{1}^{2} - p_{2}^{2}}{p_{1}^{2}}.$$

Equation (224) may be solved as follows:

$$u_{1} = \left\{ \frac{gRTm}{\zeta L} \frac{p_{1}^{2} - p_{2}^{2}}{p_{1}^{2}} \right\}^{\frac{1}{2}}.$$

$$p_{2} = p_{1} \left\{ 1 - \frac{\zeta u_{1}^{2} L}{gRTm} \right\}^{\frac{1}{2}}.$$

$$\zeta = \frac{gRTm}{u_1^2L} \frac{p_1^2 - p_2^2}{p_1^2} . . . .$$

The first two forms allow us to calculate eith or the loss of pressure; the last form may be used to the first two forms are the first two forms allowed the first two forms all two forms all two forms all two forms all two forms all two forms all two forms all two forms allowed the first two forms all two forms allowed the first two forms all two forms all two for

values of ζ from experiments on the flow through prom experiments made by Riedler and Gut fessor Unwin† deduces the following values for ζ

Replacing the round pipes, at place of equation

All of the dithe equation it venient units, t

For example, per minute if a initial parameter

The who its

7 JA 1 M

The termin.

$$p_1 = p_1 + 1$$

with per bogrounded a positively.

#### FINAL TEMPERATURE

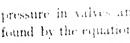
steam was used in it. The full line ab is a hyperbline ac is the adiabatic line for a gas; both lines are drathe intersection of the expansion lines of the two diabatic lines.

Power of Compressed-air Engines. — The profession curve 3 o may be assumed to be adiabatic lines for a gas represented by the equation

$$pv^{\kappa} = p_i v_i^{\kappa},$$

and the area of the diagram may be found in the use therefrom the mean effective pressure can be determ ing the mean effective pressure, the power of a give the size required for a given power may be determined. The method will be illustrated later by an example

Air-Consumption. — The air consumed by a given air engine may be calculated from the volume, present temperature at cut-off or release, and the volume, and pressure at compression, in the same way that the consumption of a steam-engine is calculated; but the indicated and actual consumption should be the there is no change of state of the working fluid intrinsic energy of a gas is a function of the temperature will not be changed by loss of prevalves and passages, and the air at cut-off will be in the supply-pipe, only on account of the chilling a walls of the cylinder during admission, which actio



If the expansion is end of expansion ma

in which  $V_\sigma$  is the vertelease,  $T_\sigma$  is the abound  $T_\sigma$  is the temper in the supply pipe, pressure nor in the opened at release the air will be expelled at ing — much as them the temperature in beginning of compressions.

The temperature in temperature of the a produced by sudden

## MOISTURE IN THE CYLINDER

the walls of the cylinder of a compressed-air engine a working therein are of the same sort as those taking pla the steam and the walls of the cylinder of a steam-end is to say, the walls absorb heat during admission and colif the latter is carried to a considerable degree, and during expansion and exhaust. Since the walls of the are never so warm as the entering air nor so cold

expansion and yield heat during the beginning of com The amount of interchange of heat is much less pressed-air engine than in a steam-engine. With a expansion the interchanges of heat between dry a walls of the cylinder are insignificant. Moisture increases the interchanges in a marked degree, bu make them so large that they need be considered in

exhausted, the walls may absorb heat during the be

calculations.

Moisture in the Cylinder. — The chief disadvant use of moist compressed air — and it is fair to a compressed air is nearly if not quite saturated whe to the engine — is that the low temperature experience the range of pressures is considerable causes the

freeze in the cylinder and clog the exhaust-valves.

to avoid destruction of combustion at all has would be fouled by u

perature of the air of

Compound Air-Engsiderable degree in a realized by dividing to as many exlinders, poreheated between the or of water at the safor this purpose. It struction have been a

would productly contract to find the dimension row indicated horse p

tituse tie all and substance . .

gauge and at 70° I of the piston displac quarter stroke, the rel comparession at one to

If the posted daughan

## CALCULATION FOR A COMPRESSED-AIR EN

automatic valve-gear the actual mean effective probe o.9 of that just calculated, or 38.7 pounds per squ

For a piston displacement D the engine will developed revolutions per minute

$$\frac{144 \times 38.7D \times 2 \times 150}{33000}$$
 horse-power;

and conversely to develop 100 horse-power the pist

$$D = \frac{100 \times 33000}{144 \times 38.7 \times 2 \times 150} = 1.974 \text{ cubic }$$

and with a stroke of 2 feet the effective area of the pi

$$1.974 \times 144 \div 2 = 142.1$$
 square inches

If the piston-rod is 2 inches in diameter it will have 3.14 square inches, so that the mean area of the p 143.7 square inches, corresponding to a diameter of

We find, consequently, that an engine developin power under the given conditions will have a diam

inches and a stroke of 2 feet, provided that it runs lutions per minute.

In order to determine the amount of air used b we must consider that the air caught at compression i of the piston displacement. If the compression occurred sufficiently early to raise the pressure to that in the supply-pip before the admission valve opened, then only 0.25 of the pisto displacement would be used per stroke and a saving of about 1 per cent would be attained; in such case the mean effection pressure would be smaller and the size of the cylinder would barger.

The air consumption for the engine appears to be  $2 \times 150 \times 0.283 \times 1.074 \approx 167$  cubic feet per minute. The actual air consumption will be somewhat less on account of loss of pressure in the valves an passages; it may be fair to assume the cubic feet per minute for the actual consumption.

In order to make one complete calculation for the use of conpressed air for transmitting power, the data for the compressed air engine have been made to correspond with the results of calculations for an air compressor on page 477 and for the loss of pressure in a pipe on page 484. Since there is a loss of pressuin flowing through the pipe at constant temperature, there a corresponding increase of volume, so that the pipe delive

cubic feet per minute. Our calculation for the air-consumption of an engine to deliver 100 horse power gives about 160 cub feet, from which it appears that the system of compressor, conducting-pipe, and compressed air engine should deliver

If the friction of the compressed air engine is assumed to leten per cent, the power delivered by it to the main shaft (or the machine driven directly from it) will be

The steam power required to drive a simple compressor we found to be 5.00 horse-power; it consequently appears that

of the indicated steam-power is actually obtained for doing wo

compound compressor is used, then the indicated steam-power is 444, and of this

$$180 \div 444 = 0.40$$

will be obtained for doing work.

If, however, we consider that the power would in any case be developed in a steam-engine, and that the transmission system should properly include only the compressor-cylinder, the pipe, and the compressed-air engine, then our basis of comparison will be the indicated power of the compressor-cylinder. For the simple compressor we found the horse-power to be 442, which gives for the efficiency of transmission

$$180 \div 442 = 0.41$$
,

while the compound compressor demanded only 377 horsepower, giving an efficiency of

$$180 \div 377 = 0.48.$$

It appeared that the failure to obtain complete compression involved a loss of about 13 per cent in the air-consumption. It may then be assumed that with complete compression our engine could deliver 200 horse-power to the main shaft. In that case the efficiency of transmission when a compound compressor is used may be 0.53.

Efficiency of Compressed-air Transmission. — The preceding calculation exhibits the defect of compressed air as a means of transmitting power. It is possible that somewhat better results may be obtained by a better choice of pressures or proportions. Professor Unwin estimates that when used on a large scale from 0.44 to 0.51 of the indicated steam-power may be realized on the main shaft of the compressed-air engine. On the other hand, when compressed air is used in small motors, and especially in rock-drills and other mining-machinery, much less efficiency may be expected.

Experiments made by M. Graillot\* of the Blanzy mines showed an efficiency of from 22 to 32 per cent. Experiments



<sup>\*</sup> Pernolet, L'Air Comprimé, pp. 549, 550.

made by Mr. Daniel at Leeds gave an efficiency varying from 0.255 to 0.455, with pressures varying from 2.75 atmospheres to 1.33 atmospheres. An experiment made by Mr. Kraft\* gave an efficiency of 0.147 for a small machine, using air at a pressure of five atmospheres without expansion.

Compressed air has been used for transmitting power either where power for compression is cheap and abundant, or where there are reasons why it is specially de liable, as in mining and tunnelling. It is now used to a considerable extent for driving hand tools, such as drills, chipping chisels, and calking-tools, in machine and boiler shops, and in shipyards. It is also used for operating cranes and other machines where power is used only at intervals, so that the condensation of steam (when used directly) is excessive, and where hydraulic power is liable to give trouble from freezing.

Compressed air has been used to a very considerable extension for transmitting power in Paris. The system appears to be expensive and to be used mainly on account of its convenience for delivering small powers or in places where the cold exhaust can be used for refrigeration. The trouble from freezing of moisture in the cylinder has been associed by allowing the air to flow through a coil of pipe which is heated externally by charcoal fire. Professor Unwin estimates that an efficiency of transmission of 0.75 may be attained under favorable conditions when the air is heated near the compressor, but he does no include the cost of fuel for reheating in this estimate.

Storage of Power by Compressed Air. Reservoirs or cylinders charged with compressed air have been used to store power for driving street cars. A system developed by Mekarski uses air at 350 to 450 pounds per square inch in reservoirs having a capacity of 75 cubic feet. The car also carries a tank of howater at a temperature of about 450° F., through which the air passes on the way to the motor and by which it is heated and charged with steam. This use of hot water gives a secondary method of storing power, and also avoids trouble from freezing

<sup>·</sup> Rossan muis avoille ides Alanies, a mirir, tristic si.

used for driving street-cars in New York City, but the particulars have not been given to the public.

The calculation for storage of power may be made in much the same way as that for the transmission of power; the chief difference is due to the fact that the air is reduced in pressure by passing it through a reducing-valve on the way from the reservoir to the motor. By the theory of perfect gases such a reduction of pressure should not cause any change of temperature, but the experiments of Joule and Thomson (page 69) show that there will be an appreciable, though not an important, loss of temperature when there is a large reduction of pressure. Thus at 70° F. or 21°.1 C. the loss of temperature for each 100 inches of mercury will be

$$0^{\circ}.92 \times \left(\frac{27.3}{20.4}\right)^2 = 0^{\circ}.79 \text{ C.} = 13^{\circ} \text{ F.}$$

Now 100 inches of mercury are equivalent to about 49 pounds to the square inch, so that 100 pounds difference of pressure will give about  $3\frac{1}{2}$ ° F. reduction of temperature, and 1000 pounds difference of pressure will give about 35° F. reduction of temperature. The last figures are far beyond the limits of the experiments, and the results are therefore crude. Again, the air in passing through the reducing-valve and the piping beyond will gain heat and consequently show a smaller reduction of temperature. The whole subject of loss of temperature due to throttling is uncertain, and need not be considered in practical calculations for air-compressors.

For an example of the calculation for storage of power let us find the work required to store air at 450 pounds per square inch in a reservoir containing 75 cubic feet. Replacing the specific volume  $v_1$  in equation (213) by the actual volume, we have for the work of compression (not allowing for losses and imperfections)

$$W = 3 \times 464.7 \times 144 \times 75 \frac{1.4}{1.4 - 1} \left\{ \left( \frac{464.7}{14.7} \right)^{\frac{1.4 - 1}{3 \times 1.4}} - 1 \right\}$$
  
= 20520000 foot-pounds.

If the pressure is reduced to 50 pounds by the gauge before it used, the volume of air will be

The work for complete expansion of one pound to the pressur of the atmosphere will be

$$W = p_3 v_3 + \frac{p_3 v_4}{\kappa} \left\{ 1 - \left(\frac{v_3}{v_4}\right)^{\frac{1}{2}} \right\} = p_3 v_4$$
$$= p_3 v_3 \frac{\kappa}{\kappa} \left\{ 1 - \left(\frac{p_4}{p_3}\right)^{\frac{1}{2}} \right\}$$

and the work for \$30 cubic feet will be

$$144 \times 64.7 \times 530 \xrightarrow{1.4} \left\{1 - \left(\frac{14.7}{64.7}\right)^{\frac{1}{14}}\right\} = 5976000$$

foot-pounds, without allowing for bases or imperfections. The maximum efficiency of storing and restoring energy by the use of compressed air in this case is therefore.

In practice the efficiency cannot be more than 0.25, if indee it is so high.

Sudden Compression. It may not be out of place to call after tion to a danger that may arise if air at high pressure is suddenlet into a pipe which has oil mingled with the air in it or eve adhering to the side of the pipe. The air in the pipe will be compressed, and its temperature may become high enough to ignite the oil and cause an explosion. That this danger is not imaginary is shown by an explosion which occurred under such conditions it a pipe which was strong enough to withstand the air-pressure.

Liquid Air. The most practical way of liquefying air on large scale is that devised by Linde depending on the reduction of the temperature by throttling. On page 60, is given the empirical expression deduced by Joule and Kelvin for the reduction in temperature of air flowing through a porous plu with a difference of pressure measured by 100 inches of mercury

freezing, and T is the absolute temperature of the air.

A modern three-stage air-compressor can readily give a pressure of 2000 pounds per square inch, and if the above expression is assumed to hold approximately for such a reduction in pressure, it indicates a cooling of

$$0.92 \times \frac{2000}{100 \times 0.491} = 37^{\circ}.5$$
 C.

or about 67° F. By a cumulative effect to be described, the air may be cooled progressively till it reaches the boiling-point of its liquid and then liquefied. Linde's liquefying apparatus consists essentially of an air-compressor, a throttling-orifice, and a heat interchange apparatus.

The air-compressor should be a good three-stage machine The throttling-orifice may be a small giving a high pressure. hole in a metallic plate. The heat interchange apparatus may be made up of a double tube about 400 feet long, the inner tube having a diameter of 0.16 and the outer tube a diameter of 0.4 of an inch; these tubes for convenience are coiled and are then thoroughly insulated from heat. The air from the compressor is passed through the inner tube to the throttle-orifice and then from the reservoir below the orifice, through the space between the inner and outer tubes back to the compressor. The cumulative effect of this action brings the air to the critical temperature in a comparatively short period, and then liquid air begins to accumulate in the reservoir below the orifice, whence it may be drawn off.

The atmospheric air before it is supplied to the condenser should be freed from carbon dioxide and moisture, which would interfere with the action, and should be cooled by passing it through pipes cooled with water and by a freezing mixture. The portion of air liquefied must be made up by drawing air from the atmosphere, which is, of course, purified and cooled.

The principal use of liquid air is the commercial production of oxygen by fractional distillation; several plants have been installed for this purpose.

## CHAPTER XVI.

### REPRIGERATING MACHINES.

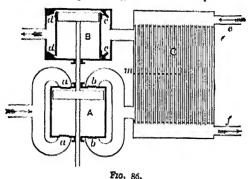
A REPRIGERATING MACHINE is a device for producing le temperatures or for cooling some substance or space. It m be used for making ice or for maintaining a low temperature a cellar or storchouse.

Refrigeration on a small scale may be obtained by the so tion of certain salts; a familiar illustration is the solution common salt with ice, another is the solution of sal ammon in water. Certain refrigerating machines depend on the rap absorption of some volatile liquid, for example, of ammonia water; if the machine is to work continuously there must be so arrangement for redistilling the liquid from the absorbent. T most recent and powerful refrigerating machines are revers heat engines. They withdraw the working substance (air ammonia) from the cold room or cooling coil, compress it, a deliver it to a cooler or condenser. Thus they take heat from cold substance, do work and add heat, and finally reject the st of the heat drawn in and the heat equivalent of the work do These reversed heat engines, however, are very far from bel reversible engines, not only on account of imperfections and los but because they work on a non reversible eyele.

Two forms of refrigerating machines are in common use, refrigerating machines and ammonia refrigerating-machin Sometimes sulphur dioxide or some other volatile fluid is us instead of ammonia. Carbon dioxide has been used, but there is difficulties due to high pressure and the fact that the critical te perature is 88° F.

Air Refrigerating-Machine. The general arrangement an air refrigerating machine is shown by Fig. 86. It consi

of a confinession-cylinder A, an expansion-cylinder B of smaller size, and a cooler C. It is commonly used to keep the atmosphere in a cold-storage room at a low temperature, and has certain advantages for this purpose, especially on shipboard. The air from the storage-room comes to the compressor at or about freezing-point, is compressed to two or three atmospheres and delivered to the cooler, which has the same form as a surface-condenser, with cooling water entering at c and leaving at f. The diaphragm mn is intended to improve the circulation of the cooling water. From the cooler the air, usually somewhat warmer than the atmosphere, goes to the expansion-cylinder B,



in which it is expanded nearly to the pressure of the air and cooled to a low temperature, and then delivered to the storageroom. The inlet-valves a, a and the delivery-valves b, b of the compressor are moved by the air itself; the admission-valves c, c and the exhaust-valves d, d of the expansion-cylinder are like those of a steam-engine and must be moved by the machine. The difference between the work done on the air in the compressor and that done by the air in the expansion-cylinder, together with the friction work of the whole machine, must be supplied by a steam-engine or other motor.

It is customary to provide the compression-cylinder with a water-jacket to prevent overheating, and frequently a spray of water is thrown into the cylinder to reduce the heating and the work of compression. Sometimes the cooler C, Fig. 86,

is replaced by an apparatus resembling a steam engine jet-condenser, in which the air is cooled by a spray of water. In any case it is essential that the moisture in the air, as well as the water injected, should be efficiently removed before the air is delivered to the expansion cylinder; otherwise snow will form in that cylinder and interfere with the action of the machine. Various mechanical devices have been used to collect and remove water from the air, but air may be saturated with moisture after it has passed such a device. The Bell Coleman Company use a jet cooler with provision for collecting and withdrawing water and then pass the air through pipes in the cold room on the way to the expansion cylinder. The cold room is maintained at a temperature a little above freezing point, so that the mois ture in the air is condensed upon the sides of the pipes and drains back into the cooler.

When an air refrigerating machine is used as described, the pressure in the cold room is necessarily that of the atmosphere and the size of the machine is large as compared with its per formance. The performance may be increased by running the machine on a closed eyele with higher pressures; for example the cold air may be delivered to a coil of pipe in a non-freezing salt solution, from which the air abstracts heat through th walls of the pipe and then passes to the compressor to be use over again. The machine may then be used to produce ice, o the brine may be used for cooling spaces or liquids. A machin has been used for producing is con a small scale, without cooling water, on the reverse of this principle; that is, atmospheric al is first expanded and chilled and delivered to a coil of pipe is a salt solution, then the air is drawn from this coil, after absorb ing heat from the brine, compressed to atmospheric pressure and expelled.

Proportions of Air Refrigerating-Machines.—The performance of a refrigerating machine may be stated in term of the number of thermal units withdrawn in a unit of time or in terms of the weight of ice produced. The latent heat of fusion of ice may be taken to be 80 calories or 144 B.T.U.

cylinder be  $p_1$ , that at which it leaves be  $p_2$ ; let the pressure at cut-off in the expanding-cylinder be  $p_3$  and that of the backpressure in the same be  $p_4$ ; let the temperatures corresponding to these pressures be  $t_1$ ,  $t_2$ ,  $t_3$ , and  $t_4$ , or, reckoned from the absolute zero,  $T_1$ ,  $T_2$ ,  $T_3$ , and  $T_4$ . With proper valve-gear and large, short pipes communicating with the cold-chamber  $p_4$  may be assumed to be equal to  $p_1$  and equal to the pressure in that chamber. Also  $t_1$  may be assumed to be the temperature maintained in the cold-chamber, and  $t_3$  may be taken to be the temperature of the air leaving the cooler. With a good cut-off mechanism and large passages  $p_3$  may be assumed to be nearly the same as that of the air supplied to the expanding-cylinder. Owing to the resistance to the passage of the air through the cooler and the connecting pipes and passages,  $p_3$  is considerably less than  $p_2$ .

It is essential for best action of the machine that the expansion and compression of the expanding-cylinder shall be complete. The compression may be made complete by setting the exhaust-valve so that the compression shall raise the pressure in the clearance-space to the admission-pressure  $p_3$  at the instant when the admission-valve opens. The expansion can be made complete only by giving correct proportions to the expanding-and compression-cylinders.

The expansion in the expanding-cylinder may be assumed to be adiabatic, so that

$$\frac{T_4}{T_8} = \left(\frac{p_4}{p_8}\right)^{\frac{\kappa - 1}{\kappa}} \dots \dots \dots (231)$$

Were the compression also adiabatic the temperature  $t_2$  could



Fig. 87.

be determined in a similar manner; but the air is usually cooled during compression, and contains more or less vapor, so that the temperature at the end of compression cannot be determined from the pressure alone, even

though the equation of the compression curve be known.

Let the air passing through the refrigerating-machine pminute be  $M_i$  then the heat withdrawn from the cold-room

$$Q_1 = M_{k_B} : l_1 = l_2 \cdot \ldots \cdot (23)$$

The work of compressing M pounds of air from the pressure to the pressure  $\rho$ , in a compressor without clearance is (Fig. 8)

$$W_{s} = M \left\{ p_{s}v_{s} + \int_{v_{s}}^{v_{s}} \rho dv - p_{s}v_{s} \right\},$$

$$W_{s} = M \left\{ p_{s}v_{s} + \frac{p_{s}v_{s}}{n} \right\} \left( \begin{pmatrix} v_{s} \\ v_{s} \end{pmatrix}^{n} - v_{s} \right\} - p_{s}v_{s} \right\},$$

$$W_{s} = M \left\{ p_{s}v_{s} + \left( \frac{p_{s}}{p_{s}} \right)^{n} - \frac{p_{s}v_{s}}{n} \right\} \left( \begin{pmatrix} v_{s} \\ p_{s} \end{pmatrix}^{n} - v_{s} \right\} - p_{s}v_{s} \right\},$$

$$W_{s} = M \left\{ p_{s}v_{s} + \left( \frac{p_{s}}{p_{s}} \right)^{n} - \frac{p_{s}v_{s}}{n} \right\} \left( \begin{pmatrix} v_{s} \\ p_{s} \end{pmatrix}^{n} - v_{s} \right) \right\}$$

$$W_{n} = Mp_{n}v_{n} = \binom{n}{n} \left( \binom{p_{n}}{p_{n}} \right)^{-n} = \left( \cdots \cdots (2, \frac{p_{n}}{p_{n}}) \right)^{-n}$$

provided that the compression curve can be represented by exponential equation. If the compression can be assumed be adiabatic,

$$W_r = M\rho_1 v_1 \xrightarrow{K} \left\{ \begin{pmatrix} \rho_1 \\ \rho_2 \end{pmatrix} \right\} = \left\{ -\frac{M \iota_R}{4} (t_1 - t_1); \quad (2) \right\}$$

for in such case we have the equations

$$\frac{T_{\lambda}}{T_{\lambda}} = \begin{pmatrix} \rho_{\lambda} \\ \rho_{\lambda} \end{pmatrix} \qquad AR = \epsilon_{\rho} \quad \epsilon_{\rho} = \epsilon_{\rho} \quad \frac{R}{\kappa} = 1.$$

If the expansion is complete in the expanding cylinder, should always be the case, then the equation for the work d by the air will have the same form as equation (233) or (2) replacing t, and p los t, and p, and t, and p, by t, and p; so the

$$W_{*} = M p_{*} t_{*} \underbrace{\begin{array}{c} p_{*} \\ p_{*} \end{array}}_{n} \left\{ \begin{pmatrix} f_{*} \\ p_{*} \end{pmatrix}^{n} - 1 \right\} . . . (2)$$

and for adiabatic expansion

$$W_s = \frac{M_{\rm in}}{A} u_s u_s u_s$$

Ine difference between the works of compression and expansion is the net work required for producing refrigeration; consequently

$$W = W_o - W_e = \frac{Mc_p}{A} \{t_2 - t_1 - t_3 + t_4\} \quad . \quad (237)$$

or, replacing M by its value from equation (232),

$$W = \frac{Q_1}{A} \frac{t_2 + t_4 - t_1 - t_8}{t_1 - t_4} \qquad (238)$$

The net horse-power required to abstract  $Q_t$  thermal units per minute is consequently

$$P_n = \frac{778Q_1}{33000} \frac{t_2 + t_4 - t_1 - t_3}{t_1 - t_4} \quad . \quad . \quad . \quad (239)$$

where  $t_1$  is the temperature of the air drawn into the compressor, and  $t_2$  is the temperature of the air forced by the compressor into the cooler, and  $t_3$  is the temperature of the air supplied to the expanding-cylinder, and  $t_4$  is the temperature of the cold air leaving the expanding-cylinder. The gross horse-power developed in the steam-engine which drives the refrigerating-machine is likely to be half again as much as the net horse-power or even larger. The relation of the gross and the net horse-powers for any air refrigerating-machine may readily be obtained by indicating the steam- and air-cylinders, and may serve as a basis for calculating other machines.

The heat carried away by the cooling water is

$$Q_2 = Q_1 + AW.$$
 . . . . (240)

If compression and expansion are adiabatic, then

$$Q_{2} = Mc_{p} (t_{1} - t_{4} + t_{2} + t_{4} - t_{1} - t_{3}) = Mc_{p} (t_{2} - t_{3}) . (241)$$

or, replacing M by its value from equation (232),

$$Q_2 = Q_1 \frac{t_2 - t_3}{t_1 - t_4} \quad . \quad . \quad . \quad (242)$$

If the initial and final temperatures of the cooling water are

 $t_i$  and  $t_k$ , and if  $q_i$  and  $q_k$  are the corresponding heats of the liquid, then the weight of cooling water per minute is

$$G = \frac{Q_2}{q_k - q_i} = Q_1 \frac{t_2 - q_i}{(t_1 - t_4)(q_k - q_i)} \cdot \cdot \cdot (243)$$

The compressor-cylinder must draw in M pounds of air perminute at the pressure  $p_1$  and the temperature  $t_1$ , that is, with the specific volume  $v_1$ ; consequently its apparent piston displacement without clearance will be at N revolutions per minute,

$$D_{c} = \frac{Mv_{1}}{2N} = \frac{MRT_{1}}{2Np_{1}} \quad . \quad . \quad . \quad (244)$$

for the characteristic equation gives

$$p_1v_1 = RT_1$$

Replacing M by its value from equation (232), we have

$$D_{e} = \frac{Q_{1}RT_{1}}{2Nc_{p}p_{1}(t_{1}-t_{4})} \quad . \quad . \quad . \quad (245)$$

Since all the air delivered by the compressor must pass through the expanding-cylinder, its apparent piston displacement will be

If  $p_1$ , the pressure of the air entering the compression-cylinder is equal to  $p_4$ , that of the air leaving the expanding-cylinder (as may be nearly true with large and direct pipes for carrying the air to and from the cold-room), equation (246), will reduce to

$$D_e = D_c \frac{T_4}{T_1} \quad . \quad . \quad . \quad . \quad (247)$$

Both the compressor- and the expanding-cylinder will have a clearance, that of the expanding-cylinder being the larger. As is shown on page 363, the piston displacement for an air-compressor with a clearance may be obtained by dividing the apparent piston displacement by the factor

$$1 - \frac{1}{m} \left( \frac{p_2}{p_1} \right)^{\frac{1}{n}} + \frac{1}{m}.$$

complete, the same factor may be applied to it. For a refrigerating-machine n may be replaced by  $\kappa$  for both cylinders. To allow for losses of pressure and for imperfect valve action the piston displacements for both compressor- and expanding-cylinders must be increased by an amount which must be determined by practice; five or ten per cent increase in volume will probably suffice. In practice the expansion in the expanding-cylinder is seldom complete. A little deficiency at this part of the diagram will not have a large effect on the capacity of the machine, and will prevent the formation of a loop in the indicator-diagram; but a large drop at the release of the expanding-cylinder will diminish both the capacity and the efficiency of the machine.

The temperature  $t_4$  and the capacity of the machine may be controlled by varying the cut-off of the expanding-cylinder. If the cut-off is shortened the pressure  $p_2$  will be increased, and consequently  $T_4$  will be diminished. This will make  $D_e$ , the piston displacement of the expanding-cylinder, smaller. A machine should be designed with the proper proportions for its full capacity, and then, when running at reduced capacity, the expansion in the expanding-cylinder will not be quite complete.

Calculation for an Air-refrigerating Machine. — Required the dimensions and power for an air refrigerating-machine to produce an effect equal to the melting of 200 pounds of ice per hour. Let the pressure in the cold-chamber be 14.7 pounds per square inch and the temperature 32° F. Let the pressure of the air delivered by the compressor-cylinder be 39.4 pounds by the gauge or 54.1 pounds absolute, and let there be ten pounds loss of pressure due to the resistance of the cooler and pipes and passages between the compressor- and the expanding-cylinder. Let the initial and final temperatures of the cooling water be 60° F. and 80° F., and let the temperature of the air coming from the cooler be 90° F. Let the machine make 60 revolutions per minute.

With adiabatic expansion and compression the temperatures

of the air coming from the compressor, and discharged from the expanding cylinder, will be

$$T_{4} = 402 \left(\frac{34.1}{14.7}\right)^{14} = 714; \qquad \therefore I_{2} = 254^{\circ}]$$

$$T_{4} = (400 + 40) \left(\frac{14.7}{14.1}\right)^{14} = 402; \qquad \therefore I_{4} = -58^{\circ}]$$

The melting of see pounds of ice is equivalent to

per minute; consequently the net horse power of the machinis by equation (2,30)

and the indicated power of the steam engine may be assume to be 14 horse power.

By equation (245) the apparent piston displacement of the compressor without clearance will be

By equation (247) the apparent piston displacement of the expanding cylinder without clearance will be

$$D_s = D_s \frac{T_L}{T_c} = s_{AA} + \frac{402}{402} = r_{AB}$$
 cubic feet.

If the clearance of the compressor cylinder is 0.02 of its pisto displacement, then the factor for clearance by equation (191)

$$1 = \frac{1}{m} \left( \frac{L}{p_1} \right)^n + \frac{1}{m} = 1 = \frac{2}{100} \left( \frac{54.1}{14.7} \right)^{\frac{1}{14}} = 0.079,$$

$$2.33 \div 0.979 = 2.38$$
 cubic feet.

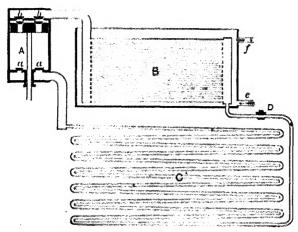
If, further, the clearance of the expander-cylinder is 0.05 of its piston displacement, the factor for clearance becomes

$$1 - \frac{5}{100} \left( \frac{44.1}{14.7} \right)^{\frac{1}{1.4}} + \frac{5}{100} = 0.963,$$

which makes the piston displacement

If now we allow ten per cent for imperfections, we will get for the dimensions: stroke 2 feet, diameter of the compressor-cylinder  $15\frac{1}{2}$  inches, and diameter of the expanding-cylinder 14 inches.

Compression Refrigerating-Machine. — The arrangement of a refrigerating-machine using a volatile liquid and its vapor is



Fro. 88.

shown by Fig. 88. The essential parts are the compressor A, the condenser B, the valve D, and the vaporizer C. The compressor draws in vapor at a low pressure and temperature, compresses it, and delivers it to the condenser, which consists of coils of pipe surrounded by cooling water that enters at e and leaves at f. The vapor is condensed, and the resulting liquid

gathers in a reservoir in the bottom, from whence it is led small pipe having a regulating valve D to the vaporize refrigerator. The refrigerator is also made up of coils of in which the volatile liquid vaporizes. The coils may be directly for cooling spaces, or they may be immersed in a of brine, which may be used for cooling spaces or for makin Fig. 88 shows the compressor with one single acting verylinder which has head valves, foot valves, and valves i piston. Small machines usually have one double acting pressor cylinder. Large machines have vertical compressor cylinder. Large machines have vertical compression may be single acting or double acting.

The cycle which has been stated for the comprerefrigerating machine is incomplete, because the working is allowed to flow through the expansion cock into the expancions without doing work. To make the cycle complete, should be a small expanding cylinder in which the liquid do work on the wax from the condenser to the vaporizing but the work gained in such a cylinder would be insignificant it would lead to complications and difficulties.

Proportions of Compression Refrigerating-Machines.—liquid condensed in the coils of the condenser flows to the e-sion cock with the temperature  $I_i$  and has in it the heat  $q_i$  passing through the expansion cock there is a partial vaption, but no heat is gained or lost. The vapor flowing froexpansion coils at the temperature  $I_i$  and the pressure usually dry and saturated, or perhaps slightly superheated approaches the compressor. Each pound consequently of from the expanding coils the total heat  $H_{ij}$ . Consequently heat withdrawn from the expanding coil by a machine M pounds of fluid per minute is

$$Q_i = M \circ H_i \circ q_i \circ \ldots \circ \ldots$$

The compressor cylinder is always conded by a water-j but it is not probable that such a jacket has much effect of working substance, which enters the cylinder dry and is heated by compression. We may consequently calculate equation (80), page 65, giving

$$T_s = T_2 \left(\frac{p_1}{p_2}\right)^{\frac{k-1}{k}} = T_2 \left(\frac{p_1}{p_2}\right)^a \quad . \quad . \quad (249)$$

This equation may be used because it is equivalent to the assumption with regard to entropy on page 121. The value of a is  $\frac{1}{4}$  for ammonia and 0.22 for sulphur dioxide as given on pages 119 and 124.

As has already been pointed out, the vapor approaching the compressor may be treated as though it were dry and saturated, each pound having the total heat  $H_2$ . The vapor discharged by the compressor at the temperature  $t_i$  and the pressure  $p_1$  will have the heat

$$c_p (t_s - t_1) + H_1$$

The heat added to each pound of fluid by the compressor is consequently

$$c_p (t_s - t_1) + H_1 - H_2,$$

and an approximate calculation of the horse-power of the compressor may be made by the equation

$$P_{\sigma} = \frac{778M \left\{ c_{p} \left( t_{s} - t_{1} \right) + H_{1} - H_{2} \right\}}{33000} \quad . \quad . \quad (250)$$

or, substituting for M from equation (249),

$$P_{c} = \frac{778Q_{1} \left\{ c_{p} \left( t_{s} - t_{1} \right) + H_{1} - H_{2} \right\}}{33000 \left( H_{2} - q_{1} \right)} \quad . \quad (251)$$

The power thus calculated must be multiplied by a factor to be found by experiment in order to find the actual power of the compressor. Allowance must be made for friction to find the indicated power of the steam-engine which drives the motor; for this purpose it will be sufficient to add ten or fifteen per cent of the power of the compressor.

The heat in the fluid discharged by compressor is equal to the sum of the heat brought from the vaporizing-coils and the heat-equivalent of the work of the compressor. The heat that must be carried away by the cooling water per minute is co sequently

$$Q_{2} = M (H_{2} - q_{1}) + M\{c_{p} (t_{s} - t_{1}) + H_{1} - H_{2}\};$$

$$\therefore Q_{2} = M\{c_{p} (t_{s} - t_{1}) + r_{1}\} . . . . . . . . . . . (25)$$

where  $r_1$  is the heat of vaporization at the pressure  $p_1$ .

If the cooling water has the initial temperature  $t_w$  and the fine temperature  $t_w$ , and if  $q_w$  and  $q_w'$  are the corresponding heats the liquid for water, then the weight of cooling water used purposes will be

$$G = \frac{M \left[ c_p(t_s - t_1) + v_1 \right]}{q_m - q'_m} . . . . . . (2)$$

If the vapor at the beginning of compression can be assum to be dry and saturated, then the volume of the piston displacement of a compressor without clearance, and making N strok per minute, is

$$D = \frac{Mv_2}{N} \quad . \quad . \quad . \quad . \quad . \quad (25)$$

To allow for clearance, the volume thus found may be divid by the factor

$$I - \frac{I}{m} \left( \frac{p_1}{p_2} \right)^n + \frac{I}{m},$$

as is explained on page 363. The volume thus found is furth to be multiplied by a factor to allow for inaccuracies a imperfections.

The vapors used in compression-machines are liable to mingled with air or moisture, and in such case the performant of the machine is impaired. To allow for such action the sand power of the machine must be increased in practice about those given by calculation. Proper precautions ought to taken to prevent such action from becoming of importance.

Calculation for a Compression Refrigerating-Machine. — I it be required to find the dimensions and power for an ammor refrigerating-machine to produce 2000 pounds of ice per he from water at 80° F. Let the temperature of the brine in

acting compressor, and that it will make 80 revolutions per minute.

The heat of the liquid for water at 80° F. is 48 B.T.U., and the heat of liquefaction of ice is 144, so that the heat which must be withdrawn to cool and freeze one pound of water will be

$$48 + 144 = 192 \text{ B.T.U.}$$

If we allow 50 per cent loss for radiation, conduction, and melting the ice from the freezing-cans, the heat which the machine must withdraw for each pound of ice will be about 300 B.T.U.; consequently the capacity of the machine will be

$$Q_1 = 2000 \times 300 \div 60 = 10000$$
 B.T.U. per minute.

The pressures for ammonia corresponding to 15° and 85° F., are 42.43 and 165.47 pounds absolute per square inch, so that by equation (249)

$$T_s = T_2 \left(\frac{p_1}{p_2}\right)^a = (15 + 460) \left(\frac{165.47}{42.43}\right)^{\frac{1}{4}} = 668.$$
  

$$\therefore t_s = 668 - 460 = 208^{\circ} \text{ F.}$$

The horse-power of the compressor is

$$\begin{split} P_c &= \frac{778Q_1 \left\{ c_p \left( t_s - t_1 \right) + H_1 - H_2 \right\}}{33000 \left( H_2 - q_1 \right)} \\ &= \frac{778 \times 10000 \left\{ 0.50836 \left( 208 - 85 \right) + 556 - 535 \right\}}{33000 \left( 535 - 58 \right)} = 41. \end{split}$$

If we allow 10 per cent for imperfections, the compressor will require 45 horse-power. If, further, 15 per cent is allowed for friction, the steam-engine must develop 53 horse-power.

From equation (248) the weight of ammonia used per minute

 $M = Q_1 \div (H_2 - Q_1) = 10000 \div (535 - 58) = 21$  pounds; and by equation (254) the piston displacement for the compressor will be

$$D = \frac{Mv_2}{N} = \frac{21 \times 6.93}{2 \times 80} = \text{ o.gr cubic feet.}$$

If 10 per cent is allowed for clearance and imperfect vaaction, the piston displacement will be one cubic foot, and diameter may be made 103 inches and the stroke 20 inches.

Fluids Available. The fluids that have been used in comprision refrigerating machines are other, sulphur dioxide, amounted a mixture of sulphur dioxide and carbon dioxide, known Pictet's fluid. The pressures of the vapors of these fluids at seral temperatures, and also the pressure of the vapors of methy other and carbon dioxide, are given in the following table:

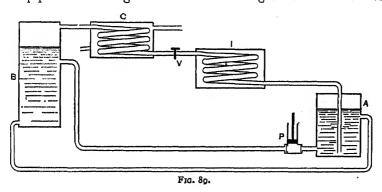
PRESSURES OF VAPORS, MM OF MURCURY,

Picti Flu	Carloca Inication	* 3	1 coursesses	Markey) Reduce		Walgoli Lengai	f 	: 4	Binter	ida arge Euch p ea ag maca	1 hoy
ACCOUNT NO.	· ************************************									i	
S		8	49.40	8371 4	3 4	#113	1			10	~6.4
7	13142	2	1 1 2 3	<b>海海</b> 3	4 4	春音诗		43	Kuta	10	:7/1
10	20140	34	: : : :	\$ \$ 100 \$	2 5	2800		4	8 8 5	10	4.70
13	stayay	\$	3494	8 4 7 14 14	<b>4</b> 8	8 B#c 4		4	自然者	158	
19	1.44993	15	4574	28.39 B	9 6	3 3 4 3		99	3 Min	\$ x 9	
25	44717	4	1.343	当年後 い	\$ B	३ कुर्रें। इ	ř	16	412	200	
33	364 119	t) <sup>‡</sup>	48.04	4334 0	出 待	黄黄重岩	;	36	F2 & #	(d)	
43	Caps 64	2	225734		13 3	4 Tz 2 15		-(3)	8904	4/4	

Ether was used in the early compression machines, but at temperatures maintained in the refrigerator the pressure small and the specific volume large, so that the machines, I air refrigerating machines, were either feeble or bulky. Mo over, air was liable to leak into the machine and unduly heat compressor cylinder. Sulphur dioxide has been used succe fully, but it has the disadvantage that sulphuric acid may formed by the leakage of moisture into the machine, in whe case rapid corrosion occurs. Ammonia has been extensive used in the more recent machines with good results. We distilled from an aqueous solution it is liable to contain easiderable moisture. As is shown by the table, Pictet's fluid a pressure at low temperature intermediate between the pressure sulphur dioxide and ammonia, and the pressure increases of sulphur dioxide and ammonia, and the pressure increases of sulphur dioxide and ammonia.

ammonia.

Absorption Refrigerating Apparatus. - Fig. 89 gives an ideal diagram of a continuous absorption refrigerating apparatus. It consists of the following essential parts: (1) the generator B, containing a concentrated solution of ammonia in water, from which the ammonia is driven by heat; (2) the condenser C, consisting of a coil of pipe in a tank, through which cold water is circulated; (3) the valve V, for regulating the pressures in C and in I; (4) the refrigerator I, consisting of a coil of pipe in a tank containing a non-freezing salt solution; (5) the absorber A, containing a dilute solution of ammonia, in which the vapor of ammonia is absorbed; and (6) the pump P for transferring the solution from the bottom of A to the top of B; there is also a pipe connecting the bottom of B with the top of A. It is apparent that the condenser and refrigerator or vaporizer correspond to the parts B and C of Fig. 88, and that the absorber and generator take the place of the compressor. The pipes connecting A and B are arranged to take the most



concentrated solution from A to B, and to return the solution from which the ammonia has been driven, from B to A. In practice the generator B is placed over a furnace, or is heated by a coil of steam-pipe, to drive off the ammonia. Also, arrangements are made for transferring heat from the hot liquid flowing from B to A to the cold liquid flowing from A to B. As



the ammonia is distilled from water in B the vapor driven contains some moisture, which causes an unavoidable loss efficiency.

Tests of an Air Refrigerating-Machine. An air refrigating machine, constructed under the Bell Coleman pate was tested by Professor Schröter at an abattoir in Hambu where it was used to maintain a low temperature in a stora room. The machine is horizontal, and has the pistons for expansion and compression cylinders on one piston-rod, expansion cylinder being nearer the crank. Power is furnishly a steam engine asting on a crank at the other end of main shaft and at right angles to the crank driving the pistons. Both the steam cylinder and the expansion-cylinhave distribution slide valves, with undependent cut-off valves main dimensions are given in the following table:

## HIMENSHANS HELL COLLEGES MACHINE.

10 m	**** *********************************	CB 12 On iBer	t and a		f tpas Criss	dre.
	\$\$2.2.\$ \$-2.5	Formal Formal	Mes 1	d sample 1	Head Find	CE
			1			Year To
Principality of pointing the	12	* *	24	7.0	51	j .
Efficiency of the grant with the second	3 a	40 9	அ. வ.	花桶	49 4	50
"HITTER CO. THE	A 134 4 9	ca face y	ie like \$	of Tour &	a figg	- 4
र मा आराज कर के दिवस है कि से से से से से कार्य कर है कि से से साम कर है कि से मार्थ कर कर है कि से मार्थ के म	2 10	ý \$	4 - 4		4 4	-

Water is sprayed into the compression cylinder, and the is further cooled by passing through an apparatus resemble a steam engine jet condenser, after which it is dried by pass it through a system of paper in the cold room before it pasto the expansion exhibiter.

In the tests, indicators were attached to each end of the sew cylinders, and the temperature of the air was taken at entrato and exit from each of the air cylinders. Specimens of indicator diagrams from the air cylinders show for the copressor a slight reduction of pressure during admission a some irregularity during expulsion, and for the expansi-

<sup># 1&</sup>quot;marrow. Aumgen am A allows. Asmon, 1987;

and compression, though neither is complete. No attempt was made to measure the amount and temperatures of the cooling water.

The data and results of the tests and the calculations are given in Table XXXVI.

TABLE XXXVI.
TESTS ON BELL-COLEMAN MACHINE.

Number of test	. l п.	III.
	5 1.63	2.02
Revolutions per minute		63.5
Temperatures of air, degrees Centigrade:	35 01.2	03.3
At entrance to compression-cylinder	3 17.5	10.1
At exit from compression-cylinder		27.2
At entrance to expansion-cylinder		10.1
At exit from expansion-cylinder		-47.0
Mean effective pressure, kgs. per sq. cm.:	-   ***-	1,
	263 2.336	2.343
	239 2.294	2.301
Compression-cylinder: head end	000 1.861	1.870
	869 1.825	1.906
Expansion-cylinder: head end	592 1.589	1.626
crank end	615 1.594	1,624
Indicated horse-power:		
Steam-cylinder		85.71
Compression-cylinder		126.01
Expansion cylinder		59.46
Mean pressure during expulsion from compression-cylinder, kgs 3.	35 3.25	3.40
	82 2.83	2.84
	53 0.42	0.56
Calculation from compression diagram :	1	1
	04 1.04	1.04
Absolute pressure at opening of admission-valve, kg.:		
	783 0.788	0.764
Crank end	765 0.749	0.765
Volume at admission, per cent of piston displacement:		6.03
	5.95 50 8.41	7.91
	50 8.41	7.91
Weight of air discharged per stroke, kg.:	2744 0.276	0.2750
	2716 0.274	
	546 0.551	1 7 %
Calculation from expansion diagram:	340 0.33-	1 -134-
Absolute pressure at release, kgs.:		
Head end	32 1.31	1.33
Crank end	45 I.44	1.46
Absolute pressure at compression, kgs. :		1
Head end	14 1.14	1.17
Crank end	20 I.19	1.22
Volume at release, per cent of piston displacement:		
Head end 104.		104.8
Crank end	r 106.3	106.4
Volume at compression, per cent of piston displacement:		
Head and		16.6
Crank end	8 rg.6	20.6
Air used per stroke, kg.:		
	234 0.233	0.238
Crank end	254 0.254	
Air used per revolution	488 0.487	0.493
Difference of weights, calculated by compression and expansion	064	0.055
	058 0.064 6 11.6	10.0
In per cent of the former		0.520
Mean weight of air per revolution, kg		66.1
		363
Heat withdrawn per H. P. per hour, calories	334	} 5-5

## TABLE XXXVII.

## TESTS ON REFRIGERATING MACHINES. By Professor Schröter.

		achine.	Dimen	sions of t cylinder	he steam	Dir	nensions o	of the					
Numb	er.	System of the machine.	Diameter of piston, mm.	Diameter of piston-rod, mm.	Stroke, mm.	Diameter of piston, mm.	Diameter of piston-rod, mm.	Stroke, mm.					
1	5		371, 25 400 " " 330 450 "	55; 5  5;2 68	800 602 " " " 740 900	325 250 " " " 430	- 63 - 55 - · · · · · · · · · · · · · · · · · · ·	540 420 " " " " " " "	36 34 106 50 46 35 11 9				
	minut	power der.	рожег	Abs ki	olute press los. per so	ures of va-	por, er.	Coolin	gw				
Number.	Revolutions per minute compressor.	Indicated horse-power of steam cylinder.	Indicated horse-power of compressor.	In compressor during expulsion.	In condenser.	In compressor during admission.	In vaporizer.	Initial temperature.					
1 2 3	64.8 59.8 54.7	53.6 66.1	45·9 26.27	9.58	6.99 9.31 13.66	2.50	2.76 2.64 {4.85   4.55 }	11.10					
4 ····································	55.I 59.I		27.30 29.23		14.06		4.90 4.53 4.91 4.55	II.2 II.2					
6 7 8 9 10 11	49.6 65.15 26.1 65.8 34.5 64.2 91.2 64.7 94.5 64.5 99.2		65.15 26.1 65.8 34.5 64.2 91.2 64.7 94.5 64.5 99.2		65.15 26. 65.8 34. 64.2 91. 64.7 94. 64.5 99.		24.49 18.1 25.8 52.01 61.70 66.42 75.02	8.13 10.68 3.77 4.11 4.23 5.81	13.78 7.87 10.41 3.22 3.50 3.62 5.11	2.36 2.97 0.45 0.63 0.73 0.67	4.27 4.83 2.63 3.24 0.82 1.03 1.15 1.06	8.77 8.82 10.15 10.1 10.15	
				Ice formed. Temperatur water or brucooled.			or brine						
	Number.				Per compressor horse-power, per hour, gross, kilos.	Per compressor horse-power, per hour, net, kilos.	At entrance,	At exit.	Trace				
I				9.0 8.3	34.8	31.7	-4·4 -5·9	-4·4 -5·9					
3	· · · · · · · · · · · ·		•••••	• • • •			11.19	2.95					
,	•			••••		••••	11.2	2.38					
5 ········ 6 ······							11.2	4.71					
7 8 9 10				11.3 11.3	16.8 25.0 28.2	 15.2 22.6	-9.50 -3.1 -18.2 -10.0	-9.97 -4.1 -18.2 -10.0					
	· · · · · · · · · · · · · · · · · · ·		<u></u>	11.3	20.6	25.9 18.5	6.05	<u>6.05</u>					

the data and results of tests on three refrigerating-machines on the Linde system using ammonia, and of a machine on Pictet's system using Pictet's fluid, all by Professor Schröter. The tests on machines used for making ice were necessarily of considerable length, but the tests on machines used for cooling liquids were of shorter duration.

The cooling water when measured was gauged on a weir or through an orifice. In the tests 3 to 6 on a machine used for cooling fresh water the heat withdrawn was determined by taking the temperatures of the water cooled, and by gauging the flow through an orifice, for which the coefficient of flow was determined by direct experiment. The heat withdrawn in the tests 7 and 8 was estimated by comparison with the tests 3 to 6. The net production of ice in the tests 1 and 2 was determined directly; and in the test 2 the loss from melting during the removal from the moulds was found by direct experiment to be 8.45 per cent. By comparison with this the loss by melting in the first test was estimated to be 7.7 per cent. The gross production of ice in the refrigerator was calculated from the net production by aid of these figures. In the tests 9 to 12 on the Pictet machine the gross production was determined from the weight of water supplied, and the net production from the weight of ice withdrawn.

A separate experiment on the machine used for cooling brine gave the following results for the distribution of power:

Total	horse-powe	er .											57.1
	expended												
"	"	"	cen	trif	ugal	рu	mĮ	)					9.8
"	"	"	wa	ter-	pum	α							3.6

The centrifugal pump was used for circulating the brine through a system of pipes used for cooling a cellar of a brewery. The water-pump supplied cooling water to the condenser and for other purposes. A similar test on the Pietet machine gave:

			K" (\$ \$ \$ \$ \$ \$ \$ \$ \$ \$ \$ \$ \$ \$ \$ \$ \$ \$ \$	
4 4	• •	• •	and intermediate gear	16.6
* *	* *	* *	gear, and pump	20.0 11

In 1888 comparative tests were made by Professor Schröte on a Linde and on a Pictet refrigerating machine, in a speci building provided by the Linde Company which had eve convenience and facility for exact work. The following talgives the principal dimensions of the machines:

# PRINCIPAL DIMENSIONS OF LINDE AND PICTET REPRIGERATING MACHINES

			- Literature
	I.e to .	ŧr.	Pictet.
The state of the s			
Diameter of strain arbitrate, one	11+	\$ 5	31 61
张 化化溶性薄草的混乱 艾斯西日泉 山 历 复等自用工業化 表 " 不 リロタ	3 %	an g	#8.6
atrigas griaticas bumā, a ses	4	NE	5
संस्थातिक विकास का का अपने के अपने का अपने का अपने का अपने का अपने का अपने का अपने का अपने का अपने का अपने का	1	4	5
Siterafter nat atmaren gefatiere, u ter.	9 8		ña
४ ४ ४५५६६ ह <i>े १९ १,७७</i> ० ८४ ,   ४ १४३	42		62
Itigenentine alf griger bie nagmielenen, nintuental, errin-	ž ·	\$	44
จัดกรีสาทิตแลลี. สตรงตร	1 2		16
Longth of pipe in tird vaporiors, in	4 4 %	6	538.3
men unders ir mymericans, ais	有音響	\$	538.2
l kingument ink gilgno die e resultationer, makmenad, sveiri	3.9	4	44
icelatoria	\$12		36
Length of pipe in condenses, m.	4 4 %	4	483.1
			2

The Linde machine used ammonia and was allowed to dra a mixture of liquid and vapor into the compressor, so that water jacket was required. The Pictet machine used Picte fluid, which is a mixture of sulphur dioxide and carbon dioxi and had the compressor cooled by a water jacket.

The data and results of the tests are given in Table XXXVI. Five tests were made on each machine. The temperature the salt solution or brine, from which heat was withdrawn by taporizers, was allowed to vary about three degrees centigrafrom entrance to exit. The entrance temperatures were intend

TESTS ON REFRIGERATING-MACHINES. By Professor M. Schröter, Vergleichende Versuche an Källemaschinen.

		0	ne vaporize	er.	
Pictet machine.	r	11	111	IV	v
Steam-engine: Revolutions per minute	57.0 21.81	56.8 20.88	57.1 18.75	57.6 15.93	59·3 27.56
Horse-power Mechanical efficiency Pressure in condenser, kilograms per square	16.82 0.771	16.10 0.771	14.26 0.761	11.83 0.743	22.9T 0.83T
centimetre	3.99	3.91	3 84	4.25	6.39
Vaporizer: Mean temperature of brine, entrance	1.47 6.10	r.o5 1.96	0.68	0.17	1.05
Mean temperature of brine, exit Specific heat per litre Initial temperature of brine, entrance Initial temperature of brine, exit Final temperature of brine, entrance Final temperature of brine, exit	3.08 0.850 6.09 3.03 6.11 3.05	-1.90 -4.98 0.847 -2.02 4.99 -2.04 -4.98	- 9.92 -12.91 0.845 - 9.91 -12.91 - 9.94 -12.88	17.93 20.96 0.841 18.00 21.00 18.00	-2.04 -5.01 0.846 -1.99 -5.02 -2.05 -4.96
Condenser: Mean temperature of cooling-water, entrance Mean temperature of cooling-water from	9.65	9.60	9.6r	9.68	9.68
condenser	19 72	10.70	19.59	19.51	35.18
jacket Initial temperature of condensing-water,	15.5	15.6	16.8	16.7	18.6
entrance Initial temperature of condensing-water, exit Final temperature of condensing-water,	9.57 19.71	9.64	9.58	9.68	9.73 35.08
entrance Final temperature of condensing-water, exit Error in heat account, per cent Refrigerative effect, calories per horse-power		9.57 19.64 +0.6	9.61 19.35 +0.4	9.72 19.59 -1.3	9.72 35.01 +8.9
Linde machine.	3507	2556	1852	1075	1
				_	
Steam-engine: Revolutions per minute Horse-power Compressor:	44.9 18.14	45.1 18.26	45.1 17.03	44.8	45.0 24.41
Horse-power  Mechanical efficiency  Pressure in condenser, kilograms per square	15.53 0.856	0.833	0.840	0.805	21.86 0.895
centimetre		9.24	9.00	8.89	14.03
Centimetre	3.80	2.95	2.13	1.56	2.05
Mean temperature of brine, entrance Mean temperature of brine, exit Specific heat per litre Initial temperature of brine, entrance Initial temperature of brine, exit. Final temperature of brine, ontrance.	6.00 2 89 0.850 5 98 2.89 5.97	-2.02 -5.02 0.846 -2.05 -5.02 2.04	- 9.99 - 12.91 - 0.843 - 9.95 -12.94	17.02 20.82 0.840 17.07 20.83 17.00	- 5.01 0.845 - 2.03 - 5.00 2.03
Final temperature of brine, exit	9.56	5.04 9.54	9.97 12.89 9.61 19.84	9.61 19.72	9.68 35·33
Mean temperature of cooling-water, exit.  Initial temperature of water, entrance Initial temperature of water, exit Final temperature of water, entrance Final temperature of water, exit  Error in heat account, per cent	19.76 9.56 29.74 9.57 19.74 —1.8	19.63 9.55 19.42 9.54 19.45 —1.8	9.61 19.82 9.60 19.89	9.64 19.79 9.56 19.88 — 2.1	9.68 35.45 9.65 35.44 +1
Refrigerative effect, calories per horse-power	4308	3182	2336	1711	2022

to be 6° C., 2° C., 10° C., and 18° C. The coolinwater was supplied to the condenser at about 0°.5 C., for a tests, and for all but one it left the condenser with a temperatu of nearly 20° C.; the lifth test on each machine was made with exit temperature of the cooling water at about 35° C.

The pressure in the compressor depended, of course, on the temperatures of the brine and the cooling water. For all the tests except the fifth on each machine, the maximum pressure of the working substance was nearly constant; about 9 kilogram per square centimetre for ammonia and about 4 kilograms for Pictet's fluid. The lifth test had considerably higher pressure corresponding to the higher temperature in the condenser. The minimum pressure of the working substance of course diminished as the brine temperature fell.

The heat yielded per hour to the ammonia in the vaporize was calculated by multiplying together the amount of brine use in an hour, the specific heat of the brine, and its increase of temperature. But the initial and final temperatures were no quite constant, and so a correction was applied. The her abstracted from the ammonia in the condenser was calculate from the water used per hour and its increase of temperatur The calculation for Pictet's machine involves also the jacke water and its imtrease of temperature. A correction is applied for the variations of initial and final temperatures of the cooling water. If the heat equivalent of the work of the con pressor is added to the heat yielded by the vaporizer the su should be equal to the heat abstracted by the cooling-wate The per cent of difference between these two calculations of the heat abstracted by the cooling water is a measure of the accuracy of the tests.

The refrigerative effect is obtained by dividing the heat yields by the vaporizer by the horse power of the steam cylinder. The first four tests with constant temperature in the condenser sho a regular decrease in the refrigerative effect for each machin as the temperature of the brine and the minimum pressure the working substance is reduced. The fifth test, with effect than the second test, which has nearly the same brine temperatures. These results are in concordance with the idea that a refrigerating-machine is a reversed heat-engine; for a heat-engine will have a higher efficiency and will use less heat per horse-power when the range of temperatures is increased, and *per contra*, a refrigerating-machine will be able to transfer less heat per horse-power as the range of temperatures is increased.

## TABLE XXXIX.

TESTS ON AMMONIA REFRIGERATING-MACHINE.

By Professor J. E. Denton, Trans. Am. Soc. Mech. Engr., vol. xii, p. 326.

Contract of the Contract of th				A CANADA LANGUAGE PARTY
	ı	11	III	IA
Pressure above atmosphere, pounds per square inch :			P. No. I.o. villamentos	
Ammonia from compressor	151	TSA	147	101
Ammonia back-pressure	28	8.2	1.3	27.5
Barometer, inclies of mercury.	30.07	20.50	20.87	30.01
Temperature, degrees Fahrenhelt :				
Brine, injet,	30.76	6.27	14.20	1
outlat	28.86	2.03	2.20	28.45
Condensing-water inlet	44 - 65	50.65	40.0	54.00
outlet,	83.66	85.4	85.46	82.86
Jacket-water, inlet	44.65	50.7	46.0	54 - 3
Ammonia-vapor, leaving brine-tank	34.2	14.7	3.0	20.2
entering compressor	30	25	10.13	34
leaving compressor	213	203	230	221
enloulated	530	304	200	237
entering condenser	200	218	300	168
Brine, pounds per minute	2281	2173	942.8	2374
Specific gravity			1.174	1.174
Specific heat	0.83	0.78	0.78	0.78
Ammonia, lbs. per min. by metre		14.68	16.67	28.32
			22.10	34.51
Heat account, B.T.U. per minute:			00-	
Given to ammonia by brine.	14776	71876	8824	14647
compressor,,,,,		3330	2518	3030
Total received by ammonia	140	147	167	141
Taken from ammonia by condenser	17702	9653	11400	17708
jackets	17242	90.50	0010	17350
atmosphere	182	712	656	400
Total taken from ammonta	18032	338	10816	18017
Error, per cent	10032	1		
Power, etc.:	2	5	3 . 5	2
Revolutions nor minute	\$8.90		57.88	58.8g
Revolutions per minute	85.0	57.7	73.6	88.6
compressor	65.7	54.7	50.4	71.2
Mechanical efficiency	0.81	0.83	0.86	0.83
Refrigerative effect:	9.01	0.03	0.60	3.63
Tons of ice (melted) in 24 hours	74.8	36.43	44.64	74.56
B.T.U. abstracted from brine per horse-power minute .	174	107	107	100
Pounds of ice (melted) per pound of coal	24.1	X4.1	17.37	23.37
wannes as and formannel first from the constitution of the	44.4	~~	1	-3.37

Table XXXIX gives the data and results of tests made by Professor Denton on an ammonia refrigerating-machine. The



only items requiring explanation are the refrigerative effect and the calculated temperature of the vapor leaving the condenser; the latter was calculated by the equation

$$T_* = T_* \left( \frac{p_*}{p_*} \right)^{\circ n}$$

and shows both the cooling effect of the jacket and the error is assuming an adiabatic compression. The exponent used her is a tritle smaller than that of equation (240) page 407. The refrigerative effect was obtained by dividing the n.r.v. give to the ammonia in a minute by the horse power of the steam cylinder. The tons per horse power in 24 hours was obtained by multiplying the refrigerative effect in thermal units perminute by the number of minutes in a day and then dividing the product by 2000 (the pounds in a short ton) and by 14 (the heat of melting a pound of ice). The pounds of ice perpound of coal was based on an assumed consumption of the pounds of coal per horse power per hour, and was calculated to multiplying the n.t.t. per horse power per minute by 6 and dividing by 3 > 144.

The main dimensions of the machine were

Penneugine uit geeren vollereilen vollereilen fahregte anderegt		8.2	Inche	*
beteraket net managarieran a. u Jadrifura	100	10	24	
Industrians and obsesses a distinct		* 18	*6	
Stronger and oterates a place-fee		36	**	
Thingsporter and grigor beer augmehbere weed ausrabenbeuer	ī	*	42	
Lærigith ist griger in bagmiriere		Property	fret	
a washada si bun d		# 00G	**	

Test of an Absorption-machine. The principal data and the results of a test made by Professor J. E. Denton\* on a absorption ammonia refrigerating machine are given in Tab XI.. The machine is applied to chill a room of about 400,00 cubic feet capacity at a pork packing establishment at Ne Haven, Conn. In connection with this test the specific heat the brine, which served as a carrier of heat from the cold root to the ammonia, was determined by direct experiment. The

<sup>\*</sup> Truns. Am New Mark Ing , and a May atthe

## SEVEN DAYS' CONTINUOUS TEST, SEPT. 11-18, 1888.

	(X)	
	Generator	150.77
Average pressures	Steam	47.70
above atmosphere	Cooler	23.69
in lbs. per sq. in.	Absorber	23.4
	Atmosphere in vicinity of machine	80
	Generator	272
	T. (Inlet	21.2
	Brine Outlet	16.16
	(Inlet	$54\frac{1}{2}$
Average tempera-	Condenser Outlet	80
tures in Fahren-	Absorber { Inlet	80
heit degrees.	(Outlet	111
Herr degrees.	(Upper outlet to generator	212
	Heater Lower " absorber	178
	Inlet from absorber	132
	Inlet from generator	272
	Water returned to main boilers from steam	
	coil	260
Average range of	Condenser	$25\frac{1}{2}$
temperatures	Absorber	31
Fahr. degrees.	Brine	5.13
Brine circulated per	(Cubic feet	1,633.7
hour.	Pounds	119,260
Specific heat of brine	<u> </u>	0.800
Cooling capacity of p	nachine in tons of ice per day of 24 hours .	40.67
Steam consumption	per hour, to volatilize ammonia, and to	•
operate ammonia r	nump pounds	1,986
	Eliminated Per pound of brine	4.1
	Eliminated Total per hour	481,260
	Of refrigerating effect per pound of steam	
	consumption	243
	(At condenser, per hour	918,000
British thermal		1,116,000
units:	On entering generator	
dimen.	_ coil	1,203
	Per pound of steam On leaving generator	
		271
	Consumed by generator per lb. of steam	
	condensed	. 932
Condensing water De	er hour, in pounds	36,000
Faviralent ice produ	action per pound of coal, if one pound of coal	
evaporates ten noi	ands of steam at boiler	17.1
Colories refrigeration	ig effect per kilogram of steam consumed	135
Annovimate coi	Condensing coil	870
surface in sq. ft.	Absorber "	350
surrace in sq. it.	Steam "	200

brine chilled and the cooling water used were measured with meters, which were afterwards tested under the conditions of the experiment.

It is interesting to compare the refrigerative effects expressed in pounds of ice per pound of coal. On this basis the compressionmachine tested by Professor Denton has an advantage of

$$\frac{24.1 - 17.1}{24.1} = 100 - 10$$
 per cent.

But this comparison is really unfair to the compressionmachine, for its steam-engine is assumed to require a consumption of three pounds of coal per horse power per hour, while the calculation for the absorption-machine is based on the assumption that a pound of coal can evaporate ten pounds of water; but an automatic condensing engine of the given power should be able to run on 20 or 22 pounds of steam per horse-power per hour.

## CHAPTER XVII.

## FLOW OF FLUIDS.

Thus far the working substance has been assumed to be at rest or else its velocity has been considered to be so small that its kinetic energy has been neglected; now we are to consider thermodynamic operations involving high velocities, so that the kinetic energy becomes one of the important elements of the problem. These operations are clearly irreversible and consequently the first law of thermodynamics only is available, and if any element of computation involves reference to equations that were deduced by aid of the second law, care must be taken that such computations are allowable. It is true that all practical thermal operations are irreversible for one reason or another; for example, the cycle for a steam engine is irreversible, both because steam is supplied and exhausted from the cylinder and because the cylinder is made of conducting material. But all adiabatic operations in cylinders (which serve as the basis of theoretical discussions) are properly treated as reversible and all the deductions from the second law may be applied to that part of the cycle. In particular the limitations of the discussion of entropy on page 32 have been observed.

Three cases of continuous thermal operations have been discussed (1) flow through a porous plug, (2) the throttling calorimeter, (3) friction of air in pipes; to which it may be well to return now. In all, the velocity of the fluid has been so small that its kinetic energy was neglected; in none of them was any reference made to equations deduced by the aid of the second law of thermodynamics. Rather curiously, all the operations were adiabatic, using the word to mean that no heat was taken from or lost to external objects; in the case of transmission of air in pipes, this comes from the natural conditions of the case

and in the other two operations there was careful insulatifrom heat. None of the operations are isoentropic; for instance the entropy of steam supplied to the calorimeter on page I is about 1,60 and the entropy of the superheated steam in t calorimeter is about 1.72; but this does not enter into the soluti of the problem and is more curious than useful.

The flow of fluids through orifices and nozzles has become even of more importance than formerly on account of the development of steam turbines. Thus far all computations have be based on adiabatic action, and when attempt is made to all for friction it is done by the application of an experimen factor to results from adiabatic computations.

The following is the sustomary method of establishing t fundamental equation. Suppose that a fluid is flowing fro the larger pipe A into the pipe there will clearly be an increase velocity, with a reduction in pressu

The first law of thermodynam as expressed by equation (16), page needs the addition of a term to to

account of the change in kinetic energy, and may be writ do - A sale + dW + dK);

the last term in the parenthesis represents the increase of kine energy.

Let it be supposed that there is a frictionless piston in ea cylinder; the piston in A exerts the pressure P, on the fluid front of it, and the piston in B has on it the fluid pressure Each unit of weight of fluid passing from A through the ori has the work p,v, done on it, while each pound entering cylinder B does the work p,v,. The assumption of piston merely a matter of convenience, and if they are suppressed name conditions with regard to caternal work will hold.

If the velocity in A is I', the kinetic energy of one unit weight in that cylinder is  $\frac{V_{i,j}}{2g}$ ; the kinetic energy in B is for a velocity V,

is no heat communicated to or from the fluid the sum of the intrinsic energy, external work, and kinetic energy must remain constant, so that

$$E_1 + p_1 v_1 + \frac{V_1^2}{2g} = E_2 + p_2 v_2 + \frac{V_2^2}{2g};$$
 (255)

this is the fundamental equation for the flow of a fluid.

If the walls of the pipes are well insulated there will not be much radiation or other external loss even if the pipes have considerable length, and in cases that arise in practice that loss may properly be neglected. There is likely to be a considerable frictional action even if the pipes are short, and the logical method appears to call for the introduction of frictional terms at this place. Such is not the custom, and a substitute will be discussed later.

Usually the velocity in the large cylinder A is small and the term depending on it may be neglected. Solving for the term depending on the velocity in B and dropping the subscript, we have

$$\frac{V^2}{2g} = E_1 - E_2 + p_1 v_1 - p_2 v_2 \quad . \quad . \quad (256)$$

Incompressible Fluids.—There is little if any change of volume or of intrinsic energy in a liquid in passing through an orifice under pressure, so that the equation of flow becomes in this case

$$\frac{V^2}{2g} = (p_1 - p_2)v_1 \dots (257)$$

If the difference of pressure is due to a difference of level or head, h, we have

$$p_1 - p_2 = hd,$$

where d is the density, or weight of a unit of volume, and is the reciprocal of the specific volume; consequently equation (257) reduces to

$$\frac{V^2}{2g} = h, \qquad (258)$$

which is the usual equation for the flow of a liquid throughall orifice.

Flow of Gases. - The intrinsic energy of a unit of weig a gas is

which depends only on the condition of the gas and not on changes that have taken or may take place. The equation the flow of a gas therefore becomes

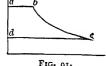
$$\frac{17}{48} = \frac{P_1 v_1}{R} = \frac{P_2 v_2}{R} + \frac{P_1 v_3}{R} + \frac{P_2 v_4}{R} = \frac{P_1 v_4}{R} + \frac{P_2 v_4}{R} +$$

At this place it is enstormany to me the equation

for the reduction of the equation \$2583 just as though we dealing with an adiabatic expansion in a non-conducting explinder. Now the fact that the isoenergic line and the thermal line are practically identical (page 63) shows the perfect gas has no disgregation energy and consequently for adiabatic change all the change in intrinsic energy is available to change all the change in intrinsic energy is available to doing outside work, which in this case is applied to increase the kinetic energy of the gas, instead of being applied to piston of a compressed air motor. If this analogy is allequation (259) may be used, and will yield

so that equation (258) may be reduced to

$$\frac{17}{28} - h = \frac{1}{2} \left[ \left( \frac{h}{h} \right)^{\frac{1}{2}} \right] \dots$$



work of air in the cylinder of a compressed air motor (Fig. 91). The work of admission is  $p_1v_1$ ; the work of expansion is by equation (81), page 65.

$$\frac{p_1 v_1}{\kappa - 1} \left\{ 1 - \left( \frac{v_1}{v_2} \right)^{\kappa - 1} \right\} = \frac{p_1 v_1}{\kappa - 1} \left[ 1 - \left( \frac{p_2}{p_1} \right)^{\frac{\kappa - 1}{\kappa}} \right];$$

and the work of exhaust is

$$-\dot{p_2}v_2 = -\dot{p_1}v_1\left(\frac{p_2}{p_1}\right)^{\frac{\kappa-1}{\kappa}};$$

so that the effective work is

$$p_1 v_1 + \frac{p_1 v_1}{\kappa - 1} \left[ 1 - \left( \frac{p_2}{p_1} \right)^{\frac{\kappa - 1}{\kappa}} \right] - p_1 v_1 \left( \frac{p_2}{p_1} \right)^{\frac{\kappa - 1}{\kappa}}$$

which is readily reduced to equation (261).

For the calculation of velocities it is convenient to replace the coefficient  $p_1v_1$  in equation (261) by  $RT_1$ , since pressures and temperatures are readily determined and are usually given, thus

$$\frac{V^2}{2g} = RT_1 \frac{\kappa}{\kappa - 1} \left[ 1 - \left( \frac{p_2}{p_1} \right)^{\kappa - \frac{\tau}{\kappa}} \right] \quad . \quad (262)$$

If the area of the orifice is a, then the volume discharged per second is

$$aV$$
,

and the weight discharged per second is

$$w = \frac{aV}{v_2},$$

when  $v_2$  is the specific volume at the lower pressure and is equal to

$$v_2 = v_1 \left(\frac{p_1}{p_2}\right)^{\frac{1}{\kappa}} = \frac{RT_1}{p_1} \left(\frac{p_1}{p_2}\right)^{\frac{1}{\kappa}} . . . . . (263)$$

Substituting V from equation  $\pm 2020$  and  $v_2$  from (263) and reducing

$$w = a \cdot \frac{p_i}{\sqrt{p_i}} \left( \frac{2g}{R} \right)_{K}^{K} \left[ \left( \frac{p_i}{p_i} \right)^{2} \cdot \left( \frac{p_i}{p_i} \right)^{2} + 1 \right]^{\frac{1}{4}}. (264)$$

The equations deduced for the flow of air apply to the flow from a large cylinder or reservoir into a small straight tub through a rounded orifice. The lower pressure is the pressure in the small tube and differs materially from the pressure of the space into which the tube may deliver. In order that the flow shall not be much affected by friction against the sides of the tube it should be short—not more than once or twice its diameter. The flow does not appear to be affected by making the tube very short, and the degree of rounding is not important; the equations for the flow of both air and steam may be applied with a fair degree of approximation to orifices in thin plates and to irregular orifices.

Professor Fliegner \* made a large number of experiments on the flow of air from a reservoir into the atmosphere, with pressure in the reservoir varying from 808 mm, of mercury to 3366 mm. He used two different critices, one 4.085 and the other 7.314 mm in diameter, both well rounded at the entrance.

He found that the pressure in the orifice, taken by means a small side orifice, was 5.5767 of the absolute pressure in the reservoir so long as that pressure was more than twice the atmospheric pressure; under such conditions the pressure in the orificial independent of the pressure of the atmosphere.

If the ratio  $\frac{P_2}{P_1}$  is replaced by the number 0.5767 and if  $\kappa$  replaced by its value 1.405 in equation (264) we shall have to the equation for the flow of a gas

$$2\nu = 0.48 \, z_{12} \, \sqrt{\frac{z_{2}^{2}}{R}} \, \frac{f_{1}}{\sqrt{f_{1}}} \, \dots \, , \qquad (46)$$

<sup>\*</sup> The Civilingenious, and un, 30. 14. 1874.

pressure less than twice the atmospheric pressure Fliegner found the empirical equation

$$w = 0.9644a \sqrt{\frac{2g}{R}} \cdot \sqrt{\frac{p_a (p_1 - p_a)}{T_1}}, \quad . \quad . \quad (266)$$

where  $p_a$  is the pressure of the atmosphere.

These equations were found to be justified by a comparison with experiments on the flow of air, made by Fliegner himself, by Zeuner, and by Weisbach.

Although these equations were deduced from experiments made on the flow of air into the atmosphere, it is probable that they may be used for the flow of air from one reservoir into another reservoir having a pressure differing from the pressure of the atmosphere.

Fliegner's Equations for Flow of Air. - Introducing the values for g and R in the equations deduced by Fliegner, we have the following equations for the French and English systems of units:

French units.

$$p_1 > 2p_a$$
,  $w = 0.395a \frac{p_1}{\sqrt{T_1}}$ ;  
 $p_1 < 2p_a$ ,  $w = 0.790a \sqrt{\frac{p_a (p_1 - p_a)}{T_1}}$ .

English units. 
$$p_1 > 2p_a, \quad w = 0.530a \frac{p_1}{\sqrt{T_1}};$$
 
$$p_1 < 2p_a, \quad w = 1.060a \sqrt{\frac{p_a (p_1 - p_a)}{T_1}}.$$

 $p_1$  = pressure in reservoir;

 $p_x$  = pressure of atmosphere;

 $T_1$  = absolute temperature of air in reservoir (degrees centigrade, French units; degrees Fahrenheit, English units).



In the English system  $p_1$  and  $p_2$  are pounds per square inches and a is the area of the orifice in square inches, while w is the flow of air through the orifice in pounds per second. If desired the area may be given in square feet and the pressures in pounds on the square foot, as is the common convention in thermodynamics.

In the French system we is the flow in kilograms per second. The pressures may be given in kilograms per square metre and the area of in square metres; or the area may be given in square centimetres, and the pressures in kilograms on the same unit of area. If the pressures are in millimetres of mercury multiply by 13.5050; if in atmospheres, multiply by 10333.

Theoretical Maxima. From a discussion of the mean velocity of molecules of a gas Fliegner deduces for the maximum velocity through an orifice

in metric units. His ratio of pressure 0.5707 inserted in equation (202) gives

The algebraic maximum of equation (204) occurs for the ratio  $p_2 + p_4 = 0.5274$ , but this figure probably has no physical significance.

Flow of Saturated Vapor. For a mixture of a liquid and it vapor equation (110), page 95, gives

$$E = \frac{1}{4} (q + vp),$$

so that equation (256) gives for the adiabatic flow from a receptacle in which the initial velocity is zero

$$\frac{1^{r_1}}{2g} - \frac{1}{A} (q_1 - q_2 + x_1 \rho_1 - x_2 \rho_2) + \rho_1 v_1 - \rho_2 v_2 \quad (267)$$

Substituting for v, and v, from

 $A = q_1 - q_2 + x_1 \rho_1 - x_2 \rho_2 + A \rho_1 x_1 u_1 - A \rho_2 x_2 u_2 + A \sigma(\rho_1 - \rho_2).$ 

But

$$\rho + A p u = r;$$

$$\therefore A \frac{V^2}{2g} = x_1 r_1 - x_2 r_2 + q_1 - q_2 + A \sigma (p_1 - p_2). \quad (268)$$

The last term of the right-hand member is small, and frequently can be omitted, in which case the right-hand member is the same as the expression for the work done per pound of steam in a non-conducting engine, equation (143), page 136, except that as in that place the steam is assumed to be initially dry,  $x_1$  is then unity. The intrinsic energy depends only on the condition of the steam, and consequently reference to the second law of thermodynamics first comes into this discussion with the proposal to compute the quality  $x_2$  in the orifice by aid of the standard equation for entropy

$$\frac{x_1 r_1}{T_1} + \theta_1 = \frac{x_2 r_2}{T_2} + \theta_2;$$

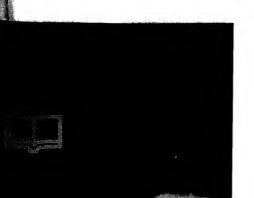
the acceptance of this method infers that the flow of steam through a nozzle differs from its action in the cylinder of an engine in that the work done is applied to increasing the kinetic energy of the steam instead of driving the piston.

Values of the right-hand member of equation (268) may be found in the temperature-entropy table which was computed for solving problems of this nature.

The weight of fluid that will pass through an orifice having an area of a square metres or square feet may be calculated by the formula

$$w = \frac{aV}{x_2u_2 + \sigma} \quad . \quad . \quad . \quad (268)$$

The equations deduced are applicable to all possible mixtures of liquid and vapor, including dry saturated steam and hot water. In the first place steam will be condensed in the tube, and in the second water will be evaporated.



receptacle, and comes to rest, the energy of motion will be turned into heat and will superheat the steam. Steam blowing into the air will be wet near the oritice, superheated at a little distance, and if the air is cool will show as a cloud of mist further from the oritice.

Rankine's Equations. After an investigation of the experiments made by Mr. R. D. Napier on the flow of steam, Rankine concluded that the pressure in the orifice is never less than the pressure which gives the maximum weight of discharge, and that the discharge in pounds per second may be calculated by the following empirical equations:

$$\begin{aligned} p_1 &= \alpha r + \frac{5}{3} p_{xx} & w &= a \frac{p_x}{p_x}; \\ p_1 &\in \frac{5}{3} p_{xx} & w &= \alpha \cos \mu a \left( p_x + p_x - p_x \right) p_x^2; \end{aligned}$$

in which  $p_i$  is the pressure in the reservoir,  $p_a$  is the pressure of the atmosphere, both in pounds on the square inch, and a is the area in square inches.

The error of these equations is liable to be about two per cent; but the flow through a given orifice may be known more closely if tests are made on it at or near the pressure during the flow, and a special constant is found for that orifice.

Grashoff's Formula. For pressures exceeding five-thirds of the external or back pressure Grashoff gives the following formula for the discharge of steam through a converging orifice,

the weight being in grams per second, the area in square centimetres and the pressure in kilograms per square centimetre. For English units the equation becomes

the discharge being in pounds per second, the area in square inches and the pressure in pounds absolute per square inch-Rateau shows that this formula is well verified by his experiments on the flow of steam, and that when the pressure is less than that required by the formula the flow can be represented by a curve which has for coördinates the ratio of the back pressure to the internal pressure and the ratio of the actual discharge to that computed by the equation on the preceding page.

The following values were taken from his curves:

Ratio of actual to computed discharge.				
Converging orifice.	Orifice in thin plates.			
0.45	0.30			
0.62	0.42			
0.73	0.51			
0.82	0.58			
0.89	0.64			
0.94	0.60			
0.97	0.73			
0.99	0.77			
	0.80			
	0.82			
	0.83			
	0.45 0.62 0.73 0.82 0.89 0.94 0.97			

He further gives a curve for the discharge from a sharp-edged orifice from which the third column was taken.

Flow of Superheated Steam. — Though there is no convenient expression for the intrinsic energy of superheated steam, and though the general equation (256) cannot be used directly, an equation for velocity can be obtained by the addition of a term to equation (268) to allow for the heat required to superheat one pound of steam, making it read

$$A \frac{V^2}{2g} = \int_{t_1}^{t} c dt + r_1 + q_1 - x_2 r_2 - q_2. \quad . \quad . \quad (269)$$

The accompanying equation for finding the quality of steam  $x_2$  is

$$\int_{T_1}^T \frac{cdt}{T} + \frac{r_1}{T_1} + \theta_1 = \frac{x_2 r_2}{T_2} + \theta_2 \quad . \quad . \quad (270)$$

Here t and T are the thermometric and the absolute temperatures of the superheated steam,  $t_1$  is the temperature of saturated steam at the initial pressure, and  $t_2$  the temperature at the final

pressure, and the letters  $r_1$  and  $r_2$  and  $\theta_4$  and  $\theta_2$  represent the corresponding heats of vaporization and entropies of the liquid.

Both equations apply only if the steam becomes moist at the lower pressure, which is the usual case. They may obviously be modified to apply to steam that remains superheated, but such a form does not appear to have practical application.

The method of reduction of the integrals in equation (269) and (270) is given on page 114; attention is called to the fact that the temperature entropy table affords ready solution of equation (200), also of the velocity flow during which the steam remains superheated.

Flow in Tubes and Nozzles. The velocity of air or steam flowing through a tube or nozzle with a large difference in pressure is very high, reaching 3000 feet a second in some cases; and consequently the effect of friction is marked even in short tubes and nozzles. A test by Büchner \* on a straight tube 3.52 inches long and 0.158 of an inch internal diameter, under an absolute pressure of 177 pounds to the square inch delivered only about 0.0 of the amount of steam calculated by the adiabatic method and the pressure in the tube fell gradually from 131 pounds near the entrance to 14.5 pounds near the exit when delivering to a condenser at about atmospheric pressure. If there were any use for such a device in engineering the problem would appear to call for a method of dealing with friction resembling that or page 380 for flow of air in long pipes, but probably more difficulty would be found in getting a satisfactory treatment.

From the investigations that have been made on the flow of steam through nozzles it appears that they should have a well rounded entrance, the radius of the curve of the section at entrance being half to three fourths of the diameter of the smalles section or throat; from the throat the nozzles should expand gradually to the exit, avoiding any rapid change of velocity as such a change is likely to roughen the surface where it occurs. The longitudinal section may well be a straight line joined to the entrance section by a curve of long radius. The taper of

<sup>\*</sup> Moittedangen über Fernkungenebesten Hoff, 18, ju 43.

the cone may be one in ten or twelve; this will give for the total angle at the apex of the cone 5° to 6°; if the entrance to the nozzle is not well rounded there will be a notable acceleration of the steam approaching the nozzle and this acceleration outside of the nozzle appears to diminish the amount of steam that the nozzle can deliver. The expansion should preferably be sufficient to reduce the steam to the pressure into which the nozzle delivers; otherwise the acceleration of the steam will continue beyond the nozzle, but the steam tends more and more to mingle with the adjacent fluid through which it moves, and a poorer effect is likely to be obtained.

If the expansion in the nozzle is not enough to reduce the pressure of the steam to (or nearly to) the external pressure into which the nozzle delivers, sound waves will be produced and there will be irregular action, loss of energy, and a distressing noise. On the other hand if the expansion in the nozzle reduces the pressure of the steam below the external pressure at the exit, sound waves will be set up in the nozzle with added resistance. This latter condition is likely to be worse than the former, and if the pressures between which the nozzle acts cannot be controlled it should be so designed as to expand the steam to a pressure a little higher than that against which it is expected to deliver, allowing a little acceleration to occur beyond the nozzle.

Friction Head. — In dealing with a resistance to the flow of water through a pipe, such as is caused by a bend or a valve, it is customary to assume that the resistance is proportional to the square of the velocity and to modify equation (258), page 425 to read

$$h=\frac{V^2}{2g}+C\frac{V^2}{2g},$$

where C is a factor to be obtained experimentally. The term containing this factor is sometimes called the head due to the resistance or required to overcome the resistance, and the equation may be changed to

$$h = \frac{V'}{2K} + h'$$

it being understood that of the available head h, a certain portion h' is used up in overcoming resistances and the remainder used in producing the velocity V. This aspect is well expressed by shifting h' to the other side of the equation and writing

$$\frac{V^{i}}{j_{K}}-h=h^{i}-h\left(i-\frac{h^{i}}{h}\right)-h\left(i-y\right).$$

This method has been used by writers on steam turbines allow for frictional and other resistance and losses. It must be admitted that it is a rough and unsatisfactory method, be perhaps it will serve. The value of y probably varies between cost and outs for flow through a single nozzle or set of guid blades or moving buckets in a steam turbine.

There is one difference between the behavior of water an an elastic fluid like air or steam that must be clearly understood and kept in mind. Frictional resistance and other resistance to the flow of water, transform energy into heat and that her is lost, or if it is kept by the water is not available afterward for producing velocity; on the other hand the energy which is expended in overcoming frictional or other resistances of like nature by steam or air, is changed into heat and remains it the fluid, and may be available for succeeding operations.

Experiments on Flow of Steam. There are five ways of experimenting on the flow of steam through oritices and nozzle that have been applied to test the theory of flow. Some of then used separately or in combination, can be made to give value of the friction factor v.

- (1) Steam flowing through an orifice or a nuzzle may be condensed and weighted.
- (2) The pressure at one or several points in a nozzle make measured by side crifices or by a scarching tube; the latte may be used to investigate the pressure in the region of the approach to the entrance, or in the region beyond the exit, and may also be used with an oribic.

- (3) The reaction of steam escaping from a nozzle or an orifice may be measured.
- (4) The jet of steam may be allowed to impinge on a plate or curved surface and the impulse may be measured.
- (5) A Pitot tube may be introduced into the jet and the pressure in the tube can be measured.

Of course two or more of the methods may be used at the same time with the greater advantage. It will be noted that none of the methods alone or in combination can be made to determine the velocity of the steam, and that all determinations of velocity equally depend on inference from calculations based on the experiments.

Formerly the weight of steam discharged was considered of the greatest importance, as in the design of safety-valves, or in the determination of the amount of steam used by auxiliary machines during an engine-test. The first method of experimenting was obviously the most ready method of determining this matter, and was first applied by Napier in 1869, and on his results were based Rankine's equations.

Since the development of steam turbines much importance is given to determination of steam velocities, though it is probable that the determination of areas is still the more important method, as on it depends the distribution of work and pressure, while a considerable deviation from the best velocity will have an unimportant influence on turbine efficiency. The first experiments on reaction were by Mr. George Wilson in 1872, but as his tests did not include the determination of the weight discharged they are less valuable.

Büchner's Experiments.—A number of experimenters have determined the weight of steam discharged by nozzles and tubes and at the same time measured the pressure in side-orifices at one or more places. The most complete appear to be those of Dr. Karl Büchner\* on the flow through tubes and nozzles. Omitting the tests on tubes and on nozzles with a very small

<sup>\*</sup> Mitteilungen über Forschungsarbeiten Heft 18, p. 47.

taper, the nozzles for which results will be quoted have the following designations and dimensions

NOZZLES TESTED BY DR. BUCHNER, ALL DIMENSIONS IN INCHES

Arangtha ti-m	i dat kangib	क्ष क्षित्रेवदश्यक्षेत्रेचे १ क्षत्रे द्वारक्षण्य	(ช้⊺กระจ ÷ รี้ สู?÷#1	Barmarunga ng Garroma	A night of	austauten Ling offin Ling offin Lings of the	Distance last side orifice from exi
							FEED TRANSPORTER
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2 2 5	2 12.7	· · · · **	g %-g	11 8 5 15	2 1	0 44	0.17
100	18 mg	0 13	8 74×5	0 259	7 3	11 44	0.14
39+	er upfic	1.12	2 87.5	1. 18.459	1 )	49 44	0 14
45	2 3 2	13 \$ 18	B 440 +	1 × 10 × 10 ×	\$11.5	13 14	0.11
5.1	1 17	11 3 4	\$ -0-4	18 3 49	8 4 2	0 24	0.11

All the nozzles had a cylindrical portion for which the lengis given in the above table including the rounding at entrange Excluding the rounding, this cylindrical portion was two or the times the diameter at the throat and appears to have had conserable influence on the distribution of the pressure. There we from one to three additional side orifices evenly distribute from pressure in these orifices Backner makes interesting contations concerning the behavior of the fluid in the tube, I the results are not different from those that are brought out the investigations of Stodola and are not included in this cussion. The data and results from such of the tests as appete bear on our present purpose of investigating the discharge a friction of nozzles are given on page 430.

Steam for these tests was taken from a boiler through a serator which probably delivered steam with a fraction of a percof priming. The pressures were all measured on one gauge aid of an eight way cook. The steam from the nozzles was edensed and weighted; the experimenter estimates the error to uncertainty of draining the condenser at two per cent, whappears to be the maximum error to be attributed to any of

results. The discharge was also computed by Grashoff's equation on page 432, and the ratio to the actual discharge is that set down in the table; the variation from unity is not greater than the probable maximum error. The method of the computation of velocities at throat and exit by the experimenter is not very clear, but it was made to depend on the equation (268), using the proper pressure and the discharge computed by Grashoff's equation.

TESTS ON FLOW OF STEAM.
Dr. Karl Büchner.

Number and designa- tion.	Pre	ssure pou		ute. External	Ratio of throat to initial.	Dis- charge pounds per second.	Ratio of actual to com- puted dis- charge.	Velocity at throat	Velocity at exit.	Ratio of actual to com- puted velocity.
1-2a 2-2a 3-2a 4-2a 5-2a	182 160.5 147.3 131.3	83.0	25.3 21.7 20.7 18.5 16.8	13.6 13.6 13.8 	0.577 0.564 0.572	0.0503 0.0449 0.0411 0.0370 0.0331	0.964 to 0.980	18co 1790 1820 1790 1780	3030 3020 2000 2000 2060	0.928 0.930 0.926 0.929 0.925
33-2h	180.2	92.1	16.5	1.j. t	0.511	0.0494		1940	3260	0.920
36-3a 37-3a 38-3a	140.0 131.5 115.7	70.4	21.2 10.5 17.4	13.6 13.8 13.8	0.535	0.0304 0.0363 0.0219		1860 1850 1850	3060 3020 3020	0.957 0.950 0.944
39-3b	183.6	99.6	18.5	18.5	0.541	0.0501	A A T	1830	3430	0.987
41-5b 42-5b 43-5b 44-5b 45-5b	103.0 89.3 75.2 61.0	58.7 49.3 37.6	38.1 32.8 27.0 22.3 16.0	15.4 14.0 14.7 14.5 14.5	o.658 o.656 o.643	0.0483 0.0419 0.0343 0.0282 0.0211	988 32 22	1550 1550 1560 1560 1630	2190 2180 2150 2160 2130	0.932 0.932 0.923 0.929 0.923
47-5c 48-5c 49-5c 50-5c	102.5 88.8 74.2 59.2	55.7 46.0	25.0 22.2 18.5 14.0	15.0 14.8 14.6 14.4	0.635	0.0540 0.0410 0.0344 0.0277	.017 to 120.	1630 1630 1620 1630	2520 2530 2530 2400	0.927 0.931 0.935 0.932

The nozzles 3a and 3b had tapers of 1:7.2 and 1:4.9 which were probably too great, so that they may not have been filled with

steam; this might account for the small ratio of the throat to t initial pressure; the nozzle 2b, which had a taper of 1:13, al shows a small ratio of throat to unital pressure.

The most interesting feature of the tests is the ratio of the velocity at exit, computed by the method referred to above, from the pressure at the side orifice near the exit from the nozzle. The does not appear to depend on the throat pressure. Leavi out tests on the nozzles 30 and 36 the mean value of this ratio about 0.03 which corresponds to a value y = 0.14.

Rateau's Experiments. These tests have already be referred to in connection with Grashoff's formula. They diffrom most tests on the discharge from orines and nozzles that the steam was condensed by a stream of cold water which steam was compensative and the amount of cold water us which latter was determined by thowing it through an orifi He estimates his error at something less than one per cent. The number of tests is too large to quote here; it may be enough say that his diagrams show a very great regularity in his results of that whatever error there may be is to be attributed to method, which does avoid, as he claims, the uncertainty draining a condenser.

Kneass' Experiments. In order to determine the press in steam-nozzles such as are used in injectors, Mr. Strickland Kneass † made investigations with a scarching tube, having small side orifice, both when the nozzles were performing the usual function in an injector and when discharging freely if the atmosphere. He also used side orifices bored through nozzles for the same purpose. The most interesting feature his investigation is that it makes practically modificence whet the discharge is free or into the combining tube of an injector.

<sup>\*</sup> Propositionental Researches on Francist Steam, trains It It Physica.

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For a well-rounded nozzle such as is used for an injector having a taper of one to six, he found the following results:

Absolute	Pressure.		Calculated Veloc-
Initial.	Throat.	Ratio.	ity at Throat.
135	82.0	0.606	1407
105	61.5	0.585	1448
75	42	0.550	1401
45	24.5	0.546	1504

Stodola's Experiments.—In his work on Steam Turbines, Professor Stodola gives the results of tests made by himself on the flow of steam through a nozzle, having the following proportions: diameter at throat 0.494, diameter at exit 1.45, and length from throat to exit 6.07, all in inches. The nozzle had the form of a straight cone with a small rounding at the entrance; the taper was 1:6.37. Four side orifices and also a searching-tube were used to measure the pressure at intervals along the nozzle; the searching-tube was a brass tube 0.2 of an inch external diameter closed at the end and with a small side orifice. This orifice was properly bored at right angles; two other tubes with orifices inclined, one 45° against the stream and one 45° down stream, gave results that were too large and two small by about equal amounts.

Stodola made calculations with three assumptions (1) with no frictional action, (2) with ten per cent for the value of y, and (3) with twenty per cent; comparing curves obtained in this way for the distribution of pressures with those formed by experiments, he concludes that the value of y for this nozzle was fifteen per cent.

Rosenhain's Experiments.—The most recent and notable experiments on flow of steam with measurement of reactions were made at Cambridge by Mr. Walter Rosenhain.\* Steam was brought from a boiler through a vertical piece of cycletubing to a chamber which carried the orifices and nozzles at its side; the reaction was counteracted by a wire that was attached to the chamber passed over an antifriction pulley to a scale pan, to which the proper weight could be added. Afterwards he determined the discharge by collecting and weighing steam

<sup>\*</sup> Proc. Inst. Civ. Eng., vol. cxl, p. 199.

under similar conditions. The steam pressure was controlled to a throttle valve. It is probable that there was some moisture the steam at high pressures and that at low pressures the steam was slightly superheated. The following table gives the dimensions of the nozzles:

ROSENHAIN'S TAPERIMENTS DIMENSIONS

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A calculation has been made by the adiabatic meth determine the pressures for which the several nozzles would expand the steam down to the pressure of the atmos

a direct calculation cannot be made, but a curve can readily be determined from which the pressure can be interpolated. The velocities corresponding to these pressures have been taken from Rosenhain's curves and the velocities were calculated also by the adiabatic method. Since the diagrams in the Proceedings are to a small scale the deduction of pressures from them cannot be very satisfactory, but the results are probably not far wrong. The table on page 442 gives the coefficient of friction obtained by this method.

Lewicki's Experiments. — These experiments were made by allowing the jet of steam to impinge on a plate at right angles to the stream, and measuring the force required to hold the plate in place; from this impulse the velocity may be determined. It was found necessary to determine by trial the distance at which the greatest effort was produced. One of his nozzles had for the least diameter 0.237 and for the greatest diameter 0.395 of an inch or a ratio of 1.28, which is proper for a pressure of 80 pounds per square inch absolute. His experiments gave the following results as presented by Büchner:

These experiments like those for reaction are liable to be vitiated by expansion and acceleration of the steam beyond the orifice.

Pressure in the Throat. — Some of the tests by Büchner show rather a low pressure in the throat of the nozzle, but in general tests on the flow of steam show a pressure in the throat about equal to 0.58 of the initial pressure provided that the back pressure has less than ratio 3/5 to the initial pressure; this corresponds with Fliegner's results and should be expected from his comparison with molecular velocity on page 430. The following table gives results of tests made by Mr. W. H. Kunhardt \* in the laboratories of the Massachusetts Institute of Technology:

The excess of the throat pressure above 0.58 of the initial

<sup>\*</sup> Transactions Am. Soc. Mech. Engs., vol. xi, p. 187.

pressure for the tests numbered a to q is to be attributed to the excessive length of the tube. Longer tubes tested by Buchner, showed the same effect in an exaggerated degree.

FLOW OF STEAM THROUGH SHORT TUBES WITH ROUNDED LNIESNESS

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Design of a Nozzle. Required the dimensions of a nozzle to deliver 500 pounds of steam per hour with a steam pressure of 50 pounds by the gauge and a vacuum of 26 inches of mercury. The vacuum of 26 inches can be taken as substantially equivalent to 2 pounds absolute and the steam pressure may be take as 165 pounds absolute. The threat pressure is then nearly pounds absolute. Assuming the steam to be initially dependently of the calculation can be arranged as follows:

$$x_{f_3} - T_3 \begin{pmatrix} r_1 & \theta_1 & \theta_2 \\ T_1 & \theta_3 & \theta_4 \end{pmatrix} = 784.141.0407 + 0.5245 + 0.4704) = 855$$

$$x_{f_3} - T_3 \begin{pmatrix} r_1 & \theta_1 & \theta_2 \\ T_1 & \theta_3 & \theta_3 \end{pmatrix} = 585.9 + 617.7 + 0.5245 + 0.1750 = 810$$

$$r_1 + q_1 = x_1 r_2 + q_2 = 855.9 + 617.7 + 850.8 + 94.1 = 288.5$$

$$r_1 + q_2 = x_3 r_3 + q_3 = 855.9 + 617.7 + 810.8 + 94.1 = 288.5$$

The quantities just obtained are the amounts of heat that would be available for producing velocity if the action were adiabatic. In order to find the probable velocity allowing for friction, they should be multiplied by  $\mathbf{r} - \mathbf{y}$ , where  $\mathbf{y}$  the coefficient for friction may be taken as 0.15 for the determination of the exit velocity  $V_s$ . As for the throat velocity, there are two considerations, the frictional effect is small because the throat is near the entrance, and all experiments indicate that orifices and nozzles which are not unduly long deliver the full amount of steam that the adiabatic theory indicates; therefore we may make the calculation for that part of the nozzle by the adiabatic method. The available heats for producing velocity may therefore be taken as

$$43.4$$
 and  $(1 - 0.15)$   $288.5 = 245$ ,

and the velocities are therefore (see page 436)

$$V_3 = \sqrt{64.4 \times .778 \times 43.4} = 1480.$$

$$V_a = \sqrt{64.4 \times 778 \times 245} = 3500.$$

The quality of steam in the throat is

$$x_1 = x_2 r_2 + r_3 = 855.1 + 885.9 = 0.967.$$

To find the quality of steam at the exit we may consider that if  $x_3$  is the actual quality allowing for the effect of friction we have

$$r_1 + q_1 - x_8' r_8 - q_8 = 245$$

$$x_8' = (855.9 + 337.7 - 245 - 94.3) + 1026 = 0.833.$$

Though not necessary for the solution of the problem it is interesting to notice that adiabatic expansion to the exit pressure would give for

$$x_1 = x_2 r_1 + r_2 = 810.8 + 1026 = 0.790.$$

Now 500 pounds of steam an hour gives

of a pound per second; consequently the areas at the throat and the exit will be by equation (208), page 431, in square inches

$$144a_2 \sim 144 \approx 0.130 \frac{x_2 a_2}{Y_2} \cdot \sigma$$

The diameters are, therefore,

$$d_1 = 0.380$$
  $d_2 = 1.030$ .

If the taper is taken to be one in ten, the conical part will hav a length of

10 (1.036 0.380) - 7.46 inches;

and allowing for the rounding at the entrance and for a fair cur joining the threat to the cone, the total length may be eiginches.

A nozzle to expand steam to the pressure of the atmosphe only, would have the computation for the exit made as follows:

$$x_{i}r_{i} = T_{i}\left(\frac{r_{i}}{T_{i}} + \theta_{i} - \theta_{i}\right) = 671.511.0170 + 0.6215 - 0.4125) = 838.$$

$$r_1 + q_1 - x_3 r_3 = q_4 - 855.0 \times 557.7 = 848.0 = 180.3 = 1750$$

Taking the coefficient for friction as corn the available he appears to be 158.0 and the velocity at exit will be

The quality of the steam comes from the equation

$$r_1 + q_1 = x_1 r_1 - q_1 - x_5 R.o.$$

$$x_3' = (855.4 + 337.7 - 158 - 180.3) = 965.8 = 0.885.$$

The area at the exit will now become

1444, - 144 8 .130 to 885 \* 20.04 \* 0.010 : 2810 - 0.168 and the corresponding diameter is 0.462 of an inch. Taki

and the corresponding diameter is 22,402 or an inch. The the taper as one in ten, the length of the conical part of the noz becomes

and its total length including throat and inlet may be 2.3 incl

## CHAPTER XVIII.

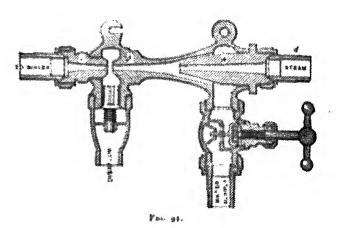
INJECTORS.

An injector is an instrument by means of which a jet of steam acting on a stream of water with which it mingles, and by which it is condensed, can impart to the resultant jet of water a sufficient velocity to overcome a pressure that may be equal to or greater than the initial pressure of the steam. Thus, steam from a boiler may force feed-water into the same boiler, or into a boiler having a higher pressure. The mechanical energy of the jet of water is derived from the heat energy yielded by the condensation of the steam-jet. There is no reason why an injector cannot be made to work with any volatile liquid and its vapor, if occasion may arise for doing so; but in practice it is used only for forcing water. An essential feature in the action of an injector is the condensation of the steam by the water forced; other instruments using jets without condensation, like the water-ejector in which a small stream at high velocity forces a large stream with a low velocity, differ essentially from the steam-injector.

Method of Working. — A very simple form of injector is shown by Fig. 91, consisting of three essential parts; a, the steam-nozzle, b, the combining-tube, and c, the delivery-tube. Steam is supplied to the injector through a pipe connected at d; water is supplied through a pipe at f, and the injector forces water out through the pipe at e. The steam-pipe must have on it a valve for starting and regulating the injector, and the delivery-pipe leading to the boiler must have on it a check-valve to prevent water from the boiler from flowing back through the injector when it is not working. The water-supply pipe commonly has a valve for regulating the flow of water into the injector.

This injector, known as a non-lifting injector, has the waterreservoir set high enough so that water will flow into the injector through the influence of gravity. A lifting injector has a speci device for making a vacuum to draw water from a reservo below the injector, which will be described later,

To start the injector shown by Fig. 91, the steam valve is fir opened slightly to blow out any water that may have gathere above the valve, through the overflow, since it is essential to hardry steam for starting. The steam valve is then closed, ar the water-valve is opened wide. As soon as water appears at the overflow between the combining-tube and the delivery-tube if



steam-valve is opened wide, and the jet of steam from the steam nozzle mingles with and is condensed by the water and imparto it a high velocity, so that it passes across the overflow spaletween the combining tube and the delivery tube and pass into the boiler. When the injector is working a vacuum is lish to be formed at the space between the combining and deliver tubes, and the valve at the overflow closes and excludes a which would mingle with the water and might interfere withe action of the injector.

Theory of the Injector. The two fundamental equations the theory of the injector are deduced from the principles of the conservation of energy and the conservation of momenta.

The heat energy in one pound of steam at the absolute pressure  $p_1$  in the steam-pipe is

$$\frac{1}{A}(x_1r_1+q_1),$$

where  $r_1$  and  $q_1$  are the heat of vaporization and heat of the liquid corresponding to the pressure  $p_1$ ;  $\frac{1}{A}$  is the mechanical equivalent of heat (778 foot-pounds), and  $x_1$  is the quality of the steam; if there is two per cent of moisture in the steam, then  $x_1$  is 0.98.

Suppose that the water entering the injector has the temperature  $t_3$ , and that its velocity where it mingles with the steam is  $V_{w}'$ ; then its heat energy per pound is

$$\frac{1}{A}q_3$$

and its kinetic energy is

$$\frac{V_{w'^2}}{2g},$$

where  $q_3$  is the heat of the liquid at  $t_3$ , and g is the acceleration due to gravity (32.2 feet).

If the water forced by the injector has the temperature  $t_4$ , and if the velocity of the water in the smallest section of the delivery-tube is  $V_w$ , then the heat energy per pound is

and the kinetic energy is 
$$\frac{\frac{1}{A}q_4}{\frac{V_w^2}{2g}}.$$

Let each pound of steam draw into the injector y pounds of water; then, since the steam is condensed and forced through the delivery-tube with the water, there will be x + y pounds delivered for each pound of steam. Equating the sum of the heat and kinetic energies of the entering steam and water to the sum of the energies in the water forced from the injector, we have

$$\frac{1}{A}(x_1r_1 + q_1) + y\left(\frac{1}{A}q_3 + \frac{V_w'^2}{2g}\right) = (1 + y)\left(\frac{1}{A}q_4 + \frac{V_w^2}{2g}\right) \quad (269)$$

The terms depending on the velocities  $V_{\omega}$  and  $V_{\omega}$  are new large and can commonly be neglected.

To get an idea of the influence of the former, we may consict that the pressure forcing water into a non-lifting injector is a dom, if ever, greater than the pressure of the atmosphere, a the corresponding pressure for a lifting injector is always le Now, the pressure of the atmosphere is equivalent to a head

A liberal estimate of v (the pounds of water per pound steam) is lifteen. Therefore,

$$y \frac{V_{a''}}{2k} - vh' - 15 - 34 - 510.$$

In order that an injector shall deliver water against the steat pressure in a boiler its velocity must be greater than would impressed on cold water by a head equivalent to the boil pressure. Taking the boiler pressure at 250 pounds by gange, or 265 pounds absolute, the equivalent head will be

Again taking fifteen for y, the value of the term depending on will be

$$(1 + y) \frac{1}{2x} - 11 + 151610 - 9150.$$

But the steam supplied to an injector is nearly dry and 205 pounds absolute

so that the term depending on that quantity will have the value

It is, therefore, evident that the term depending on  $V_w$  an influence of less than one persent and that the term depend on  $V_w$  can be entirely neglected.

For practical purposes we may calculate the weight of water delivered per pound of steam by the equation

$$y = \frac{x_1 r_1 + q_1 - q_2}{q_4 - q_5} \dots \dots (270)$$

This equation may be applied to any injector including double injectors with two steam-nozzles.

The discussion just given shows that of the heat supplied to an injector only a very small part, usually less than one per cent, is changed into work. When used for feeding a boiler, or for similar purposes, this is of no consequence, because the heat not changed into work is returned to the boiler and there is no loss.

For example, if dry steam is supplied to the injector at 120 pounds by the gauge or 134.7 pounds absolute, if the supply-temperature of the water is 65° F., and if the delivery-temperature is 165° F., then the water pumped per pound of steam is

$$y = \frac{r_1 + q_1 - q_4}{q_4 - q_8} = \frac{867.5 + 321.1 - 133.1}{33.1 - 33.16} = 10.5$$
 pounds.

From the conservation of energy we have been able to devise an equation for the weight of water delivered per pound of steam; from the conservation of momenta we can find the relation of the velocities.

The momentum of one pound of steam issuing from the steam-nozzle with the velocity  $V_s$  is  $V_s + g$ ; the momentum of y pounds of water entering the combining-tube with the velocity  $V_{w'}$  is  $yV_{w'} \rightarrow g$ ; and the momentum of x + y pounds of water at the smallest section of the delivery-tube is  $(x + y)V_w + g$ . Equating the sum of the momenta of water and steam before mingling to the momentum of the combined water and steam in the delivery-tube,

$$V_n + y V_{w'} = (1 + y) V_w \dots (270)$$

This equation can be used to calculate any one of the velocities provided the other two can be determined independently. Unfor-

that the proper sizes of the oritices and of the forms and propotions of the several members of an injector have been determine mainly by experiment. The best exposition of this matter given by Mr. Strickland Kneass,\* who has made many experments for William Sellers & Co.—The practical part of whifollows is largely drawn from his work.

Velocity of the Steam-jet. Laquation 12(4) gives

$$1 = \frac{1}{\sqrt{3}} \left\{ x_i r_i - x_j r_j + q_i - q_j r_j^{-1} \right\} . \quad (27)$$

where  $r_i$  and  $q_i$  are the heat of vaporization and the heat of the liquid of the supply of steam at the pressure  $p_i$ , and  $r_i$  and are corresponding quantities at the pressure  $p_i$  for that section the tube for which the velocity is calculated;  $v_i$  is the quality of the steam at the pressure  $p_i$  anomally o qS to unity) and  $x_i$  the quality at the pressure  $p_i$  to be calculated by aid of tequation

Here  $F_i$  and  $F_j$  are the absolute temperatures corresponding the pressures  $p_i$  and  $p_j$ , and  $\theta_j$  and  $\theta_j$  are the entropies of the liquid at the same pressure. Also  $\frac{\pi}{4}$  is the mechanical equivalent of heat and g is the acceleration due to gravity.

Some steam nozzles for injectors are simple converging orifiand others have a throat and a diverging portion. It will found in all cases including double injectors, that the pressbeyond the steam nozzle is less than half the pressure caus the flow, and consequently the pressure at the narrowest p of the steam nozzle and also the vehicity at that place, depeonly on the initial pressure. As was developed in the precedchapter, the pressure and velocity at any part of an expand nozzle depend on the ratio of the area at that part to the thr area, and are consequently under control. Also, as was emp-

<sup>\*</sup> Practice and Theory at the Infection, I Willey & South.

sized by Rosenhain's experiments, the steam will expand and gain velocity beyond the nozzle, if it escapes at a pressure higher than the back-pressure. For an injector this last action is influenced by the fact that the jet from the steam-nozzle mingles with water and is rapidly condensed. Some injector makers use larger tapers than those recommended in the preceding chapter for expanding nozzles. The throat pressure may be assumed to be about 0.6 of the initial pressure; with the information in hand it is probably not worth while to try to make any allowance for friction.

The calculation of the area at the throat of a steam nozzle by the adiabatic method will be found fairly satisfactory; the calculation of the final velocity of the steam will probably not be satisfactory, as complete expansion in the nozzle seldom takes place, but it is easy to show that the velocity is sufficient to account for the action of the instrument.

For example, the velocity in the throat of a nozzle under the pressure of 120 pounds by the gauge or 134.7 pounds absolute is

$$V_{s} = \left\{ \frac{2g}{A} \cdot (x_{1}r_{1} - x_{2}r_{2} + q_{1} - q_{2}) \right\}^{\frac{1}{2}}$$

$$= \left\{ 2 \times 32.2 \times 778 \cdot (867.5 - 0.967 \times 894.6 + 321.1 - 282.7) \right\}^{\frac{1}{2}}$$
= 1430 feet per second,

having for  $x_2$ 

$$x_2 = \frac{T_2}{r_2} \left( \frac{r_1}{T_1} + \theta_1 - \theta_2 \right) = \frac{1}{1.1587} (1.0719 + 0.5032 - 0.4546)$$
= 0.967,

provided that  $p_2 = 0.6p_1 = 80.8$  pounds absolute.

If, however, the pressure at the exit of an expanded nozzle is 14.7 pounds absolute, then

$$x_3 = \frac{1}{1.4390} (1.0719 + 0.5032 - 0.3125) = 0.877,$$

and

$$V_1 = \{2 \times 32.2 \times 778 \ (867.5 - 0.8775 \times 966.3 + 321.1 - 180.3)\}^{\frac{1}{2}}$$
  
= 2830 feet per second,

which is nearly twice that just calculated for the velocity at the smallest section of the steam nozzle. Since there is usually a vacuum beyond the steam nozzle, the final steam velocity is likely to be considerably larger, but this computed velocity will suffice for explaining the dynamics of the case.

Velocity of Entering Water. The velocity of the water in the combining tube where it mingles with the steam depends on (a) the lift or head from the reservoir to the injector, (b) the pressure for vacuum) in the combining tube, and (c) on the resistance which the water experiences from friction and eddies in the pipe, valves, and passages of the injector. The first of these can be measured directly for any given case; for example, where a test is made on an injector. In determining the proportions of an injector it is safe to assume that there is neither lift nor head for a non-lifting injector, and that the lift for a lifting injector is as large as can be obtained with certainty in practice. The lift for an injector is usually moderate, and soldom if ever exceeds so feet.

The vacuum in the combining tube may amount to 22 or 24 inches of mercury, corresponding to 25 or 27 feet of water; that is, the absolute pressure may be 3 or 3 pounds per square inch. The vacuum after the steam and water are combined appears to be limited by the temperature of the water; thus, if the temperature is 165° F., the absolute pressure cannot be less than 5.3 pounds. But the final temperature is taken in the delivery-pipe after the water and condensed steam are well mixed and are moving with a moderate velocity.

The resistance of friction in the pipes, valves, and passages of injectors has never been determined; since the velocity is high the resistance must be considerable.

If we assume the greatest vacuum to correspond to 27 feet of water, the maximum velocity of the water entering the combiningtube will not exceed

If, on the contrary, the effective head producing velocity is as small as 5 feet, the corresponding velocity will be

$$\sqrt{2 \times 32.2 \times 5} = 18 \text{ feet.}$$

It cannot be far from the truth to assume that the velocity of the water entering the combining-tube is between 20 and 40 feet per second.

Velocity in the Delivery-tube. — The velocity of the water in the smallest section of the delivery-tube may be estimated in two ways; in the first place it must be greater than the velocity of cold water flowing out under the pressure in the boiler, and in the second place it may be calculated by aid of equation (271), provided that the velocities of the entering steam and water are determined or assumed.

For example, let it be assumed that the pressure of the steam in the boiler is 120 pounds by the gauge, and that, as calculated on page 451, each pound of steam delivers 10.5 pounds of water from the reservoir to the boiler. As there is a good vacuum in the injector we may assume that the pressure to be overcome is 132 pounds per square inch, corresponding to a head of

$$\frac{132 \times 144}{62.4} = 305$$
 feet.

Now the velocity of water flowing under the head of 305 feet is

$$\sqrt{2gh} = \sqrt{2 \times 32.2 \times 305} = 140$$
 feet per second.

The velocity of steam flowing from a pressure of 120 pounds by the gauge through a diverging-tube with the pressure equal to that of the atmosphere at the exit has been calculated to be 2830 feet per second. Assuming the velocity of the water entering the combining-tube to be 20 feet, then by equation (271) we have in this case

$$V_w = \frac{V_s + y V_w'}{1 + y} = \frac{2830 + 10.5 \times 20}{1 + 10.5} = 266 \text{ feet};$$

this velocity is sufficient to overcome a pressure of about 470 pounds per square inch if no allowance is made for friction or losses.

Sizes of the Orifices. — From direct experiments on injectors as well as from the discussion in the previous chapter, it appears

that the quantity of steam delivered by the steam-nozzle can calculated in all cases by the method for the flow of ster through an orifice, assuming the pressure in the orifice to be of the absolute pressure above the orifice.

Now each pound of steam forces y pounds of water from reservoir to the builer; consequently if w pounds are drawn from the reservoir per second the injector will use were y pounds steam per second.

The specific volume of the mixture of water and steam in smallest section of the steam mostle is

where x<sub>j</sub> is the quality, u<sub>j</sub> is the increase of volume due to varization, and σ is the specific volume of the water. The volume steam discharged per second is

unet the area eef the estates or bo

$$\omega_{s} = \frac{n\pi}{2} \frac{1}{s}$$
 (6)

where I', is the velocity at the smallest section.

For example, for a them from 144.7 pounds absolute to be pounds absolute x, is contept and V, is 1440 feet, as found page 454. Again, for an increase of temperature from 65 to 165° F, the water per pound of steam is 16.5. Calculathe specific volume at 86.8 pounds, we have

r, - x,u, + a - 0.967 15.35 | 0 0167 + 0.016 - 5.20 cubic f

If the injector is required to deliver 1 7000 gallons an hour, c

munch per second, the area of the steam notate must be

The corresponding diameter is 6.420 of an inch, or 10.6 metres.

In trying to determine the size of the orifice in the deliverytube we meet with two serious difficulties; we do not know the velocity of the stream in the smallest section of the deliverytube, and we do not know the condition of the fluid at that place. It has been assumed that the steam is entirely condensed by the water in the combining-tube before reaching the deliverytube, but there may be small bubbles of uncondensed steam still mingled with the water, so that the probable density of the heterogeneous mixture may be less than that of water. Since the pressure at the entrance to the delivery-tube is small, the specific volume of the steam is very large, and a fraction of a per cent of steam is enough to reduce the density of the steam to one-half. Even if the steam is entirely condensed, the air carried by the water from the reservoir is enough to sensibly reduce the density at the low pressure (or vacuum) found at the entrance to the delivery-tube.

If  $V_w$  is the probable velocity of the jet at the smallest section of the delivery-tube, and if d is the density of the fluid, then the area of the orifice in square feet is

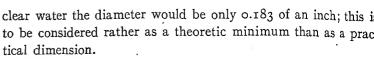
$$T_w = \frac{w(1+y)}{V_w dy}, \ldots (274)$$

for each pound of steam mingles with and is condensed by y pounds of water and passes with that water through the delivery-tube; w, as before, is the number of pounds of water drawn from the reservoir per second.

For example, let it be assumed that the actual velocity in the delivery-tube to overcome a boiler-pressure of 120 pounds by the gauge is 150 feet per second, and that the density of the jet is about 0.9 that of water; then with the value of w = 2.78 and y = 10.5, we have

$$a_w = \frac{w (i + y)}{V_w dy} = \frac{2.78 \times 11.5}{150 \times 0.9 \times 62.4 \times 10.5} = 0.00036 \text{ sq. ft.}$$

The corresponding diameter is 0.257 of an inch, or 6.5 millimetres. If this calculation were made with the velocity 266 (computed for expansion to atmospheric pressure) and with



Steam-nozzle. — The entrance to the steam-nozzle should be well rounded to avoid eddies or reduction of pressure as the steam approaches; in some injectors, as the Sellers' injector Fig. 92, the valve controlling the steam supply is placed near the entrance to the nozzle, but the bevelled valve-seat will not interfere with the flow when the valve is open.

It has already been pointed out that the steam-nozzle ma advantageously be made to expand or flare from the smalles section to the exit. The length from that section to the end ma be between two and three times the diameter at that section.

Consider the case of a steam-nozzle supplied with steam a 120 pounds boiler-pressure: it has been found that the velocit at the smallest section, on the assumption that the pressure is then 80.8 pounds, is 1430 feet per second, and that the specific volume is 5.20 cubic feet. If the pressure in the nozzle is reduced to 14.7 pounds, at the exit, the velocity becomes 283 feet per second, the quality being  $x_2 = 0.8775$ . The specific volume is consequently

$$v_2 = x_2 u_2 + \sigma = 0.877 (26.66 - 0.016) + 0.016 = 23.4 \text{ cu. ft.}$$

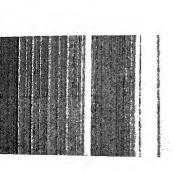
The areas will be directly as the specific volumes and inversel as the velocities, so that for this case we shall have the ratio of the areas

$$\left.\begin{array}{ccc}
5.20 : & 23.4 \\
2830 : & 1430
\end{array}\right\} = 1 : 2.27;$$

and the ratio of the diameters will be

$$\sqrt{1} \cdot \sqrt{2.27} = 1:1.5.$$

Combining-tube. — There is great diversity with different injectors in the form and proportions of the combining-tube. It is always made in the form of a hollow converging constraight or curved. The overflow is commonly connected to space between the combining-tube and the delivery-tube; it is



Sellers' injector, Fig. 92. In the latter case the combining- and delivery tubes may form one continuous piece, as is seen in the double injector shown by Fig. 93.

The Delivery-tube. — This tube should be gradually enlarged from its smallest diameter to the exit in order that the water in it may gradually lose velocity and be less affected by the sudden change of velocity where this tube connects to the pipe leading to the boiler.

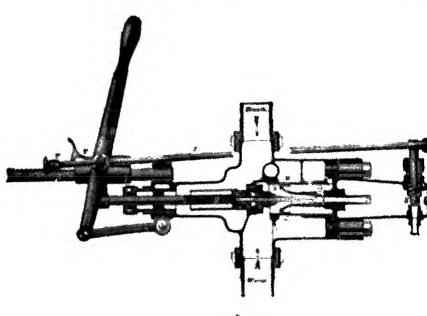
It is the custom to rate injectors by the size of the deliverytube; thus a No. 6 injector may have a diameter of 6 mm. at the smallest section of the delivery-tube.

Mr. Kneass found that a delivery-tube cut off short at the smallest section would deliver water against 35 pounds pressure only, without overflowing; the steam-pressure being 65 pounds. A cylindrical tube four times as long as the internal diameter, under the same conditions would deliver only against 24 pounds. A tube with a rapid flare delivered against 62 pounds, and a gradually enlarged tube delivered against 93 pounds.

If the delivery-tube is assumed to be filled with water without any admixture of steam or air, then the relative velocities at different sections may be assumed to be inversely proportional to the corresponding areas. This gives a method of tracing the change of velocity of the water in the tube from its smallest diameter to the exit.

A sudden change in the velocity is very undesirable, as at the point where the change occurs the tube is worn and roughened, especially if there are solid impurities in the water. It has been proposed to make the form of the tube such that the change of velocity shall be uniform until the pressure has fallen to that in the delivery-pipe; but this idea is found to be impracticable, as it leads to very long tubes with a very wide flare at the end.

Efficiency of the Injector. The injector is used for feeding boilers, and for little else. Since the heat drawn from the boiler is returned to the boiler again, save the very small part which is changed into mechanical energy, it appears as though the efficiency was perfect, and that one injector is as good as and provided that it works with certainty. We may almost constthe injector to act as a feed water heater, treating the pump in of feed water as incidental. It has already been pointed



on page 450 that the kinetic energy of the jet in the delice tube is less than one per cent of the energy due to the condetion of the steam. On this account the injector is used when cold water must be forced into a boiler, as on a becomotive when sea water is supplied to a marine boiler. Considerally the advantage of supplying hot water to the boiler almost seems as though the more steam an injector uses better it is. Such a seew is excensive, as it is often desire to supply water without immediately reducing the stepressure and then it is necessary to use as lattle steam as may it is, however, true that supplicate of construction and certain action are of the light importance in injectors.

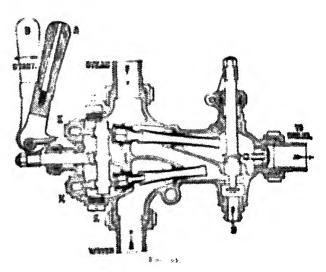
Lifting Injector. The injector described at the beginning

placed higher than the reservoir a special device is provided for lifting the water to start the injector. Thus in the Sellers' injector, Fig. 92, there is a long tube which protrudes well into the combining-tube when the valves w and x are both closed. When the rod B is drawn back a little by aid of the lever H the valve w is opened, admitting steam through a side orifice to the tube mentioned. Steam from this tube drives out the air in the injector through the overflow, and water flows up into the vacuum thus formed, and is itself forced out at the overflow. The starting-lever H is then drawn as far back as it will go, opening the valve x and supplying steam to the steam-nozzle. This steam mingles with and is condensed by the water and imparts to the water sufficient velocity to overcome the boilerpressure. Just as the lever H reaches its extreme position it closes the overflow valve K through the rod L and the crank at R.

Since lifting-injectors may be supplied with water under a head, and since a non-lifting injector when started will lift water from a reservoir below it, or may even start with a small lift, the distinction between them is not fundamental.

Double Injectors. — The double injector illustrated by Fig. 93, which represents the Körting injector, consists of two complete injectors, one of which draws water from the reservoir and delivers it to the second, which in turn delivers the water to the boiler. To start this injector the handle A is drawn back to the position B and opens the valve supplying steam to the lifting-injector. The proper sequence in opening the valves is secured by the simple device of using a loose lever for joining both to the valve-spindle; for under steam-pressure the smaller will open first, and when it is open the larger will move. The steam-nozzle of the lifter has a good deal of flare, which tends to form a good vacuum. The lifter first delivers water out at the overflow with the starting lever at B; then that lever is pulled as far as it will go, opening the valve for the second injector or forcer, and closing both overflow valves.

Self-adjusting Injectors. In the discussions of injector thus far given it has been assumed that they work at full capacity, but as an injector must be able to bring the water-leving a boiler up promptly to the proper height, it will have muc more than the capacity needed for feeding the boiler steadily Any injector may be made to work at a reduced capacity I simply reducing the opening of the steam-valve, but the lim



of its action is soon reached. The limit may be extended sor what by partially closing the water supply valve and so limit

the water supply.

The original Giffard injector had a morable steam-nozale control the thickness of the sheet of water mingling with steam, and also had a long conical valve thrust into the steam or the steam jet could be related. Thus both water and steam passages could be control without changing the pressures under which they were supplied the injector could be regulated to work through a variety of pressures and capacities. The main objection that the injector was regulated by hand and required mattention.

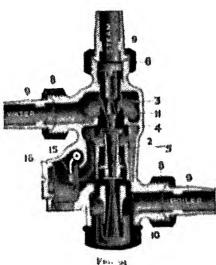
In the Sellers' injector, Fig. 92, the regulation of the steamsupply by a long cone thrust through the steam-nozzle is retained, but the supply of water is regulated by a movable combining-tube, which is guided at each end and is free to move forwards and backwards. At the rear the combining-tube is affected by the pressure of the entering water, and in front it is subjected to the pressure in the closed space O, which is in communication with the overflow space between the combiningtube and the delivery-tube, in this injector the space is only for producing the regulation of the water-supply by the motion of the combining-tube, as the actual overflow is beyond the delivery-tube at K. When the injector is running at any regular rate the pressures on the front and the rear of the combining-tube are nearly equal, and it remains at rest. When the startinglever is drawn out or the steam-pressure increases, the inflowing steam is not entirely condensed in the combining-tube as it is during efficient action; lateral contraction of the jet therefore occurs when crossing the overflow chamber, causing a reduction of pressure in O, which causes the tube to move toward D and increase the supply of water. When the starting-lever is pushed inward, reducing the flow of steam, the impulsive effort is insufficient to force a full supply of water through the deliverytube, and there is an overflow into the chamber O which pushes the combining-tube backwards and reduces the inflow of water. The injector is always started at full capacity by pulling the steam-valve wide open, as already described; after it is started the steam-supply is regulated at will by the engineer or boiler attendant, and the water is automatically adjusted by the movable combining-tube, and the injector will require attention only when a change of the rate of feeding the boiler is required on account of either a change in the draught of steam from the boiler, or a change of steam-pressure, for the capacity of the injector increases with a rise of pressure.

A double injector, such as that represented by Fig. 93, is to a certain extent self-adjusting, since an increase of steam-pressure causes at once an increase in the amount of water drawn in by



the lifter and an increase in the flow of steam through the steamnozzle of the forcer. Such injectors have a wide range of action and can be controlled by regulating the valve on the steampipe.

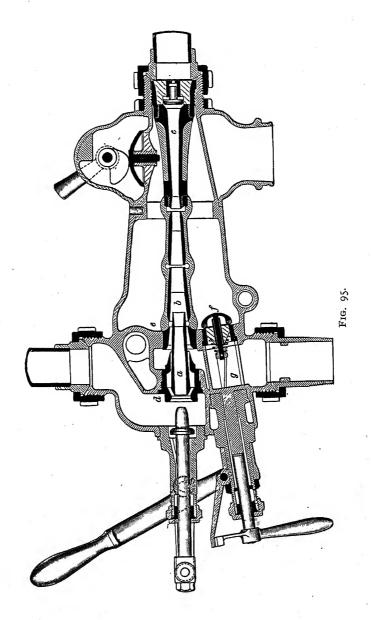
Restarting Injectors. If the action of any of the injector thus far described is interrupted for any reason, it is necessary to



shut off steam and start the injector anew; sometimes the injector has become heated while its action is interrupted and there may be difficulty in starting. To overcome this clifficulty various forms o restarting injectors have been dexised, such as the Sellers Fig. 91. This injector ha four travel mossles in line, th stram mossle 4, the draft-tub 11, the combining-tube ; and the delivery tube at th There is also a slic ing bushing sand an overflo

valve 15. The steam nozzle has a wide there and makes a vacuur which draws water from the supply tank under all conditions; the water passes through the draught tube and out at the overflountil the condensation of steam in the combining tube makes partial vacuum that draws up the bushing 5 against the draught tube and shuts off the passage to the overflow; the injector the forces water to the boiler. If the injector stops for any caus the bushing falls and the injector takes the starting position and will start as soon as supplied with water and steam.

Self-acting Injector. The most recent type of Sellers' injects invented by Mr. Kneass and represented by Fig. 95 is both self-acting and self-actinating. It is a double injector with all the je in one line; a, b, and s are the steam nozzle, the combining-tub and the delivery-tube of the forcer; the lifter is composed of the



annular steam nozzle d, and the annular delivery-tube e, su rounding the nozzle d. The proportions are such that the lifte can always produce a suction in the feed pipe even when the is a discharge from the main steam nozzle, and it is this fathat establishes the restarting feature. When the feed-waterises to the tubes it meets the steam from the lifter-nozzle aris forced in a thin sheet and with high velocity into the combining tube of the forcer, where it comes in contact with the masteam jet, and mingling with and condensing it, receives high velocity which enables it to pass the overflow orifices are proceed through the delivery tube to the boiler.

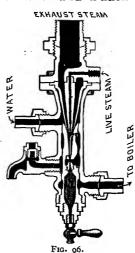
Like any double injector, the lifter and forcer have a cosiderable range of action through which the water is adjust to the steam supply; but there is a further adjustment in the injector, for when a good vacuum is established in the spasurrounding the combining tube, water can enter through to check valve f, and flowing through the orities in the combiing tube mingles with the jet in it, and is forced with that into the boiler.

The steam valve is scated on the end of the lifter nozz and it has a protruding plug which enters the forcer-nozz. When the valve is opened to start the injector, steam is at plied first to the starter, and soon after, by withdrawing to plug, to the forcer. If the steam is dry the starting-leverance he moved back promptly; if there is condensed water the steam pipe, the starting handle should be moved a lit way to first open the valve of the lifter, and then it is draw as far back as it will go, as soon as water appears at the overthow. The water supply may be regulated by the valve which can be rotated a part of a turn. The minimum delive of the injector is obtained by chosing this valve till puffs steam appear at the overthow, and then opening it enough to stop the escape of steam.

When supplied with cold water this injector wastes v little in starting. If the injector is hot or is filled with water when started, it will waste hot water till the injector cooled by the water from the feed-supply, and will then work as usual. If air leaks into the suction-pipe or if there is any other interference with the normal action, the injector wastes water or steam till normal conditions are restored, when it starts automatically.

Exhaust Steam Injectors. — Injectors supplied with exhaust-steam from a non-condensing engine can be used to feed boilers up to a pressure of about 80 pounds. Above this pressure a supplemental jet of steam from the boiler must be used. Such an injector, as made by Schäffer and Buden-

berg, is represented by Fig. 96; when used with low boiler-pressure this injector has a solid cone or spindle instead of the live-steam nozzle. To provide a very free overflow the combining-tube is divided, and one side is hung on a hinge and can open to give free exit to the overflow when the injector is started. When the injector is working it closes down into place. The calculation for an exhaust-steam injector shows that enough velocity may be imparted to the water in the delivery-tube to overcome a moderate boiler-pressure.



For example, an injector supplied with steam at atmospheric pressure, and raising the feed-water from 65° F. to 145° F., will draw from the reservoir

$$y = \frac{r_1 + q_1 - q_4}{q_4 - q_3} = \frac{966.3 + 180.3 - 113.0}{113.0 - 33.1} = 12.9$$

pounds of water per pound of steam. In this case as the steamnozzle is converging we will use for computing the velocity the pressure

$$0.6 \times 14.7 = 8.8$$
 pounds.

This will give

$$v_j r_j \sim F_j \left( \frac{r_1}{F_4} + \theta_1 + \theta_2 \right) \sim 646.881.4366 + 6.3125 \approx .2746 \right) \approx 954.6$$

consequently

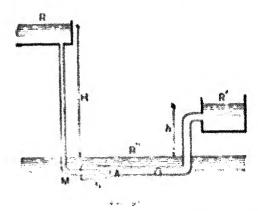
$$V = \sqrt{\frac{g}{A}} (r_1 + q_1 + x_2 r_2 - q_2)$$

$$\begin{split} & V = \sqrt{\frac{28}{4}} (r_1 + q_1 - x_1 r_2 - q_2) \\ & = \sqrt{2} (2.2 + 778) (400.2 + 180.1) + 454.0 + 155.3 = 1370. \end{split}$$

Assuming the velocity of the water entering the combining tube will give for the velocity of the jet in the combining-tube

This velocity is equivalent to that produced by a static pressur ()É

pounds absolute, or a gauge pressure of 100 pounds. No allow ance is made for reduction of density by bubbles of steam i the combining tube or for resistance of pipes and valves. I



such an injector can take advantage of further expansion eithe in the steam nozzle or beyond, the velocity may be greater tha that computed and a better action might ensue.

Unless the exhaust-steam is free from oil its use for feeding

the boiler with an exhaust steam injector will result in fouling the boiler.

Water-ejector. Fig. 97 represents a device called a water-ejector, in which a small stream of water in the pipe M flowing from the reservoir R raises water from the reservoir R' to the reservoir R'.

Let one pound of water from the reservoir R draw y pounds from R'', and deliver i + y pounds to R'. Let the velocity of the water issuing from A be v; that of the water entering from R'' be  $v_2$  at N; and that of the water in the pipe O be  $v_1$ . The equality of momenta gives

$$v + yv_1 - (1 + y)v_1 \dots (275)$$

Let x be the excess of pressure at M above that at N expressed in feet of water; then

$$v_2^2 \sim 2gx;$$
  
 $v^2 = 2g(H+x);$   
 $v_1^2 \sim 2g(h+x)$ 

Substituting in equation (275),

$$\sqrt{H+x}+y\sqrt{x}=(x+y)\sqrt{h+x};$$

$$\therefore y=\frac{\sqrt{H+x}-\sqrt{h+x}}{\sqrt{h+x}-\sqrt{x}} . . . (276)$$

It is evident from inspection of the equation (276) that y may be increased by increasing x; for example, by placing the injector above the level of the reservoir so that there may be a vacuum in front of the orifice A.

If the weight G of water is to be lifted per second, then  $\frac{G}{y}$  pounds per second must pass the orifice A, G pounds the space at N, and  $\left(\mathbf{r} + \frac{\mathbf{i}}{y}\right)G$  pounds through the section at O; which, with the several velocities v,  $v_2$ , and  $v_1$ , give the data for the calculation of the required areas.

PROBLEM. - Required the calculation for a water-ejector

to raise 1200 gallons of water an hour, H - of ft., h - 12 ft

The velocities are

The areas are

The diameters corresponding to the velocities r and r, are

$$d_1 = 0.38 \text{ of an inch:}$$

$$d_2 = 0.38 \text{ of an inch.}$$

The area a, is of annular form, having the area o.4 of a squa inch.

Ejector. - When the ejector is used for raising water whe there is no advantage in heating the water, it is a very wastel instrument. The efficiency is much improved by arrangi



the instrument as in Fig. 08, that the steam nozzle A shall deliv vehalty, which, as in the water a justim, elulivers a larger stream

a less velocity. Each additional conical mozzle increases t quantity at the expense of the schools, so that a large quanti of water may be lifted a small height.

Ejectors are commonly fitted in steamships as auxiliary pumps in case of leakage, a service for which they are well fitted, since they are compact, cheap, and powerful, and are used only in emergency, when economy is of small consequence.

Ejector-condensers. — When there is a good supply of cold condensing water, an exhaust-steam ejector, using all the steam from the engine, may be arranged to take the place of the air-pump of a jet-condensing engine. The energy of the exhaust-steam flowing from the cylinder of the engine to the combining-tube, where the absolute pressure is less and where the steam is condensed, is sufficient to eject the water and the air mingled with it against the pressure of the atmosphere, and thus to maintain the vacuum.

For example, if the absolute pressure in the exhaust-pipe is 2 pounds, and if the temperatures of the injection and the delivery are 50° F. and 97° F., then the water supplied per pound of steam will be about 20 pounds. If the pressure at the exit of the steam-nozzle can be taken as one pound absolute, the velocity of the steam-jet will be 1460 feet per second. If the water is assumed to enter with a velocity of 20 feet, the velocity of the water-jet in the combining-tube will be 88 feet, which can overcome a pressure of 50 pounds per square inch.

## CHAPTER XIX.

## STEAM TURBINES.

The recent rapid development of steam turbines may be attributed largely to the perfecting of mechanical construction making it possible to construct large machinery with the accurac required for the high speeds and close adjustments which these motors demand.

An adequate treatment of steam turbines, including details of design, construction, and management, would require a separat treatise; but there is an advantage in discussing here the therms problems that arise in the transformation of heat into kinetic energy, and the application of this energy to the moving part of the turbine. For this purpose it is necessary to give attention to the action of jets of thuids on vanes and to the reaction of jet issuing from moving particles, subjects that otherwise would appear foreign to this treatise.

The fundamental principles of the theory of turbines are the same whether they are driven by water or by steam; but the use of an elastic fluid like steam instead of a fluid like water, which as practically a constant density, leads to differences in the application of those principles. One feature is immediately evident from the discussion of the flow of fluids in Chapter XVI namely, that exceedingly high velocities are liable to be developed. Thus, on page 444 it was found that steam flowing from a gauge pressure of 150 pounds per square inch into a vacuum of 36 inches of mercury 12 pounds absolute through a propenozale, developed a velocity of 5000 feet per second, with a allowance of 0.15 for friction. This range of pressure corresponds to a hydraulic head of

and such a head will give a velocity of

$$V = \sqrt{2 \times 32.2 \times 376} = 156$$
 feet per second.

But so great a hydraulic head or fall of water is seldom, if ever, applied to a single turbine, and would be considered inconvenient. One hundred feet is a large hydraulic head, yielding a velocity of 80 feet per second, and twenty-five feet yielding a velocity of 40 feet per second is considered a very effective head.

If heads of 300 feet and upward were frequent, it is likely that compound turbines would be developed to use them; except for relatively small powers, steam-turbines are always compound, that is, the steam flows through a succession of turbines which may therefore run at more manageable speeds.

The great velocities that are developed in steam turbines, even when compounded, require careful reduction of clearances, and although they are restricted to small fractions of an inch the question of leakage is very important. Another feature in which steam turbines differ from hydraulic turbines is that steam is an elastic fluid which tends to fill any space to which it is admitted. The influence of this feature will appear in the distinction between impulse and reaction turbines.

Impulse. — If a well formed stream of water at moderate velocity flows from a conical nozzle, on a flat plate it spreads over it smoothly in all directions and exerts a steady force on it. If the velocity of the stream is  $V_1$  feet per second, and if w pounds of water are discharged per second, the force will be very nearly equal to

$$P = \frac{w}{g} V_1$$
.

Here we have the velocity in the direction of the jet changed from  $V_1$  feet per second to zero; that is, there is a retardation, or negative acceleration, of  $V_1$  feet per second; consequently the force is measured by the product of mass and the acceleration, g being the acceleration due to gravity. A force exerted by a jet or stream of fluid on a plate or vane is called an *impulse*. It

is important to keep clearly in mind that we are dealing wi velocity, change of velocity or acceleration, and force, and the the force is measured in the usual way. The use of a speci name for the force which is developed in this way is unfortuna but it is too well established to be neglected.

If the plate or vane, instead of remaining at rest, moves with evelocity of V feet per second, the change in velocity or negation evelocity or will be  $V_1 - V$  feet per second, and the force impulse will be

$$P = \frac{w}{s}(V_1 - V).$$

This force in one second will move the distance V feet and w do the work

$$\frac{w}{g}\left(V_{1}-V\right)V = \frac{w}{g}\left(V_{1}V-V^{2}\right) . . . . (27)$$

foot pounds.

Since the vane would soon move beyond the range of the jit would be necessary, in order to obtain continuous action or motor, to provide a succession of vanes, which might be mount on the rim of a wheel. There would be, in consequence, was of energy due to the motion of the vanes in a circle and splattering and other imperfect action.

If the velocity of the jet of water is high it would fail to spre fairly over the plate in Fig. 99, when it is at rest, and a cru motor of the sort mentioned would show a very poor efficient. Now steam has exceedingly high velocity when discharged from a nozzle, and the jet is more easily broken, so that adverse inferences have even a worse effect than on water, and there is t greater reason for following methods which tend to avoid was Also, as pointed out on page 434, the nozzle must be so formed to expand the steam down to the back pressure, or expansi will continue beyond the nozzle with further acceleration of the steam under unfavorable conditions.

It is easy to show that the best efficiency of the simple action a jet on a vane, which we have discussed, will be obtained making the velocity V of the vane half the velocity  $V_4$  of the j

For if we differentiate the expression (276) with regard to V and equate the differential coefficient to zero we shall have

$$V_1 - 2V = 0; \quad V = \frac{1}{2}V_1;$$

and this value carried into expression (276) gives for the work on the vane

$$\frac{1}{4}\frac{w}{\varrho}V_1^2;$$

but the kinetic energy of the jet is

$$\frac{1}{2}\frac{w}{g}V_1^2,$$

so that the efficiency is 0.5.

If the flat plate in Fig. 99 be replaced by a semi-cylindrical vane as in Fig. 99a, the direction of the stream will be reversed, and the impulse will be twice as great. If the vane as before has the velocity V the relative velocity of the jet with regard to the vane will be

V. - V F10. 99a.

and neglecting friction this velocity may be attributed to the water where it leaves the vane. This relative velocity at exit will be toward the rear, so that the absolute velocity will be

$$V - (V_1 - V) = 2V - V_1$$

The change of velocity or negative acceleration will be

$$V_i - (2V - V_i) = 2(V_i - V),$$

and the impulse is consequently

$$P = \frac{w}{g}.2 (V_1 - V).$$

The work of the impulse becomes

$$\frac{w}{g} \cdot 2 (V_1 - V) V = 2 \frac{w}{g} (V_1 V - V^2) \cdot (277)$$

The maximum occurs when

$$\frac{d}{dV} (V_1 V - V^2) = V_1 - 2 V = 0 \text{ or } V = \frac{1}{2} V_1.$$

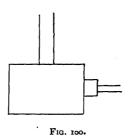
But this value introduced in equation (277) now gives

$$\frac{1}{2}\frac{w}{g}V_{1}^{2},$$

which is equal to the kinetic energy of the jet, and consequently the efficiency without allowing for losses appears to be unity.

Certain water-wheels which work on essentially this principle give an efficiency of 0.85 to 0.90. The method in its simplest form is not well adapted to steam turbines, but this discussion leads naturally to the treatment of all impulse turbines now made.

Reaction. — If a stream of water flows through a conical nozzle into the air with a velocity  $V_1$  as in Fig. 100, a force



$$R = \frac{w}{g} V_1 \dots (278)$$

will be exerted tending to move the vessel from which the flow takes place, in the contrary direction. Here again w is the weight discharged per second, and g is the acceleration due to gravity. The force R is called the *reaction*, a name that is so commonly used that it must be accepted

Since the fluid in the chamber is at rest, the velocity  $V_1$  is that imparted by the pressure in one second, and is therefore at acceleration, and the force is therefore measured by the product of the mass and the acceleration. However elementary this may appear, it should be carefully borne in mind, to avoid future confusion.

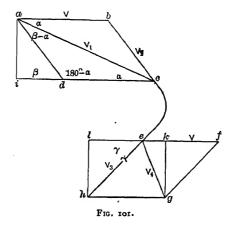
If steam is discharged from a proper expanding nozzle, which reduces the pressure to that of the atmosphere, its reaction will be very nearly represented by equation (278), but if the expansion is incomplete in the nozzle it will continue beyond, and the added acceleration will affect the reaction. On the other hand if the expansion is excessive there will be sound waves in the nozzle and other disturbances.

The velocity of the jet depends on the pressure in the chamber, and if it can be maintained, the velocity will be the same relatively to the chamber when the latter is supposed to move. The work will in such case be equal to the product of the reaction, computed by equation (278), and the velocity of the chamber. There is no simple way of supplying fluid to a chamber which moves in a straight line, and a reaction wheel supplied with fluid at the centre and discharging through nozzles at the circumference is affected by centrifugal force. Consequently, as there is now no example of a pure reaction steam turbine, it is not profitable to go further in this matter. It is, however, important to remember that velocity, or increase of velocity, is due to pressure in the chamber or space under consideration, and is relative to that chamber or space.

General Case of Impulse. — In Fig. 101 let ac represent the velocity  $V_1$  of a jet of fluid, and let V represent the velocity of a

curved vane ce. Then the velocity of the jet, relative to the vane is  $V_2$  equal to bc. This has been drawn in the figure coincident with the tangent at the end of the vane, and in general this arrangement is desirable because it avoids splattering.

If it be supposed that the vane is bounded at the sides so that the steam cannot spread laterally and



if friction can be neglected, the relative velocity  $V_3$  may be assumed to equal  $V_2$ . Its direction is along the tangent at the end e of the vane. The absolute velocity  $V_4$  can be found by drawing the parallelogram efgh with ef equal to V, the velocity of the vane.

The absolute entrance velocity  $V_1$  can be resolved into the

two components ai and ie, at right angles to and along the direction of motion of the vane. The former may be called the velocity of flow,  $V_P$  and the latter the velocity of whirl,  $V_w$ . In like manner the absolute exit velocity may be resolved into the components ek and kg, which may be called the exit velocity of whirl  $V_w$ , and the exit velocity of flow,  $V_P$ .

The kinetic energy corresponding to the absolute exit velocity  $V_{\star}$  is the lost or rejected energy of the combination of jet and vane, and for good efficiency should be made small. The exit velocity of whirl in general serves no good purpose and should be made zero to obtain the best results.

The change in the velocity of whirl is the retardation or negative acceleration that determines the driving force or impulse and the change in the velocity of flow in like manner produces an impulse at right angles to the motion of the vane, which in a turbine is felt as a thrust on the shaft.

Let the angle acd which the jet makes with the line of motion of the vane be represented by  $\alpha$ , and let  $\beta$  and  $\gamma$  represent the angles bed and leh which the tangents at the entrance and exit of the vane make with the same line.

The driving impulse is in general equal to

$$P = \frac{w}{R}(V_w - V_w')$$
; . . . . . . (279)

and the thrust is equal to

$$T = \frac{u'}{g}(V_f - V_f')$$
. . . . . . . (280)

which may be written

$$T = \frac{\pi}{\kappa} (V_x \sin \alpha - V_x \sin \gamma) . . . . (28\pi)$$

If there is no velocity of whirl at the exit the impulse becomes

$$P = \frac{w}{\kappa} \Gamma_1 \cos \alpha \quad , \quad , \quad , \quad , \quad (282)$$

The work delivered to the vanc per second is

$$W = \frac{2}{8}VV_1\cos \alpha, \qquad (383)$$

GENERAL CASE OF IMPULSE

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and since the kinetic energy of the jet is  $wV_1^2 \div 2g$  the efficiency is

$$e = 2 \frac{V}{V_1} \cos \alpha \dots \dots (284)$$

To find the relations of the angles  $\alpha$ ,  $\beta$ , and  $\gamma$ , we have from inspection of Fig. 102 in which el is equal to ef,

$$V_1 \sin \alpha = V_2 \sin \beta \dots (285)$$

$$V = V_2 \cos \gamma \dots \dots (286)$$

$$V = V_1 \cos \alpha - V_2 \cos \beta;$$

from which

$$V_1 \cos \alpha - V_1 \frac{\sin \alpha}{\sin \beta} \cos \beta = V_1 \frac{\sin \alpha \cos \gamma}{\sin \beta}$$
.

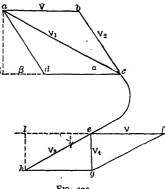
$$\therefore \sin \beta \cos \alpha - \cos \beta \sin \alpha = \sin \alpha \cos \gamma$$

and

$$\sin (\beta - \alpha) = \sin \alpha \cos \gamma$$
 . . . . . . (287)

The equations given above may be applied to the computation of forces, work, and efficiency when w pounds of fluid are discharged from one or several nozzles and act on one or a number of vanes; that is, they are directly applicable to any simple impulse turbine.

Example. Let  $V_1$ , the velocity of discharge, be 3500 feet per second as computed for a nozzle on page 444, and let  $a = \gamma = 30^{\circ}$ .



By equation (287)

$$\sin (\beta - \alpha) = \sin \alpha \cos \gamma = 0.5 \times 0.866 = 0.433.$$

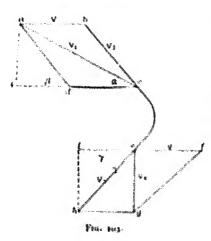
$$\beta - \alpha = 25 \text{ 40'}; \beta = 55^{\circ} \text{ 40'}$$

$$V_2 = V_1 \frac{\sin \alpha}{\sin \beta} = 3500 \frac{0.5}{0.866} = 2020$$

$$V = V_2 \cos \gamma = 2020 \times 0.866 = 1750$$

$$e = 2 \times 1750 \times 0.866 \div 3500 = 0.866.$$

No Axial Thrust. - The builders of impulse steam turl



attribute much important avoiding axial thrust, which be done by making the entrand exit angles of the vequal, provided that friend other resistances can eglected. This is evident equation (280), provided  $\gamma$  is made equal to T and also that sin  $\alpha$  is replaced by  $V_{\gamma}$  si Or the same conclusion of drawn from Fig. 104 begin this case

$$ai = V$$
,  $\sin a = V$ ,  $\sin \beta = V$ ,  $\sin \gamma = hl$ ,

and consequently there is no axial retardation.

The de Laval turbine has only one set of nozzles which exthe steam at once to the back pressure, and consequently velocity of the vanes is very high and even with small wit is difficult to balance them satisfactorily. This difficulmet by the use of a dexible shaft, and consequently axial tis likely to be troublesome; as a matter of fact the turbine arranged that the axial force (if there is any) shall be a The importance of avoiding axial thrust in other types of imturbines does not appear to be so great, and in some cases thrust may be an advantage, for example in marine propulse

If  $\gamma$  is made equal to  $\beta$  in equation (287) we have

and from inspection of Fig. 193 it is evident that V is half a velocity of whirl or

If this value is carried into equations (283) and (284) the work and efficiency become

$$W = \frac{1}{2} \frac{w}{g} V_1^2 \cos^2 \alpha \dots (290)$$

and

$$e = \cos^2 \alpha$$
. . . . . . . . . (291)

This freedom from axial thrust appears to be purchased dearly unless the accompanying reduction of velocity of the wheel is to be considered also of importance.

Example. If as in the preceding case the velocity of discharge is 3500 feet per second, and if  $\alpha$  is 30°, we have now the following results,

$$\cot \beta = \frac{1}{2} \cot \alpha = \frac{1}{2} \times 1.732 = 0.866 \therefore \beta = 49^{\circ} \text{ 1o'}$$

$$V = \frac{1}{2} V_1 \cos \alpha = \frac{1}{2} \times 3500 \times 0.866 = 1515$$

$$e = \cos^2 30^{\circ} = 0.75.$$

Effect of Friction. — The direct effect of friction is to reduce the exit velocity from the vane; resistance due to striking the edges of the vanes, splattering, and other irregularities, will reduce the velocity both at entering and leaving. The effect of friction and other resistances is two-fold; the effect is to reduce the efficiency of the wheel by changing kinetic energy into heat, and to reduce the velocity at which the best efficiency will be obtained. There does not appear to be sufficient data to permit of a quantitative treatment of this subject. Small reductions from the speed of maximum efficiency will have but small effect.

The question as to what change shall be made in the exit angle (if any) on account of friction will depend on the relative importance attached to avoiding velocity of whirl and axial thrust. If the latter is considered to be the more important, then  $\gamma$  should be made somewhat larger so that the exit velocity of flow may be equal to the entrance velocity of flow. But if it is desired to make the exit velocity of whirl zero, then  $\gamma$  should be somewhat decreased.

Design of a Simple Impulse Turbine. — The following computation may be taken to illustrate the method of applying the

foregoing discussion to a simple impulse turbine of the de Laval type.

Assume the steam-pressure on the nozzles to be 150 pounds gauge and that there is a vacuum of 26 inches of mercury; required the principal dimension of a turbine to deliver 150 brake horse-power.

The computation on page 444 for a steam-nozzle under these conditions gave for the velocity of the jet, allowing 0.15 for friction,  $V_1 = 3500$  feet per second. The throat pressure was taken to be 96 pounds absolute, giving a velocity at the throat of 1480 feet per second. The dryness factor was 0.965 at the throat; at the exit this factor was 0.833 for 0.15 friction and for adiabatic expansion was 0.790.

The thermal efficiency for adiabatic expansion with no allowance for friction or losses whatsoever, as for an ideal non-conducting engine, is given by equation (144) page 136 as

$$e = 1 - \frac{x_3 r_3}{r_1 + q_1 - q_3} = 1 - \frac{810.8}{856.0 + 337.6 - 94.3} = 0.262;$$

the corresponding heat consumption is

$$42.42 \div 0.262 = 162,$$

by the method on page 144.

Let the angle of the nozzle be taken as 30° as on page 481, then the angle  $\beta$  becomes 49° 10′, the efficiency is 0.75 and the velocity of the vanes must be 1515 feet per second.

Suppose that ten per cent be allowed for friction and resistance in the vanes, and that the friction of the bearings and gears is ten per cent; then, remembering that 0.15 was allowed for the friction in the nozzle, and that the efficiency deduced from the velocities is 0.75, the combined efficiency of the turbine should be

$$0.262 \times 0.75 \times 0.85 \times 0.9 \times 0.9 = 0.135$$
;

which corresponds to

$$42.42 \div 0.135 = 314$$
 B.T.U.

per horse-power per minute.

Now it costs to make one pound of steam at 150 pounds by the gauge or 165 pounds absolute, from feed water at 126° F. (2 pounds absolute)

 $r_1+q_1-q_2=856.0+337.6-94.3=1099$  B.T.U., consequently 314 B.T.U. per horse-power per minute correspond to

$$314 \times 60 \div 1099 = 17.2$$

pounds of steam per horse-power per hour.

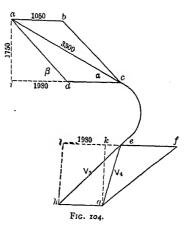
The total steam per hour for 150 horse-power appears to be

$$150 \times 17.2 = 2580.$$

If the nozzle designed on page 444 be taken it appears that

five would not be sufficient, as each would deliver only 500 pounds of steam per hour. But if allowance be made for a moderate overload, six could be supplied.

Not uncommonly turbines of this type are run under speed as a matter of convenience. Suppose, for example, the speed of the vanes is only 0.3 of the velocity of whirl, instead of 0.5; that is, in this case take V = 1050.

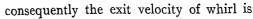


This case is represented by Fig. 104, from which it is evident that

$$V_f = V_f' = ai = V_1 \sin 30^\circ = 3500 \times 0.5 = 1750$$
  
 $V_w = V_1 \cos 30^\circ = 3500 \times 0.866 = 3030$   
 $\tan \beta = ai \div id = 1750 \div (3030 - 1050) = 0.884$ 

 $\beta = 41^{\circ} 30'$ . The two triangles *aid* and *elh* are equal, and

$$le = id = 3030 - 1050 = 1980;$$



$$W_f' = ek = 1050 - 1980 = -930.$$

Consequently the work delivered to the vane is

$$PV = \frac{w}{g} [3030 - (-930)] 1050 = \frac{w}{g} 3960 \times 1050$$
$$= 416000 \frac{w}{g}.$$

But the kinetic energy is  $wV_1^2 \div 2g$ , so that the efficient

$$416000 \times 2 \div \overline{3500}^2 = 0.68.$$

The combined efficiency of the turbine therefore becomes

$$0.262 \times 0.68 \times 0.85 \times 0.9 \times 0.9 = 0.123$$

instead of 0.135; and the heat consumption becomes

$$42.42 \div 0.123 = 345 \text{ B.T.U.}$$

per horse-power per minute; and the steam consumption incito

$$345 \times 60 \div 1099 = 18.8$$

pounds per horse-power per hour. The total steam per appears now to be about

$$18.7 \times 150 = 2800,$$

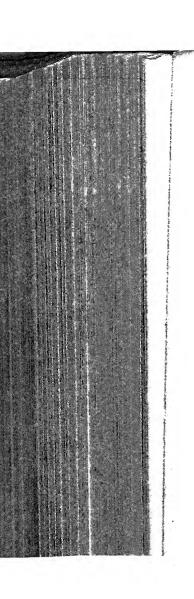
so that six nozzles like that computed on page 444 would only a margin for governing.

If the turbine be given twelve thousand revolutions per m the diameter at the middle of the length of the vanes will b

$$D = 1050 \times 12 \times 60 \div (3.14 \times 12000) = 20$$
 inches

The computation on page 444 gave for the exit diamet the nozzle 1.026 inches, and as the angle of inclination t plane of the wheel is 30°, the width of the jet at that would be twice the exit diameter or somewhat more, due to natural spreading of the jet. The radial length of the may be made somewhat greater than an inch, perhaps 176 in

The circumferential space occupied by the six jets will be



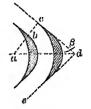
12½ inches out of 62.8 inches (the perimeter), or somewhat less than one-fifth. The section of the nozzle is shown by



Fto. 105.

Fig. 105, and the form of the vanes may be like Fig. 106. In this case the thickness of a vane is made half the space

from one vane to the next, or one-third the pitch from vane to vane. The normal width of the passage is made constant, the face of one vane and the back of the next vane being struck from the same centre. The form and spacing of vanes can be determined by experience only and appears to depend largely on the judgment of the designer. In deciding on the axial width of the vanes it must be borne in mind that



Fu. 106.

increasing that width increases the length and therefore the friction of the passage; but that on the other hand, decreasing the width increases the curvature of the passage which may be equally unfavorable. Sharply curved passages also tend to produce centrifugal action, by which is meant now a tendency to crowd the fluid toward the concave side which tends to raise the pressure there, and decreases it at the convex side. Mr. Alexander Jude,\* for a particular case with a steam velocity of 1000 feet per second, computes a change of pressure from 100 to 107.1 pounds on the concave side and a fall to 93.4 on the convex side. Even if this case should appear to be extreme there is no question that sharp curves are to be avoided in designing the steam passages.

Tests on a de Laval Turbine. — The following are results of tests on a de Laval turbine made by Messrs. J. A. McKenna

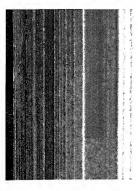
and J. W. Regan \* and by Messrs, W. W. Ammen and H. A. C. Small.†

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Compound Steam-Turbines. There are three ways in which impulse-turbines have been compounded at the steam may be expanded at once to the back pressure and then allowed to act on a succession of moving and stationary sanes, at the steam may flow through a succession of chambers each of which has in it one simple impulse wheel or sat a combination of these methods may be made, the steam flowing through a succession of chambers in each of which it acts on a succession of moving and stationary vanes. The first method which gives a very compact but an inefficient wheel, is used for the backing turbine of the Curtis marine-turbine. The second method is used in the Rateau turbine, which has usually a large number of chambers. The third method is found in the Curtis turbine which has from two to seven chambers in each of which are from two to four sets of revolving vanes.

The Parsons turbine, which is an impulse reaction wheel, has a very large number of sets of moving vance, i.e., from fifty to one hundred and fifty.

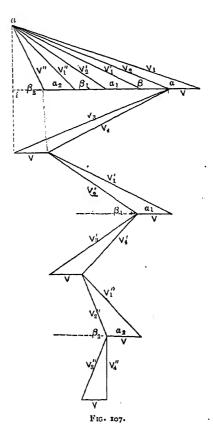
The various forms of compound turbines have been devised to reduce the speed of the vanes and the resolutions per minute to convenient conditions without sassificing the efficiency.



<sup>\*</sup> Thereis, MIII' again

Velocity Compounding. — In Fig. 107, let  $V_1$  represent the velocity of a jet of steam that is expanded in a proper nozzle

down to the back-pressure. Suppose it acts on an equalangled  $(\beta = \gamma)$  vane which has the velocity V. The relative velocity at entrance to that vane is  $V_2$  and this velocity reversed and drawn at  $V_n$  may represent the exit velocity, neglecting friction.  $V_4$  is the absolute velocity at exit from the vane, which may be reversed by an equal-angled stationary guide, and then becomes the absolute velocity  $V_1'$  acting on the next vane. The diagram of velocities for \*the second moving vane is composed of the lines lettered  $V_1'$ ,  $V_2'$ ,  $V_3'$  and  $V_4'$ ; the last of these is reversed by a stationary guide, and the velocities of the third vane are  $V_{1}'', V_{2}'', V_{8}''$  and  $V_{4}''$ . The diagram is constructed by dividing the velocity of whirl



$$V_w = V_1 \cos \alpha$$

into six equal parts, and the final exit velocity  $V_4$ " is vertical, indicating that there is no velocity of whirl at that place.

It is immediately evident, since the velocity of flow is unaltered in Fig. 107, and since there is no exit velocity of whirl that the efficiency neglecting friction is the same as for Fig. 103, namely

$$e = \cos^2 \alpha$$

as given by equation (291) page 481.

It is, however, interesting to determine the work done on each vane; the sum of the works of course leads to the same result. In Fig. 107 the velocity of whirl at entrance to the first vane is

and the velocity of which at exit is

consequently the work done on the vanc is

because I was made equal to one sixth of the velocity of whirl. This expression reduces to

The second and third vanes receive the works

so that the resultant work is

and the efficiency is evidently given by the expression already quoted. The most instructive feature of this discussion is that the relation of the works done on the three sames is

A similar investigation will show that the distribution among four vanes is

The first figure in such a series is editained by adding to the number of vanes one less than that number, and each succeeding term is two units smaller. Thus seven sance give the distribution

It is considered that this type of turbine cannot be made to give good efficiency in practice on account of large losses in passing through a succession of vanes and guides, especially as the steam in the earlier stages has high velocities. The turbine, however, has certain advantages when used as a backing device for a marine-turbine, in that it may be very compact, and can be placed in the low pressure or exhaust chamber, so that it will experience but little resistance when running idle during the normal forward motion of the ship.

In dealing with this problem it is convenient to transfer the construction to the combined diagram at abi, Fig. 107; diagrams for guides like that made up of the velocities  $V_s$ ,  $V_4$  and  $V_1$  being inverted for that purpose. It is clear that the absolute velocities at exit from the nozzle and the guides are represented by  $V_1, V_1'$  and  $V_1''$ , while the relative velocities are  $V_3$ ,  $V_2'$  and  $V_2''$  which with no axial thrust are equal to  $V_s$ ,  $V_s'$  and  $V_s''$ . The absolute velocity at entrance to a given guide is taken as equal to the absolute velocity at exit from the preceding vane, thus  $V_1'$  is equal to  $V_4$ , etc. The last absolute velocity  $V_4''$  is equal to ai the constant velocity of flow.

The angles  $\alpha_i$ ,  $\beta_i$ ,  $\alpha_{1i}$ ,  $\beta_{1i}$ ,  $\alpha_{2i}$  and  $\beta_{2i}$  are properly indicated as may be seen by comparing the original with the combined diagram.

If the diagram is accurately drawn to a large scale, the velocities and angles can be measured from it, or they may readily be calculated trigonometrically. Thus

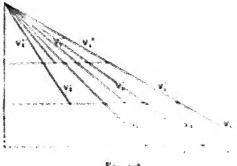
$$\tan \beta = \frac{\sin \alpha}{4 \cos \alpha}$$
;  $\tan \alpha_1 = \frac{\sin \alpha}{4 \cos \alpha}$  etc.,

$$V_y \rightarrow V_i \sin \alpha \cos \alpha \beta$$
;  $V_i' \rightarrow V_i \sin \alpha \csc \alpha_i$ , etc.

The radial length of the vanes and guides must be increased inversely proportional to the velocities, using relative velocities for the vanes and absolute velocities for the guides.

There appears to be no reason why the guides should be relieved from axial thrust provided they can be properly supported.

Except that the passages in the guides might become too long or too sharply curred, they might all be given the same delivery angle as the nozzle, and thus a notable improvement



in as othermy could be realized In Fig. 108 the schwitzer I. V. attel fig. afer efrawn in the armal manner, V. being equal to I'; the relients I'm is laid off along the patter line as - 1, and a letteral I. lifting reflect course been Action 118 foot in the W casts.

struction as indicated. It is in like manner last off for I.". metel their the elimptuete by averegeletert. The actimate at the catter a reclaim velle of the standards and the section of the

Following the problem on page 441 for a notice declarging from 140 mounds les the gauge into 26 moleco of sacuran we have V, - 3500 feet per as and with v - 0 15. The value of V may he taken as 620 feet per second, which gives a diagram with no final velocity of whirl.

The exit velocity of which from the first set of sames is a thio feet per second as measured on the diagram, and since the initial velocity of whirl is

the returdation is

The retardation for the second set of cames in

and for the third act is \$ 200, so that the work of the impulae is

and as the intrinsic energy of the jet is

$$\frac{3e}{2K}V_1^2 = \frac{1}{3}3500\frac{w}{K} = 6125000\frac{w}{g}$$

the efficiency of this arrangement without losses and friction appears to be

Effect of Friction. -- The effect of friction is to change some of the kinetic energy into heat, thereby reducing the velocity and at the same time drying the steam and increasing the specific volume so that the length of the guides and vanes must be increased at a somewhat larger ratio than would otherwise be recentierel.

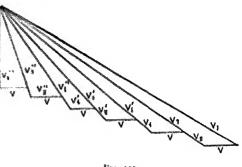
A method of allowing for friction is to redraw the diagram of Fig. 107, shortening the lines that represent the velocities to allow for friction.

In order to bring out the method clearly an excessive value will be assigned to the coefficient for friction, namely, y = 0.19, so that the equation for velocity may have for its typical form

$$V_a - \nabla agh(x - y) = 0.0 \sqrt{agh}$$
.

Again the coefficient will be assumed to be constant for sake of simplicity, more especially as but little is known with regard to its real value.

The diagram shown by Fig. 100 was drawn by trial with  $V_1 = 3500$ and with a - to". It appeared necessary to reduce I' to 380 feet per second, instead of 505 feet, which would be present without frie tion, this latter quantity bring one-sixth of the initial velocity of whirl,



Fu. 100

$$V_{*} = V_{*} \cos \alpha = 3500 \times 0.800 = 3030.$$

Starting with  $V_i$  the velocity of the jet, the triangle  $V_i$ ,  $V_i$  is drawn to determine the initial relative velocity for the first set of vanes. The exit velocity  $V_i$  is made equal to 0.0  $V_i$ , and the triangle  $V_i$ ,  $V_i$  is drawn to determine the absolute velocity at exit  $V_i$  from the guides. This is taken to be the velocity at entrance to the guides, but the exit velocity from them is taken to be  $V_i' = \cos V_i$ . Two repetitions of this process complete the diagram. The velocities of whirl at entrance to the three sets of vanes as measured on the diagram are

and the who ities of which at exit from those same are

so that the negative accelerations are

making a total of \$480. Since the schoots of the sames is 480 feet per second the work delivered to the turbane is

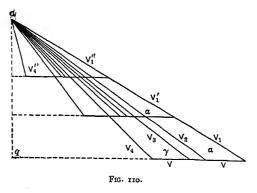
and consequently, using the kinetic energy already computed for the jet on the preceding page, the efficiency to

This method preserves the equality of the angles of the same and guides, but does not avoid axial thrust, for Fig. 100 shows a large reduction of the velocity of flow, and as there are no reversals of flow, the reduction is a measure of the impulse producing axial thrust. Nearly half of the thrust is borne by the fixed guides, and it is to be borne in small that the assumption of at exaggerated coefficient for fraction greatly exaggerates this feature, which in practice may not be acres troublesome.

To entirely avoid axial thrust it appears to be necessary only to slightly increase the angle y at the exit from the sane; the angles of the guides may be reduced if desired as an offset. In Fig. 110 an attempt is made to avoid axial thrust on the vanes, and at the same time to retain a fair efficiency

by making the delivery angle of the guides constant.

A calculation like that on page 492 indicates that an efficiency of 0.76 might be expected in this case. It is quite likely that in practice there might be difficulty



in making the delivery angle of the guide as small as 30°, but it appears as though the common idea that it is practically impossible to make an economical turbine on this principle is not entirely justified.

Pressure Compounding. — The second method of compounding impulse turbines with a number of chambers each containing a single impulse wheel like that of the de Laval turbine requires a large number of stages to give satisfactory results. For sake of comparison with preceding calculation we will take the same initial and final pressure and the same angle for the nozzles, namely, 150 pounds by the gauge and 26 inches vacuum, and  $\alpha = 30^{\circ}$ .

Nine stages in this case will give approximately the same speed of the vanes as in the problem on page 490. The temperature-entropy table which was made for work of this nature is most conveniently used with temperature, and in this case the initial and final temperature can be taken as 366° F. and 126° F. At 366° F. the steam is found to be nearly dry for the entropy 1.56 and that column will be taken for the solution of this problem. The heat contents is 1193.3 instead of 1193.6 as found for 366° F. in Table I of the "Tables of Properties of Steam." On the other hand the table gives at

126° for the heat contents 904.9, and the difference is

If we divide the available heat into mne portions we have for each

If again we take y = o, t which may be excessive in this case since, as will be evident, simple converging nozzles will be required, the velocity of the steam jet will be

$$V_{i} = N_{i} + 45.5 + 778 + 45 + 4 + 0.1 - 4500$$

feet per second. This is of contact the schoots for all the stages.

The choice of a - 40" gives for the achieuts of whiel

and the velocity of the vanes to give the maximum economy is half of this or \$30 feet per second or somewhat less if allowance be made for friction and other lesses.

Since we have to deal with a single impulse wheel in each chamber and since the wheels are usually designed to avoid axial thrust, all the combissions concerning that type of wheel may be assumed at once as has already facilly been done.

One of the important conclusions to that the efficiency without friction as given by equation (2013 page 481 to

with  $a = 30^\circ$ , this gives r = 0.75.

It is but fair to say that a smaller angle of a is used for this type of turbine and that the range of temperature is likely to be extended at both limits, and that in particular great importance is attached to occuring a good vacuum, 38 inches of mercury, corresponding to one pound absolute, is commonly obtained in good practice with all compound turbines.

If the peripheral speed of the wheel must be kept down, this type of turbine is likely to have a very large number of chambers. For example, if the speed must be no more than 500 feet per second (half of \$50), there must be 30 chambers instead of 9.

This will give for the available heat for each chamber 8 thermal units, and using as before y = 0.1 we shall have

$$V_1 - V_2 \times 32.2 \times 778 \times 8 \times 0.9 = 600$$

feet per second. With  $\alpha = 30^{\circ}$  the velocity of whirl is now 520 feet and the velocity of the vanes as stated is 260 feet per second.

The next question in the discussion of this turbine is the distribution of pressure. If the coefficients for friction and other losses are taken to be constant, then the pressure can be at once determined by the adiabatic method.

In the problem already discussed 32 B.T.U. are assigned to each stage, and if this figure be subtracted nine times in succession from the heat contents 1104 at the initial temperature we shall have the values which may be used in determining the intermediate temperatures from the temperature-entropy table. Also from that table or from Table I in the "Tables of Properties of Steam," the corresponding pressures can be determined. The work is arranged in the following table:

DISTRIBUTION OF PRESSURE.

	Values of or by	lemperatures.	Pressures absolute.	Ratios of pressures
fr.s	# # # # # # # # # # # # # # # # # # #	366	165	0.68
2	1 2612	336	113	0.66
3	2 2 31)	des	73.5	0.65
3	10217	278	47.8	0.64
4	tisfet	251	30.4	0.61
er.	1611	224	18.6	0.6r
E)	\$ 60,60 \$	100	11.3	0.58
7	e <sub>3</sub> f <sub>ee<sub>3</sub></sub>	174	6.55	0.57
K	417	150	3.71	0.53
**	4,0618	126	1.08	0.

The last column gives the ratio of any given pressure to the preceding pressure, i.e. 112:165 = 0.68. These ratios indicate that simple conical converging nozzles will be sufficient for all but the last stage. With the usual number of stages, twenty or more, the ratios are certain to be larger than 0.6 in all cases, indicating the use of converging nozzles throughout.

To determine the sizes of the nozzles or the passages in the guides it is necessary to estimate the quality of the steam in order to find the specific volume. To do this we may consider that, of the heat supplied to a certain stage of the turbine, a portion is changed into work on the turbine vanes, some part is radiated, and the remainder is in the steam that flows from the chamber of that stage; if there is appreciable leakage, special account must be taken of it, but both radiation and leakage can be left at one side for the present.

Now in the case under consideration, 32 thermal units were assigned to each stage in the adiabatic calculation for the distribution of pressure. But 2.10 part was assigned to y to allow for friction so that only 0.9 was applied to the calculation of velocity; of the kinetic energy of the jet 0.75 only was assumed to be applied to moving the vanes without friction, the remainder being in the kinetic energy of the flow from the vanes which was assumed to be changed into heat again; and further there was an allowance of 0.1 for losses in the vanes, leaving a factor, 0.9, to be applied for that action. Consequently instead of 32 thermal units changed into work per stage, our calculation gives only

will be changed into work. A method of determining the qualities and specific volumes at the several nozzles is illustrated in the table on the following page.

The quantity of heat changed into work per stage is subtracted successively, giving the apparent remaining heat contents as set down in the tables. At a given temperature we may find the quality by subtracting the heat of the liquid from the heat contents and dividing the remainder by the value of r. The specific volumes are determined by the equation

but as x is in all cases large, the effect of  $\sigma$  may be neglected altogether.

FIRST COMPUTATION OF QUALITIES AND VOLUMES.

	Temper atter (1)	finat ensimite (er by)	Heat of liquid	Value of xr	Heat of Vapori sation (r)	Quality (v)	Specific (s.	volumes
63	ztoto	2 2 2 2 2	338	855	855	Bir C Mithin Magazini indişi deyildi. T	2.78	2.78
ŧ	330	1174	307	867	878	880.0	3.95	3.90
2	tiefe	8844	170	HTH	800	0.978	5.79	5.66
.1	27%	11.45	247	HHH	910	0.076	8.65	8.44
4	188	2224	2313	Box	030	0.953	13.3	12.7
5	131	\$ cmaffx	194	004	958	0.044	21.0	19.8
(1	11713	1076	167	epidic	975	0.032	34.1	31.8
1	17.1	\$1167	140	915	993	0.012	56.8	52.2
M	\$ & CF	\$1197	12%	919	1010	0.010	97.0	88.3
E)	2.5%	\$102.56	1) 4	43.3.3	1016	0.001	175	158.0

By the aid of the temperature-entropy table, the qualities and specific volumes may be determined directly with good approximation, it being necessary only to follow the line of the temperature to an entropy column, having nearly the proper heat contents.

There is a serious objection to this method as applied, because it does not take any account of the fact that as the steam passes from stage to stage losing less heat than it would with adiabatic action, the entropy increases, and that with increased entropy the difference of heat contents between two given temperatures increases. This will be very apparent from inspection of a temperature-entropy diagram or the temperature-entropy table. This matter will be discussed more at length in connection with the Curtis type of turbine.

It has been assumed that the same amount of heat should be assigned to each stage for the adiabatic calculation and that the values of y to allow for friction and losses remain constant. As to the values that should be assigned to y, we have very little published information; it may be noted in passing that our allowance for friction in the nozzles and guides is probably too large. It will be evident that there is no difficulty in maintaining the amount assigned to each stage in its proper proportion even

though y shall be varied from stage to stage. For example, or choice of o.1 for both y and  $y_1$  gives

$$32 \times 0.9 \times 0.9 = 25.92 \text{ B.T.U.},$$

which multiplied by 0.75, the efficiency due to the angles are velocities, gives 19.44 B.T.U. as above. Let it be assumed for the moment that the above product shall be kept constant, so a to obtain the same velocity of jet in each stage. Then the following table exhibits a way of accomplishing this purpose while varying y and  $y_1$ :

Stage	ı	2	3	4	5	6	7	8	9
$y \cdot \cdot \cdot \cdot \cdot \cdot y_1 \cdot \cdot \cdot \cdot \cdot \cdot \cdot \cdot \cdot \cdot \cdot \cdot \cdot \cdot \cdot \cdot \cdot \cdot \cdot$	0.088	0.091	0.094 0.824	0.097	0.10	0.105 0.103 0.803 32·3	0.106	0.109	0.1

The last line shows the proper assignment of thermal unifor this condition. For simplicity both y and  $y_1$  are assume to vary uniformly, but other variations can be worked out with a little more trouble. Evidently the sum of the figures in the last line should be equal to

$$9 \times 32 = 288;$$

it is a trifle larger in the table.

Now it is probable that the best values of the factor for friction and resistance are to be derived from investigations on turbin rather than from separate experiments on nozzles and vane and it is evident that the use of the methods of representing the friction by a factor y is rather a crude way of trying to attain a new design favorable conditions found in a turbine alread built.

Since the general conditions of this problem are the same those on page 481, the efficiency due to adiabatic action will the same as is also the efficiency due to the angles and velocities. Taking the factors for friction in the guides and blades as each

o.1, the corresponding factors are 0.9 and 0.9. The efficiency due to velocities is 0.75, and the mechanical efficiency may be estimated as 0.9. The combined efficiency of the turbine is

$$0.262 \times 0.75 \times 0.9 \times 0.9 \times 0.9 = 0.143$$

A computation like that on page 483 with this efficiency gives for the probable steam consumption 16.2 pounds per brake horse-power per hour.

Assume that the turbine is to deliver 500 brake horse-power; then the steam consumption per second will be

$$16.2 \times 500 \div 3600 = 2.25$$
 pounds.

We can now determine the principal dimensions of the turbine to suit the conditions of its use. Suppose that it is desired to restrict the revolutions to 1200 per minute or 20 per second; then with nine stages and a peripheral velocity of 520 for the vanes the diameter will be

$$520 \div 20\pi = 8.28$$
 feet.

For a turbine of the power assigned this diameter will be found to be inconveniently large. If, however, the number of stages can be made 36, the velocity will be reduced to 260 feet per second as computed on page 495. This will give for the diameter

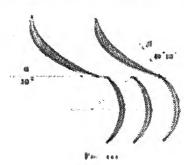
$$260 \div 20\pi = 4.14 \text{ feet.}$$

The remainder of our calculation will be carried out on these assumptions, namely, that the power is to be 500 brake-horse-power, and that there are to be 36 stages. If the method of the table on page 497 were applied to a turbine having the full 36 stages now contemplated, it would have 37 lines; namely, the ten already set down, and three intermediate entries between each pair of consecutive lines; but the temperatures found in that table would be found in the more extended table together with their specific volumes. We can, therefore, use that table to calculate areas and lengths of vanes for 9 out of the 36 stages,

which will suffice for illustration. Heginning with the lowest stage the area to be supplied will be

where boo is the velocity of the jet computed on page 493.

The circumference of a circle having the diameter of 4.14 fee is 13 feet; but of this a portion, one fourth or one third, must be assigned to the thickness of the guides. If we take one fourth



in this case the effective perimeter becomes 1.75 feet. But as is evident from Fig. 222 the periphera space assigned to the distance between guides must be multiplied by our a morder to find the effective opening. As a ro taken to be 10°, the sine is one half, so that the total width of spaces between guides to reduced to 4 % feet. The

radial length of the gunles for the last stage will consequently be

provided that there is full peripheral admission to the guides,

Now the angles for this case are the same as those on page 481 and J is 40° 16'. Consequently the relative velocity is

$$V_3 = V_4 \sin \alpha + \sin \beta = 600 \sin 40^\circ + \sin 49^\circ + 60^\circ = 507$$
 feet.

If the passages between the vanes are made of constant width as shown in Fig. 111, the effective perimeter will be the entire perimeter of the wheel less the allowance for this kness. As allowance like that for the guides will make the sames shorter than the guides in this case. Let us ter making the thickness equal to a space, then the effective perimeter will be 6 \$ feet. If the density of the steam is assumed to be constant for a giver stage, then the lengths of the guides and sames will be inversely as the product of the achorities by the effective perimeters, we that the length of the same will be

Conversely, if desired, the thickness of the vanes could be adjusted to give the same length. Such a construction as this leads to is likely to give too sharp a curvature to the backs of the vanes, and it may be better to give only the thickness demanded for strength and take the chance that the passage between the vanes shall not be filled. If allowance is made for friction and the consequent reduction in velocity the lengths of the vanes should be correspondingly increased.

The lengths of the guides for the other stages will be directly proportional to the specific volumes in the table on page 497, because the velocities have been made the same for all the stages. For example, at 100° the length for full admission will be

which will be the proper length for the twenty-fourth stage. If it is considered undesirable to further reduce the length we may resort to admitting steam through guides for only a portion of the periphery. Making the arc of admission vary as the specific volumes, the fourth stage (line 1 of the table on page 497) will have admission for

Intermediate lengths of vanes and arcs of admission may be computed by filling out a table like that on page 497 for all the stages, or a diagram may be drawn from which the required information can be had by interpolation; the values on the line numbered o are for this purpose, there being of course no corresponding stage. In fact the method of computing at convenient intervals and interpolating from curves is likely to be more accurate as well as more convenient, as the error of adiabatic calculations for steam with small change of temperature is liable to be excessive.

Leakage and Radiation. This type of turbine, as will be seen in the description of the Rateau turbine, has a number of wheels each in its own chamber, and the chambers are separated by stationary disks that extend to the shaft. Reduction of leakage must be attained by a small clearance between the disk and the

shaft for a proper bearing or stuffing how cannot be placed in so inaccessible a place. The leakage can be estimated by aid of Rankine's equation on page 432 or from Rateau's experiments on page 433; but both methods are likely to give results that are too large, and a factor less than unity should be applied; but the value of such a factor for a long, narrow, annular passage is not known, and any estimate must be a fude. For a turbine of the Rateau type the leakage is likely to be less than five per cen at the high pressure end. Now the leakage is proportional nearly to the difference of pressure between successive chambers and as the difference decreases so also does the leakage till it becomes of no account at the lower end. To allow for leakage the length of guides of the art of admission may be increased a the high pressure end of the turbane. There does not appear to be any information concerning the radiation from steam turbines. On the one hand the area of tashating surface is larger than for steam engines and on the other the temperature are less for the greater part if and all of that area. For compac steam engines the radiation is likely to be from twe to ten pe cent. For turbines of the Rateau and Curtis types the effecof radiation is to require larger areas in guides and passages at the high premater end.

Lead. Turbines with pressure compounding usually have some space between the vanes of one wheel and the nex set of guides or nozzles, and consequently the absolute exit velocity is mainly if not entirely dissipated, so that the steam enters those nozzles with no appreciable velocity. If this action is complete it would appear to be of little consequence where the guides or nozzles are placed. Nevertheless considerable importance is attached to locating the guides so that steam from the wheel shall flow directly into them. Clearly, as it takes as appreciable time to flow through the passages between the vanes, the steam will be discharged at some distance from the place at which it was received and the general path of the steam is a spiral wound around the turbine case in the direction or rotation.

Let abede represent a vane which has steam entering it tangentially with the velocity  $V_2$ , while it has itself the velocity

I'. Assuming that the relative velocity is constant we may divide the curve into a number of equal small parts that are approximately straight. From b lay off

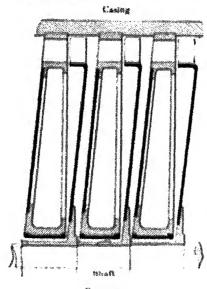
$$bb^* = ab = \frac{V}{V_a}$$



then b' will be a point in the trajectory of the particle of steam. In like manner  $ee' = 2ab \frac{V}{V_n}$ , etc.

The path alte'd'e' may be taken as the trajectory of the steam, and ere' is the lead as defined above. Properly a similar construction should be made also for the back of the vane, and the mean path should be taken to establish the lead. Extreme refinement is probably neither necessary nor justifiable in this work.

Rateau Turbine. The construction of this turbine, which is



of the pure pressure-compound type is represented by Fig. 113. which is a half section through the shaft, wheels and casing. The wheels are light dished plates which are secured to hubs that are pressed onto the shaft and which carry the moving vanes. The chambers are separated by diaphragms of plate steel, riveted to a rim and to a hub casting. The hubs are bushed with antifriction metal that is expected to wear away if it by chance touches the shaft. This turbine is sometimes divided into

two sections to provide a middle bearing for the shaft, which has considerable length and should preferably have a small

diameter to reduce leakage. The high pressure portion may have a smaller diameter to farilitate arrangement of guides and vanes. Sometimes there are three diameters for the same purpose. But little extra complication of computation is introduced by such change of diameter; all that is necessary is to make the portion of available heat per stage larger in proportion to the increase in peripheral speed.

# TESTS ON BATEAU IURDIST

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The accompanying table gives results of tests on a Rateau turbine by Professor Stodola. To compare with results from steam-engines, these latter should be referred to brake horse-power, with a mechanical efficiency of 6.5% to 6.96.

This type of turbine has been applied our esolully to use exhaust steam from reciprocating engines which for some purpose exhaust at atmospheric pressure or into a poor vacuum. Such application can, however, be but local or acculental

Steam Friction of Rotating Disks. The resistance which a turbine wheel experiences while rotating in steam can be divided into two parts: first, that due to the friction of the smooth disk and second, that due to the action of the sames, which have an effect comparable to that of a centrifugal pump.

From a consideration of tests made by Culcil t on cardboard disks, and by Lewicki I on a de Labal turbuse wheel driven it

<sup>\*</sup> Stogen Turbines, trans. Its 1. 1 Tamenatein

P. Engineering, January, 1904. I Lestiche if V. Joudsch Ing. 2902

its casing, and from tests of his own, Professor Stodola gives the following equations for the horse-power required to drive smooth wheels and to drive wheels with vanes forward:

Smooth wheels

H.P. =0.02295 
$$\alpha_1 D^{2.5} \left( \frac{V}{100} \right)^{\circ} \gamma$$
.

Wheels with vanes

H.P. = 
$$[0.02295 \ \alpha_1 D^{2.5} + 1.4346 \ \alpha_2 L^{1.25}] \left(\frac{V}{100}\right)^3 \gamma$$

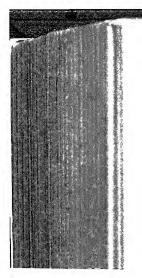
where D is the diameter in feet, L is the blade length in inches, V is the peripheral speed in feet per second, and  $\gamma$  is the density of the medium. The values of the other factors are

$$\alpha_1 = 3.14$$
  $\alpha_2 = 0.42$ .

These formulæ explain why the backing turbine for marine propulsion is always run in a vacuum when idle.

Turbines which have only a partial admission must be affected by some such action for that part of the revolution during which steam is not admitted; but this matter is obscure and such a resistance must be combined with friction and other resistances. It is therefore very difficult to assign the proper value to the friction factor y for steam in the vanes or in the guides and vanes of a velocity-compound turbine. In particular any change of the angle  $\gamma$  (Fig. 103, page 480) to avoid end thrust must be made with caution and should be checked by experiment.

Side Thrust. — If admission is restricted to only a part of the periphery of a turbine, then in order to preserve a balance and avoid unnecessary pressure on the bearings of the shaft, the arc of admission should be divided into two equal portions, that are diametrically opposite. Some builders, however, prefer to ignore this effect, and concentrate the admission at one side, because there is tendency for the steam to spread which will have double the effect if the arc is divided as suggested. The amount of side thrust can be estimated from the powers developed at the several wheels, having partial admission, together with the dimensions and speed of revolutions, making allowance of course for the distribution of the torque over an arc of a circle.



Pressure and Velocity Compounding. A favorable companies tion may be made of the two methods of compounding attending in that is, the pressure and temperature range tracks divided between two or more chambers in each of which attantive two or three sets of moving vanes. This has been dones are large scale with the Curtis turbine which appears to have at secitarnee of economical application than any other type.

Since the principles of each method have been disa an already, we will illustrate the application to a comparingly simple problem avoiding too great minutic of detail.

Let us take for the principle conditions the delivery of \$ 000 \$ watts of electrical energy, which, with an efficients of the electrical energy which, with an efficients of the electrical energy of about 0.0, will correspond to nearly 770 brake horse present

Let the initial pressure be 150 pounds by the gauge, as say, vacuum be 28 inches of menury. Let the angle of the record be  $x \to 20^\circ$ . The absolute pressures will be about 105 gauge and one pound absolute, and the compounding temperature  $300^\circ$  and  $100^\circ$  F. Dry saturated steam at the given gauge will have nearly 1.30 units of entropy, and for this the temperature entropy table gives for adiabatic expansion with the above  $20^\circ$  of temperature the heat contents as 1104 and 871. There we of  $q_2$  is 70 at the lower temperature, and consequently is equal to for n.r.t.

The thermal efficiency of adiabatic expansion without attawn for any losses is

the corresponding heat consumption is

per horse power per minute.

The efficiency for the turbine without friction by wagnast (291), page 481 is

The efficiency of the mazzles has already been determinant. A 0.85 by the selection of 0.15 for y. Let us further assurance

the combined effect of losses in the vanes may be taken to be equivalent to making  $y_0$  equal to 25 so that  $x_0 = 0.75$ ; this is in effect the efficiency factor for the vanes as affected by friction. If, further, we take the mechanical efficiency of the machine as 0.9, then the combined efficiency for the turbine will be

$$0.285 \times 0.883 \times 0.85 \times 0.75 \times 0.9 = 0.144$$

This corresponds to

$$42.42 \div 0.144 = 205 B.T.U.$$

per horse-power per minute. Now it costs to make steam from water at  $102^{\circ}$ , and at an absolute pressure of 165 pounds, 1123  $(r_1 + q_1 - q_2)$  thermal units, as already calculated in the deduction of the efficiency of adiabatic action. Consequently the steam per horse-power per hour will be

$$295 \times 60 \div 1123 = 15.7$$

pounds per brake horse-power per hour. To this should properly be added a fraction, to allow for leakage and radiation, amounting to five or ten per cent; this added amount of steam will affect the size of the high pressure nozzles only in this case, and as extra nozzles are sure to be provided we will take no further account of it than to say that the steam consumption may amount to 16.5 to 17.3 pounds per brake horse-power per hour.

The heat contents which have already been found give for the adiabatic available heat

$$1193 - 871 = 322,$$

and if this be divided equally we have 161 thermal units per stage. Using 0.15 for y in the nozzles, the velocity of the jet becomes

$$V = \sqrt{2 \times 32.2 \times 778 \times 161 \times 0.85} = 2610$$

feet per second.

Assuming that we may use three sets of moving vanes the velocity for them will be

$$2610 \div (2 \times 3) = 435$$

feet per second.

If we choose a diameter of 4½ feet for the pitch surface of the vanes it will lead to the use of 1850 revolutions per minute.

To find the intermediate pressure we may take for the heacontents at that pressure

which in the temperature entropy table corresponds to agg F, or 18.2 pounds. Since the back pressure for the nozzles is relatively small in each case, the nozzles will have throats for which the velocities must be determined in order to find the areas. The throat pressures may be taken to be

and the corresponding temperatures are 424" and 1969 F.

Since the rounding of the nozzle is likely to give but small area for friction compared with the cone for expanding to the back-pressure, we may assume adiabatic expansion to the threa and allow the entire value of y = 0.15 for the computation for the exit. This appears to agree with tests showing that such nozzles give nearly full theoretical discharge. The heat content by the temperature entropy table at entropy 1.50 and 324° F amounts to 1149 B.T.C., the value of x is 0.964 and the specific volume is 4.45 cubic feet. The apparent available heat is

giving a throat velocity of

The apparent available heat for producing velocity at the exiwith y taken at 0.14 is

leaving for the available heat

The heat of the liquid is 191 so that with 939 for e we have

$$x' - x'y' + y' - \exp(6 - \exp(1 + \exp g) - \exp g)$$

The specific volume is

$$v = (xu + \sigma) = 0.902 (21.6 - 0.016) + 0.016 = 19.5.$$

With 15.7 pounds of steam per brake horse-power per hour and 770 horse-power the steam per second is

$$w = 15.7 \times 770 \div 3600 = 3.36$$
 pounds.

The combined area of discharge of all the first stage nozzles is therefore, with the velocity at exit equal to 2610 feet,

$$3.36 \times 19.5 \times 144 \div 2610 = 3.62$$
 square inches.

The nozzles of turbines of this type are sometimes made square at the exit so as to give a continuous sheet of steam to act on the vanes. If the side of such a nozzle were made half an inch there would appear to be fourteen and a half such nozzles; the turbines would probably be given 16 or 18 of them, which could be arranged in two groups. Since the angle of the nozzle is 20° the width of the jet measured along the perimeter of the wheel will be

$$0.5 \div \sin 20^{\circ} = 0.5 \div 0.3420 = 1.46$$
 inch.

Allowing one-fourth of the width of the orifice for the thickness of the walls, the width occupied by eight nozzles would be

$$1.46 \times 1.25 \times 8 = 14\frac{1}{2}$$
 inches.

The combined throat area of all the nozzles will be

$$3.36 \times 4.45 \times 144 \div 1480 = 1.41$$
 square inch.

Dividing by  $14\frac{1}{2}$ , the number of necessary nozzles, gives for the throat area of one nozzle

$$1.41 \div 14.5 = 0.0972$$
 square inch,

so that the diameter will be about 0.35 of an inch.

A method of calculation for the second set of nozzles consistent with the method of determining the intermediate pressure is as follows: The pressure in the throat has already been found to be 10.6 pounds, corresponding to 196° F., for which the temperature-entropy table at 1.56 units of entropy gives for heat

contents 908. The heat contents at 18.2 pounds (223) has already been found to be 1032, so that the available heat for adiabatic flow appears to be 34 n.f.v., which gives for the velocity in the throat

The next step is the determination of the qualities at the throat and exit, and from them the specific volumes. Now of the 161 n.r.v. available for adiabatic flow in the first nozzles only a part has actually been changed into work, because there was allowed 0.15 for friction in the nozzle, and 0.24 for losses in the guides and vanes, while the efficiency due to angles and velocities was 0.883. The heat changed into work was therefore

Consequently the heat left in the steam as it approaches the second nozzle is

per pound. Now r has the value 959 at 223 F., and q is 191,80 that the quality is

$$x = (110) = 101) : 000 = 0.000.$$

If the flow from the entrance to the throat 34 s.r.v. are assumed to be changed into kinetic energy leaving for

and as r is equal to 978 and q is 164 at 196° F., we have

at the throat of the second nozzle,

Allowing as before 0.15 for the friction of the nozzle there will be

changed into kinetic energy for the entire nozzle leaving

and at a pound or 102° F., the values of r and y are 1043 and 70

at exit from the second set of nozzles. The volume of saturated steam at  $102^{\circ}$  is 335 cubic feet, and with x equal to 0.858 the specific volume is 288 cubic feet. Consequently, with a weight of 3.36 pounds per second, and a velocity of 2610 feet, the united areas of all the nozzles at exit will be

$$3.36 \times 288 \times 144 \div 2610 = 53.4$$
 square inches.

Now the perimeter of a circle having a diameter of  $4\frac{1}{2}$  feet is about 170 inches. Allowing for the sine of the angle 20° and one-fourth for thickness of guides there will be about 43.5 inches for the united width of passages between guides so that the radial length will be

$$53.4 \div 43.5 = 1.23$$
 inch.

The specific volume of saturated steam at 197° is 35.5 cubic feet, so that with x equal to 0.925 the specific volume is 32.9. Now the areas are proportional to the specific volumes and inversely as the velocities, consequently the length of guides at the throat is

$$1.27 \times \frac{2610}{1300} \times \frac{32.0}{288} = 0.29$$
 inch.

The length of the vanes and guides can be found by the method on page 500, using relative velocities for the vanes and absolute velocities for the guides. The velocities decrease as indicated by Fig. 107, page 487, and the lengths must be correspondingly increased. In this case, however, there are two considerations which influences the lengths that should be finally assigned to the guides and vanes. (1) The thickness may be diminished, which tends to decrease the length. (2) Friction reduces the velocity which tends to increase the length. Friction of course diminishes all velocities including the peripheral velocity of the wheel, but a proper discussion of that matter would be both long and uncertain-

Attention has already been called to the defect of this method of making all the calculations at a single value of entropy and trying to allow for friction and other losses by simple factors. The difficulty is aggravated in this case by the fact that the

second set of nozzles or guides have proper throats. The proper method after having selected a set of intermediate pressures appears to be to calculate the turbine step by step. The steam supplied to the second set of nozzles (or guides) has been found to have the quality 0.950, and this is probably a good approximation to the actual condition, even if allowance is made for radiation and leakage. The temperature-entropy table gives for steam having that quality and the temperature 223, the entropy as nearly 1.66. At that entropy the heat contents at the initial, throat and exit pressures, are given in the following table with also the quality and specific volume at the throat; the table also gives the quality and specific volumes at exit with y equal to 0.15.

Pressure.	Temperature.	Heat contents.	Quality.	Specific volume.
18.2 10.6 1.0	223 196 102	1100 1063 927	0.95 0.92 0.85	32·7 245

The apparent available heaf for adiabatic flow to the throat is now

$$1101 - 1063 = 37$$

which would give a velocity of

$$V = \sqrt{2 \times 32.2 \times 778 \times 37} = 1360,$$

instead of 1280 as previously found. The apparent available heat to the exit with 0.15 for the friction factor is now

$$(1101 - 927) 0.85 = 147,$$

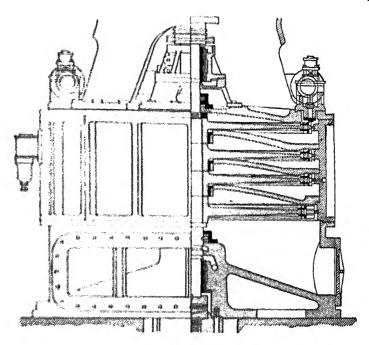
which gives for the exit velocity

$$V = \sqrt{2 \times 32.2 \times 778 \times 147} = 2710,$$

instead of 2610 previously computed.

This comparison shows that the intermediate pressure determined by the customary method will be too high, and that to obtain the desired distribution of temperature the factors for the lower stages must be modified arbitrarily as may be determined by comparison with practice.

Curtis Turbine. Fig. 114 shows a partial elevation and section of the essential features of a Curtis turbine, which has four chambers and two sets of moving vanes in each chamber. The axis of the turbine is vertical which demands an end bearing, the difficulties of which construction appear to have been met by



Pitt. Tra-

pumping oil under pressure into the bearing, so that there is complete lubrication without contact of metal on metal. The condenser is placed directly under the turbine, and the electric-generator is above on a continuation of the shaft. The arrangement appears to be convenient, and in particular to demand small floor space only.

When used for marine propulsion the Curtis turbine has a horizontal shaft from necessity, and has a large number of stages.

A turbine developing 8000 horse-power has seven pressure stages, each of which but the first has three velocity stages, that one has four velocity stages. The diameter is ten feet and the peripheral velocity is 180 feet per second.

Tests on Curtis Turbines. — The following tables give tests on two Curtis turbines, having two and four pressure stages, respectively; both were made by students at the Massachusetts Institute of Technology.

TESTS ON A TWO-STAGE CURTIS TURBINE.

#### DARLING AND COOPER.\*

Duration minutes	120 146.3	120 145.3	120	120	60 149.3
Throttle temperature F	512	520	464	502	512
Barometer inches	29.8	29.9	29.9	29.9	30.0
Exhaust pressure absolute pounds	0.82			0.84	
Load kilowatts	161.4	255.7	374.0	512.9	731.9
Steam per kilowatt hour, pounds	21.98	19.63	19.98		17.75
Thermal units kilowatt minute	440	396	392	369	357

If the efficiency of the dynamo is taken at 0.9 and one kilowatt is rated as 1.34 horse-power, the steam and heat consumptions per brake horse-power are, for the best result,

11.8 pounds

239 B.T.U.

#### TESTS ON A FOUR-STAGE CURTIS TURBINE

### COE AND TRASK.†

<sup>\*</sup> Thesis, M. I. T., 1905.

<sup>†</sup> Thesis, M. I. T., 1906.

Taking the efficiency of the dynamo as 0.9 and a kilowatt as 1.34 horse power, the best result is equivalent to a steam consumption of 12.6 pounds and a heat consumption of 237 thermal units.

Reaction Turbines. The essential feature of a reaction turbine is a fall of pressure and a consequent increase of velocity in the passages among the vanes of the turbine. Since such wheels commonly are affected by impulse also they are sometimes called impulse-reaction wheels, but if properly understood the shorter name need not lead to confusion. In consequence of the feature named the

relative exit velocity  $V_a$  is greater than  $V_a$ . Another consequence is that steam leaks part the ends of the vanes which are usually open, and there is also leakage past the inner ends of the guides which are also open; this feature  $\mathbb{Z}$  is shown by Fig. 115.

The reaction turbine is always made compound with a large number of stages, one set of guides and the following set of vanes being counted as a stage. In consequence the exit pressure either from the guides or the vanes is

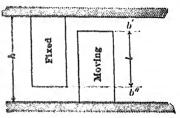




Fig. 115.

only a little less than the entrance pressure, and the passages are all converging.

There is no attempt to avoid axial thrust, and therefore the exit angle  $\gamma$  from the vanes may be made small; it is commonly equal to the exit angle  $\alpha$  from the guides. A common value for these angles is  $zo^{\circ}$ .

The guides and vanes follow alternately in close succession leaving only the necessary clearance; the kinetic energy due to the absolute exit velocity from a given set of vanes is not lost but is available in the next set of guides. The turbines are usually

made in two or three sections as shown by Fig. 117, page 326, and it is only at the end of a section that the kinetic energy due to the absolute exit velocity is rejected, at the end of a section this kinetic energy is changed into heat and is in a manner available for the next section; at the end of the turbine it is of course wasted. Since there are usually sixty stages or more the influence of the kinetic energy rejected is likely to be less than five per cent and it may properly be combined with the general factor to allow for friction and leakage past the ends of the guides and values. Both influences resince the change of heat into work applied to the turbine and increase the value of the quality cand also of the specials solutine of the mixture of steam and moisture.

Since the exit absolute schools from the sames is applied to driving the steam into the next set of guides, there is no direct advantage in avoiding schools of which at this place, it is only necessary to give the guides the proper angle at entrance to receive the steam. Indirectly it is disadvantageous to have a high velocity at the entrance to the guides, or, for that matter, in any part of the turbine, as the friction is probably proportional to the square of the velocity as has been assumed in the use of the friction factor y.

The steam enters a set of guides with a certain velocity, i.e., the exit absolute velocity from the preceding set of vines. On account of the loss of pressure in the guides a certain amount of heat is changed into kinetic energy and the equivalent increase of velocity may be added to the entrance velocity to find the exit velocity which is of course an absolute selecity. This absolute velocity combined with the schoolity of the blades gives the relative entrance velocity is to be added the gain in velocity also to change of heat into kinetic energy in the sames, in order to had the relative exit velocity. The ratio of the heat used in the sames to that used in the entire stage is called the degree of reaction. Commonly the degree of reaction is one half; that is, the amount of heat used in the values is equal to that used in the guides; and

the gain of velocity in the vanes is equal to the gain in the guides.

In Fig. 116 let  $V_1$  be the velocity of the steam leaving the guides and V the velocity of the vanes; then  $V_2$  is the relative velocity of the steam entering the vanes.  $V_3$  is the relative exit velocity which is greater than  $V_2$  on account of the change of heat into work.  $V_4$  is the absolute exit velocity from the vanes with which the steam enters the next set of guides. If the conditions for successive stages are the same,  $V_4$  is also equal to the entrance velocity to the set of guides of the stage under discussion, and if ce is laid off at ac' then c'b is the gain of velocity in the

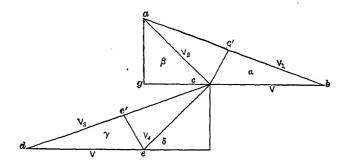


Fig. 116.

guides. Consequently to construct  $V_s$  we may lay off ce' equal to ac and e'd equal to c'b. Now a and  $\gamma$  are commonly made equal, and therefore the triangles abc and cde are equal. Consequently the angle  $\delta$  for the entrance to the guides is equal to  $\beta$  at the entrance to the vanes. In fact the guides and vanes have the same form.

Choice of Conditions. — The foregoing discussion shows that the designer is given a wider latitude in his choice of conditions for the compound reaction turbines than appeared possible for impulse turbines, though if the restriction of no axial thrust were removed from the latter the comparison would be quite different.

The most authoritative statement of the preferable conditions in practice for reaction turbunes of the Parson's type is formed in a paper by Mr. E. M. Speakman,\* but much of the information in the hands of the builders "being based on long and costly experiments, much reticence is observed regarding their publication." The statement of practical conditions is therefore based on such information as can be gleaned from his paper, with obvious applications by ordinars methods. Factors for friction and leakage are largely conjectural, as must in fact be the case at present for all turbunes, and for our purpose may perhaps be limited to giving the student an idea of the nature of the problems.

The ratio of the velocity of the vanes to the velocity of the steam has varied in turbunes built by the Parsons Company from 0.25 to 0.85. In general the ratio may be taken as 0.6.

Three turkings are somally leads with two or three diameters of the revolving splinder or total an alcown on lag 117. The following tables give the practice of that company with regard to peripheral speed and number of stages

PARTING TABLES - BERETRE 61. MARK

North at well and	ş ş'a şêşikanını tyanı.		Shines look all	数は おる あおかけ
Biston affa	Promo o degladorio des	<b>装净板 电影撒娜2.4.1</b> 00	ない会議を対象	gus comme
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2.4	8.**	\$ 1-4-A	4.2	कु र संस्थेत

<sup>\*</sup> Frank Inst ling and they had adequate and elete, and elete,

## PARSONS TURBINE -- MARINE WORK.

Type all equant,	Peripheral per se	speed, feet cond.	Ratio of velocities,	Number
Hardware Court (1997) - Carron (1997) - The Court (1997) - Carron (1997) - Carron (1997)	H.P.	L.P.	vanes to steam.	shafts.
High speed mail steamers Intermediate mail steamers Channel steamers Rattleships and large cruisers Small cruisers Torpeds crafts	70-80 80-90 90-105 85-100 105-140 110-130	110-130 110-135 120-150 115-135 130-160	0.45-0.5 0.47-0.5 0.37-0.47 0.48-0.52 0.47-0.5	4 3-4 3 4 3-4 3-4

The Westinghouse Company have used much higher velocities of vanes for electrical work than given in the above tables; as much as 170 feet per second for the smallest cylinder and 375 for the largest cylinder.

The blade height should be at least three per cent of the diameter of the cylinder in order to avoid excessive leakage over the tips. Mr. Speakman says that leakage over the tips of the blades is perhaps not so detrimental on account of actual loss by leakage as because it upsets calculations regarding passages by increasing the steam volume.

The following equation represents Mr. Speakman's diagram for clearances over tips of vanes,

The proportions of blades may be taken from the following table:

PROPORTIONS OF BLADES—INCHES.

Mr. Parsons \* gives for the efficiency of the steam in the turbine blades themselves 0.70 to 0.80.

<sup>\*</sup> Inst. Naval Arch., 1903.

In addition to the leakage past the tipe of the blades whech and in practice be separated in its effects from frictioner is likely to be a considerable leakage past the bala pistons which will be described in connection with Fig. 1. This leakage is in the end direct to the condenser, and no acconnect be taken of it in the design of the blading of the turbibut allowance should be made in comparing theoretical calcutions with results of tests.

Design for a Reaction Turbine. Let us take for the prine conditions the delivery of 500 kilosatts of electrical energy, wh with an efficiency of the dynamic of about 0.9 will correspond 1770 brake horse power, as for the calculation on page 500, the initial pressure be 150 pounds by the gauge, and the vacable 28 inches. The absolute pressures corresponding are pounds and one pound, and the temperatures are 365%, 9 100.0 F. The calculation referred to gives for the their efficiency of adiabatic action 0.285, which corresponds 149 n.r.v. per horse-power per minute. If we allow 0.500 the turbine efficiency, and ten per cent for leakage to the denser and radiation, and take 0.9 for the mechanical efficience shall have for the combined efficiency of the turbine

This will give for the heat and steam consumption per hippower, 10,3 pounds per hour and 305 n.r. 10, per minute. There to be compared with results of tests to eletermine whithe constants assumed are proper.

For the estimate of the weight of steam to be used in dimining the dimensions of the tuclone we should omit the for leakage to condenser and radiation, which will give for steam per horse-power per hour 14.7 pounds. The weigh steam per second to be used in computing passage then becomes

Let the peripheral speed of the smallest exhiber be take 225 feet per second, and let the intermediate and low pre-

cylinders be 1½ and 2½ times the diameter of the small cylinders. Let the peripheral speed be 0.75 of the steam velocity, then the latter will be 300 feet per second. If the exit angles for guides and vanes be taken as 20° and if the degree of reaction is 0.5, the velocities and angles will be represented by Fig. 116, page 517. In that figure

$$gb = V_1 \cos 20^\circ = 0.940 \ V_1;$$
and as
$$V \text{ is } 0.75 \ V_1,$$
we have
$$gc = (0.940 - 0.75) \ V_1 = 0.190 \ V_1.$$
But
$$og = V_1 \sin 20^\circ = 0.342 \ V_1;$$
and
$$\tan \beta = 0.342 \ \ge 0.190 = 1.800 \ \therefore \beta = 61^\circ.$$

The angle f is given to the backs of the blades, and the angle at the faces is somewhat larger, as will appear by Fig. 115, page 515; in consequence there is some impulse at the entrance to the vanes. To get the relative velocity we have

$$V_3^3 - ag^3 + gc^3 = (0.342^3 + 0.190^2) V_1^2$$
  
 $\therefore V_3 - 0.392 V_1.$ 

But it is shown on page 517 that for the conditions chosen the increase of velocity in either guides or vanes is equal to

$$V_1 - V_2 - (1 - 0.392) V_1 - 0.608 \times 300 = 182$$

feet per second.

Now the equation for velocity when h thermal units are available is

$$V = \sqrt{2 \times 32.2 \times 778h},$$

and conversely

$$h = 183^2 + (64.4 \times 778) = 0.661 \text{ B.T.U.}$$

This is the amount with allowance for friction and leakage past the ends of the blades which has been assigned the factor o.o., so that for the preliminary adiabatic computation we may take for one set of blades

and for a stage, consisting of a set of guides and vanes, we may take for the basis of the determination of the proper number of stages 2.2 B.T.U. per pound of steam used.

It appears on page 507 that adiabatic expansion from 165 pounds absolute to one pound absolute gives 322 thermal units for the available heat. If this is to be distributed to the stages of a turbine with 2.2 units per stage, then the total number of stages will be

$$322 \div 2.2 = 146$$

stages. This is under the assumption that the turbine has a uniform diameter of rotor with 225 feet for the velocity of the vanes; we have, however, taken the intermediate diameter 1½ times the high-pressure and the low-pressure 2½ times. The peripheral velocities will have the same ratios, and the amounts of available heat per stage will be proportional to the squares of those ratios, namely, 2.25 and 6.25. Consequently the amounts of heat assigned per stage will be as follows:

High-pressure Intermediate Low-pressure.

2.2
4.95
13.75

If we decide to use ten low-pressures and twenty intermediate stages they will require

$$10 \times 13.75 + 20 \times 4.95 = 236.5 \text{ B.T.U.},$$

leaving 85.5 thermal units which will require somewhat less than 39 stages. Reversing the operation it appears that one distribution calls for

$$10 \times 13.75 + 20 \times 4.95 + 39 \times 2.2 = 322 \text{ B.t.u.}$$

For convenience of manufacture it is customary to make several stages identical, that is, with the same length of blades, clearances, etc.; this of course will derange the velocities to some extent and interfere with the realization of the best economy. That part of the cylinder which has the same length of blades is known technically as a barrel. Let there be three barrels for each cylinder, making nine in all, which may be conveniently numbered, beginning at the high-pressure end and may have

the number of stages assigned above. In that table is given also the number of the stage counting from the high-pressure end, which is at or near the middle of the length of the barrel, for which calculations will be made. The values of the heat contents xr + q are readily found for each stage given in the table by subtracting the amounts of heat changed into kinetic energy, down to that stage, allowing 2.2 for each stage of the high-

### COMPOUND REACTION TURBINE.

Charles	AND THE COMMENT OF TH	New Arthur	Middle Mide	- Temprestur.	- Pressure.	4 Heat contents 4 adiabatic	Heat consents + protestic.	~ Heat of liquid.	e Heat of vaporization.	4 Quality.	Spec	Length of blades.
II	1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1	A TABLE OF THE PARTY OF THE PAR	THE SECOND SECON	151 5 101 5 101 5 270 1 280 6 110 1 111 5	136 7 04 8 64 7 41 6 25 1 15 0 8 61 2 04 1 12	1177 0 1140.3 1140.3 1140.7 1687 7 1683 0 1624.3 981 0 981 0 981 0	1184 1167 1140 1130 1100 1001 1008	305 208 330 200 184 151 100 80	867 886 985 985 946 964 987 1016 1046	. 905 . 984 . 975 . 963 . 959 . 941 . 927 . 910 . 896	3.20 4.50 6.52 0.04 16.0 24.8 47.1 120.4 257	0.572

pressure cylinder, 4.05 for each intermediate stage and 13.75 for each low-pressure stage. For example, the fiftieth stage has its heat contents found by subtracting from the initial heat contents 1193, the amount

leaving for the heat contents after that stage 1053 thermal units. The probable heat contents allowing for friction and leakage is found by subtracting the product of the above quantity by the factor 0.6. Giving

Having the values of x'r + q obtained in this way, the values of x' can be found by subtracting the heat of the liquid q, and

will lar

dividing the remainder by r. Finally the specific volumes are computed by the equation

but in practice of may be neglected giving

because we have either x nearly equal to unity or else  $\epsilon$  will be larger compared with  $\alpha$ .

The steam velocity for the first cylinder is 100 feet per second the weight of steam per second is 1.15 pounds and the specific volume at the seventh stage, i.e., the middle of the first barrel is 3.27 cubic feet. The effective area must therefore be

$$a = 144 \frac{47}{V} - 144 \frac{3.15}{1.00} = 4.57 - 4.91$$
 square inches.

To this must be added a fraction of one-third or one-fourth to allow for the thickness of the blades, and the result must be divided by sine  $\alpha$  in order to find the area of the peripheraring through which the steam will flow. Taking one-fourth for the fraction in this case, and  $\infty$  for  $\alpha$ , we have

It is recommended that the height of the blades shall be 0.0; of the diameter, which gives for the expression for the peripheraring

$$0.03 \text{ eV} - 18.1$$
.

 $\therefore d - 18.1 = 0.01 = -11.85 \text{ in her.}$ 

The diameters of the intermediate and low pressure cylinder

$$d_4 = i 3.85 \times i.5 = 20.77 \text{ in.; } d_7 = i 3.85 + 23 = 34.63 \text{ in.}$$

The length of blade at the seventh stage will be

and this length will be assigned to all the blades of the first barrel. The blades of the second and third barrels will have their lengths increased in proportion to the specific volumes at the middle of those barrels, as set down in the table. The effect of increasing the diameters of the intermediate and low-pressure cylinders is to increase the steam velocity, and the peripheral length of the steam passage, both in proportion to the diameter. Consequently the lengths of the blades for these cylinders are directly proportional to the proper specific volumes and inversely proportional to the squares of the diameters. Thus the length of the blades at the forty-second stage, i.e., the middle of the fourth barrel is

$$\frac{0.415 \times 0.43}{3.27 \times 1.5^2}$$
 = 0.532 inch.

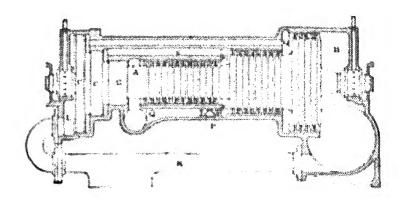
The lengths are computed for the other barrels in the same way, using 2.5 for the ratio of the low-pressure diameter.

Since the diameter of the small cylinder is 13.85 inches and the speed of the vanes on it is 225 feet per second, the revolutions per minute are

$$\frac{225 \times 60 \times 12}{13.85 \pi} \approx 3750.$$

Parsons Turbine. — The essential features of the Parsons turbine are shown by Fig. 117. Steam is admitted at A and passes in succession through the stages on the high-pressure cylinder, and thence through the passage at E to the stages of the intermediate cylinder; after passing through the intermediate stages it passes through G to the low-pressure stages and finally by B to the condenser.

The axial thrust is counterbalanced by the dummy cylinders, C, C, the first receiving steam from the supply directly, the second from the passage between the high and intermediate cylinders through the pipe F, and the third through the pipe near G from the passage between the intermediate and low-pressure cylinders. Leakage past the dummy cylinders is checked by labyrinth packing, which is variously arranged to give a succession



S'e. . . . . .

of spaces through which the steam must pass with narrow passages, which throttle the steam as it passes from chamber to hamber. One method is to let narrow strips of brass into the surface of the cylinder and into the surface of the case these strips are adjusted to leave a very small axial clearance so that the steam is strongly throttled as it passes through, is reported that the labyrinth clearance is entirely successful i reducing the leakage past the dummy cylinder to a small amount it is pointed out by Mr. Jude that the most effective throttlin is at the last section of the labyrinth, and that the other section are comparatively inefficient. This feature will be evident if a attempt is made to calculate the loss by continual application of Rankine's equations, page 432. Of course such a method can but crude, and yet its indications should be of value for estimatin leakage which should be small.

When applied to marine propulsion the dummy pistons are omitted and the axial thrust is usefully applied to the propuller shaft. Since an absolute balance cannot be obtained, a thrust bearing is provided but it may have small bearing area and withave but little friction. Stationary turbines also have a bearing for residual unbalanced thrust.

Test on a Parsons Turbine. A test on a Westinghouse

Parsons turbine in Savannah was made under the direction of Mr. B. R. T. Collins and reported by Messrs. H. O. C. Isenberg and J. Lage,\* which is interesting because the steam consumption of the auxiliary machines was determined separately. The data and results of tests on the turbine are given in the following table.

The tests made at full load with varying degrees of vacuum show clearly the advantage obtained in this machine from a good vacuum, which amounted to a saving of

$$\frac{289 - 279}{289} = 0.035.$$

TESTS ON WESTINGHOUSE-PARSONS TURBINE.

COLLINS, ISENBERG AND LAGE.

	load.	1 load.	ıl load.	1 load.			
Duration minutes Steam pressures, gauge Vacuum inches Revolutions per minute	60 131 28.1 3616 260	3601		60 127 26.7 3612 501	60 · 128 28.0 3562 499	45 127 26.7 3540 620	45 125 26.6 3537 733
Steam consumption, pounds per kilowatt-hour per electric h.p. per hour . Heat consumption B.T.U. per kilowatt-minute per horse-power per minute	24.3 18.1 462 345		20.7	19.8	19.7	19.8	20.2

A great importance is attributed by turbine builders to obtaining a low vacuum, in many cases special air-pumps and other devices being used for that purpose. Unless discretion is shown both in the design and operation of this auxiliary machinery, its size and steam consumption is likely to be excessive, and what appears to be gained from the vacuum may be entirely illusory.

<sup>\*</sup> Thesis, M.I.T. 1906.

The steam consumption in pounds per hour for the several auxiliary machines was as follows:

Centrifugal pum	p for	£ 1	reti	Lati	ng	15,	iter		•	٠	,	881
Dry vacuum pun	ų.		•					•	٠	•		212
Hot-well pump		*	,			,				*		
											1	115.8

This total was equivalent to o.rrs of the steam consumption of the turbine at full load and with 28 inches vacuum. Some tests of turbine installations show twice or three times this proportion.

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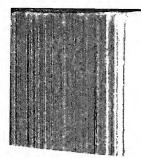
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